Discrete Cosine Analysis

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A Maple notebook to load in an audio signal (stored in an Excel workbook) and perform a discrete cosine analysis of the frequency content.

> restart;

Load in various useful packages.

with(SignalProcessing): with(plots): with(ArrayTools): with(ExcelTools):

Load and Plot Audio Signal:

First switch to the directory with the file we want (change this to wherever you stored the .xlsx file).

> currentdir("C:/Users/bryan/Documents/texstuff/simiode_ODE_book/chapter8/figure_code/")

Read in the audio file, here stored as column 1 in an Excel worksheet. Here "n" is the number of data points.

$$> Q0 := Import("gong.xlsx") :$$

$$n := Size(Q0)[1]; #Number of data points$$

Store in an array suitable for Maple's DCT command.

$$fs := Array([seq(Q0[k][1], k=1..n)]):$$

Compute the duration "T" of the signal, and set the sampling rate (16000 Hz).

> samprate := 16000;

$$T := evalf\left(\frac{n}{samprate}\right);$$

Here's a plot of the entire signal versus time.

> fsize = 12 : #fontsize for plot

$$dataplt := \left[seq \left(\left[\frac{k - 0.5}{samprate}, fs[k] \right], k = 1..n \right) \right]:$$

plot(dataplt, thickness = 1, labels = ["Time (seconds)", "Signal Intensity"], labeldirections = [horizontal, vertical], axes = boxed, color = red, font = [TimesRoman, fsize], labelfont = [TimesRoman, fsize]

= [TimesRoman, fsize])

For time t = 1 to t = 1.01 seconds plot from k = 16000 to k = 16161, roughly

>
$$dataplt := \left[seq\left(\left[\frac{k-0.5}{samprate}, fs[k]\right], k=16000...16161\right)\right]$$
:

> plot(dataplt, thickness = 1, labels = ["Time (seconds)", "Signal Intensity"], labeldirections

= [horizontal, vertical], axes = boxed, color = red, font = [TimesRoman, fsize], labelfont = [Tim

= [TimesRoman, fsize])

Compute the DCT of the Signal Vector and Plot

$$C := DCT(fs)$$
:

Display the DCT versus frequency (C[k] is frequency (k-1)/(2*T)).

Select data for plotting, plot.

>
$$Cplot := \left[seq\left(\left[\frac{k-1}{2 \cdot T}, abs(C[k]) \right], k=1 \dots n \right) \right] :$$

> plot(Cplot, thickness = 1, labels = ["Frequency (hz)", "DCT Magnitude"], labeldirections

```
= [horizontal, vertical], axes = boxed, color = red, font = [TimesRoman, fsize], labelfont = [TimesRoman, fsize])
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