

# The Mathematics of Marriage

Kurt Bryan and SIMIODE

Here is the data from Table 3.11 for the male 1940-44 cohort, percentage data rescaled to fractions:

```
men4044 = [0.211, 0.661, 0.831, 0.888, 0.912, 0.927, 0.940];  
times = [0 5 10 15 20 25 30];  
N = length(times);
```

A plot of the data

```
plot(times,men4044)
```

The function  $P(t)$  that might fit this data, according to the model, is

```
syms t;  
syms A;  
syms b;  
P0 = men4044(1);  
P(t,A,b)=P0./(P0+(1-P0).*exp(-A*(b.^t-1)./log(b)))
```

Form a sum of squares to fit the data

```
SS(A,b)=sum((P(times,A,b)-men4044).^2);
```

Now minimize in  $A$  and  $b$ . A contour plot of  $\log(SS)$  may be helpful.

```
fcontour(log(SS(A,b)), [0 1 0 1])
```

Something near  $A = 0.6$ ,  $b = 0.9$  looks promising. We can set  $dSS/dA = 0$  and  $dSS/db = 0$  to find this point.

```
dSSdA = diff(SS(A,b),A);  
dSSdb = diff(SS(A,b),b);  
vpasolve([dSSdA==0,dSSdb==0],[A,b],[0.6,0.9]);  
fprintf("A = %f\n",Absol.A)  
fprintf("b = %f\n",Absol.b)
```

Plot  $P(t)$  with these values, compare to the data

```
plot(times,men4044)  
hold on  
fplot(P(t,Absol.A,Absol.b),[0 30], '-r')
```

Here is the data for the 1945-49 men

```
men4549 = [0.223, 0.655, 0.801, 0.861, 0.893, 0.913, 0.925]
```

Here is the data for the 1940-44 women:

```
women4044 = [0.481, 0.782, 0.868, 0.897, 0.914, 0.925, 0.932]
```

Here is the data for the 1945-49 women:

```
women4549=[0.431, 0.769, 0.850, 0.884, 0.902, 0.915, 0.922]
```