

Specialization and Task Allocation

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Simple Threshold Model

- ▶ No changing polyethism/specialization
- ▶ No strong task specialization within castes
- ▶ Valid only when thresholds are constant
- ▶ No ability to adapt to changing ages



Overcoming Limitations

- ▶ Two possibilities
 - ▶ Varying thresholds
 - ▶ Age based changes



Varying Thresholds

$$T_{\theta_{ij}}(s_j) = \frac{s_j^2}{s_j^2 + \theta_{ij}^2}$$

If i performs task j :

$$\theta_{ij} \leftarrow \theta_{ij} - \xi \Delta t$$

If i does not perform task j :

$$\theta_{ij} \leftarrow \theta_{ij} + \varphi \Delta t$$

Overall:

$$\theta_{ij} \leftarrow \theta_{ij} - x_{ij} \xi \Delta t + (1 - x_{ij}) \varphi \Delta t$$

$$\partial_t \theta_{ij} = [(1 - x_{ij}) \varphi - x_{ij} \xi] \Theta(\theta_{ij} - \theta_{\min}) \Theta(\theta_{\max} - \theta_{ij})$$



Varying Thresholds

Change in time taken for a task:

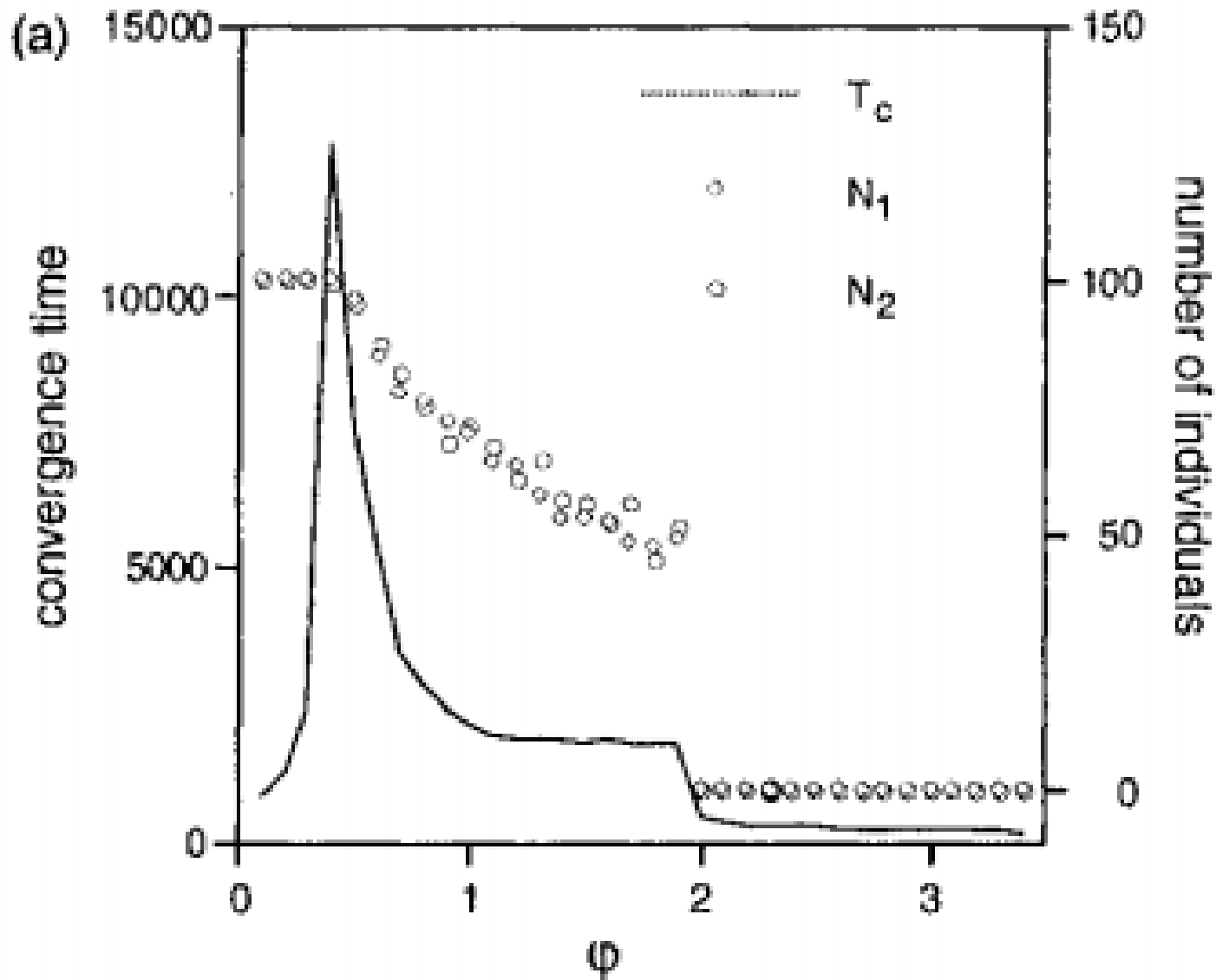
$$\partial_t x_{ij} = T_{\theta_{ij}}(s_j) \left(1 - \sum_{k=1}^m x_{ik} \right) - px_{ij} + \psi(i, j, t)$$

Change in stimuli:

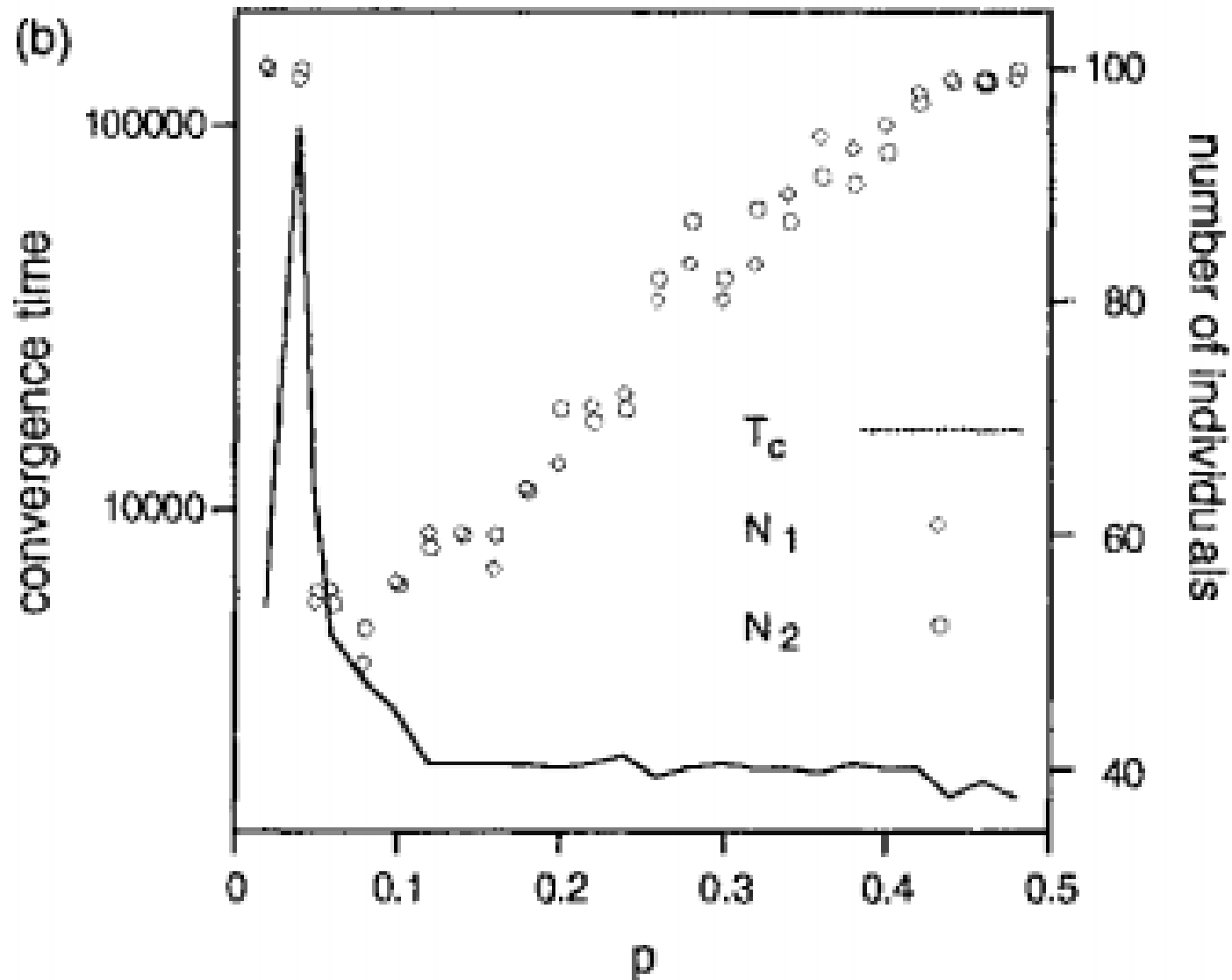
$$\partial_t s_j = \delta - \frac{\alpha_j}{N} \left(\sum_{i=1}^N x_{ij} \right)$$



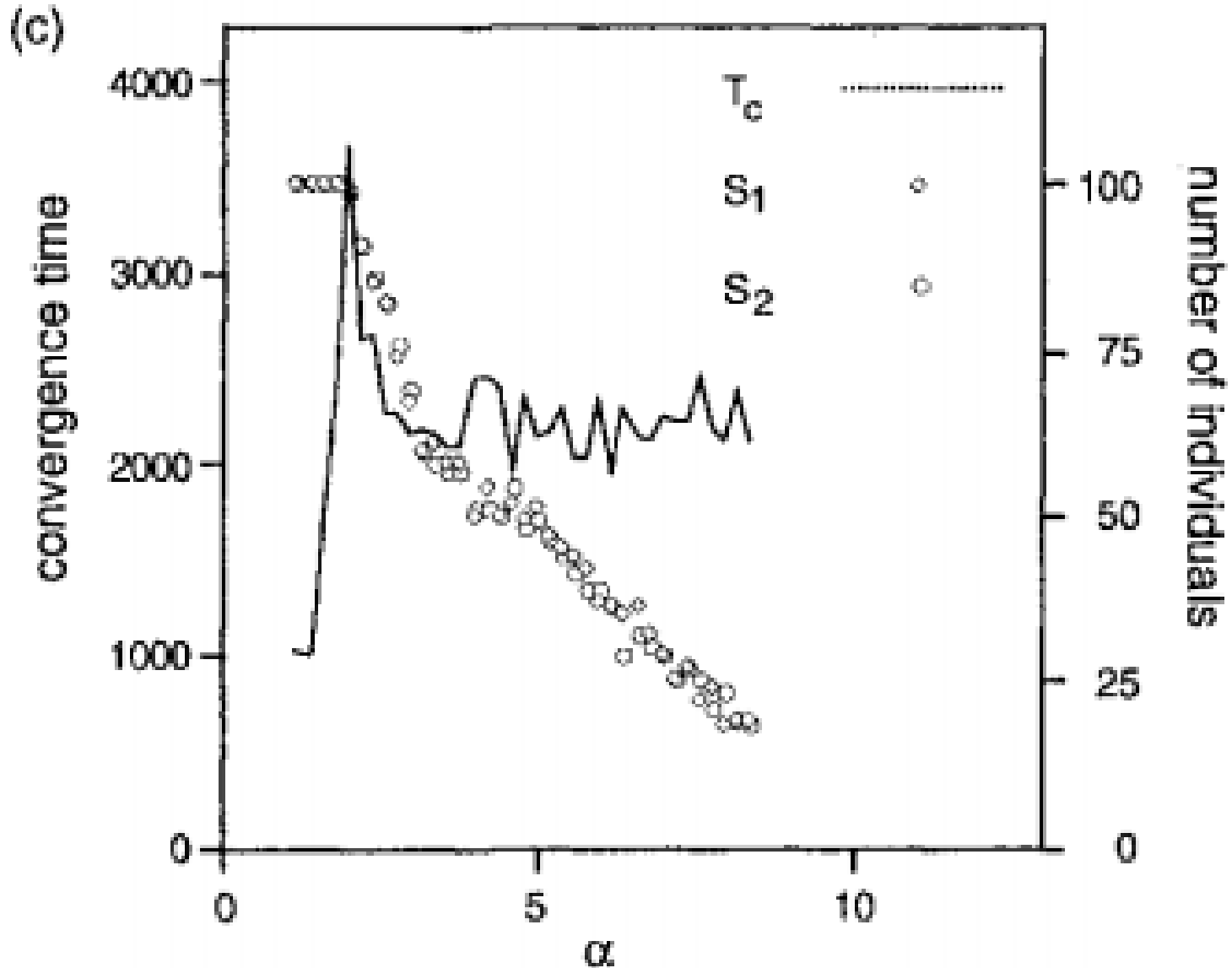
Convergence Time vs Forgetting Factor



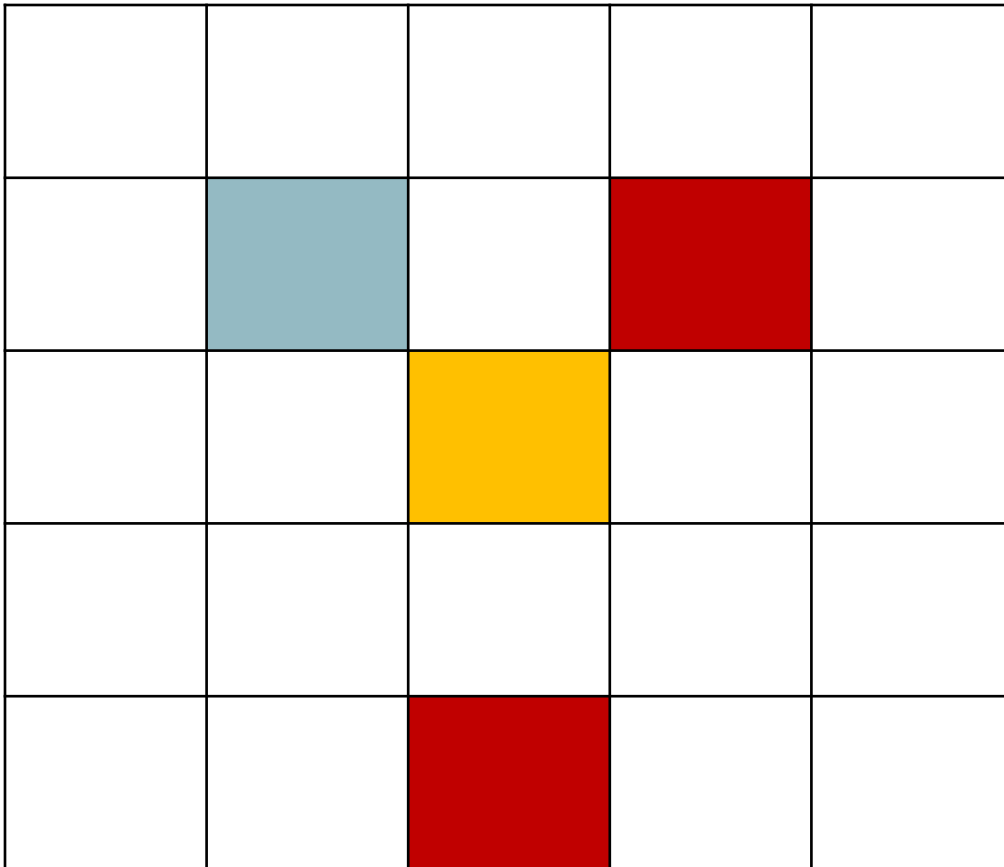
Convergence Time vs Nap Constant



Convergence Time vs Efficiency



The Mailman Problem



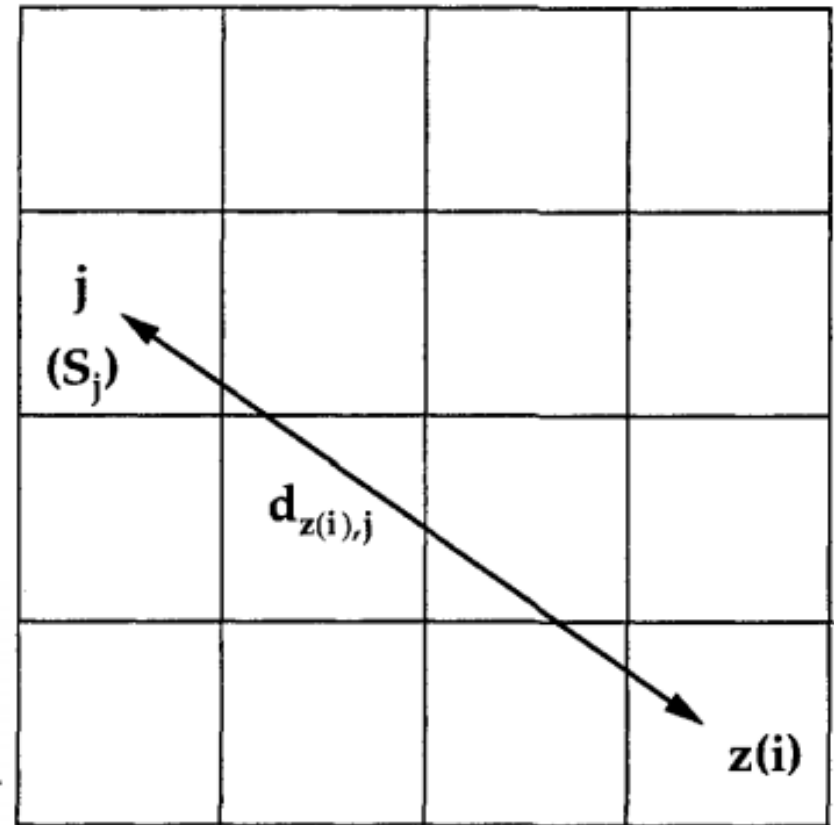
The Mailman Problem

Chance to switch zones:

$$P_{ij} = \frac{S_j^2}{S_j^2 + \alpha \theta_{i,j}^2 + \beta d_{z(i),j}^2}$$

Threshold Variance:

$$\begin{aligned}\theta_{i,j} &\leftarrow \theta_{i,j} - \xi_0, \\ \theta_{i,n(j)} &\leftarrow \theta_{i,n(j)} - \xi_1, \quad \forall n(j), \\ \theta_{i,k} &\leftarrow \theta_{i,k} + \varphi \text{ for } k \neq j, k \notin \{n(j)\}\end{aligned}$$



Bidding Algorithms

1. Try to take another truck the same color as the current
2. Take important jobs
3. Take any job to stay busy
4. Don't take a job if paint booth is down or queue is large

