

[Worksheet to support Exercise 3.4.10, modeling a cooling potato.

[> *restart*;
[*with(plots)* :

[The data, in time/temperature pairs:

[> *data* := [[0, 204], [2, 193], [4, 184], [8, 169], [10, 162], [13, 156], [17, 149], [20, 143],
[24, 138], [30, 130]] :

[Number of data points is

[> *N* := *nops(data)*

[However, we will operate on the quantities $(t, \log(u(t)-A)-\log(u(0)-A))$, with $u(0)=204$ and $A = 72$.

[> *logdata* := [*seq*([*data*[*j*][1], $\log(\text{data}[j][2] - 72) - \log(204 - 72)$], $j = 1 \dots N$)]

[A plot

[> *plt1* := *pointplot(logdata, color = red, symbol = solidcircle, symbolsize = 20, labels*
= ["time (minutes)", "Temperature"], *labeldirections* = [*horizontal*, *vertical*]) :

display(plt1);

[We seek to fit a line $y = -k \cdot t$ to this

[> $u(t) := -k \cdot t$;

[A least-squares function can be formed as

[> *SS* := *add*(($u(\text{logdata}[j][1]) - \text{logdata}[j][2]$)², $j = 1 \dots N$)

[Now adjust k to minimize this.

[>