

Direction Fields

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A worksheet to illustrate how to draw a direction field for an ODE.

> *restart*;

Load in DEtools package, which contains the helpful **DEplot** command.

> *with(DEtools)* :

A differential equation

> $de := u'(t) = t \cdot \cos(u(t)) - \sin(t)$

Sketch a direction field on the range $0 \leq t \leq 5$, $0 \leq u \leq 5$ using the **DEplot** command.

> *DEplot*(*de*, *u*(*t*), *t* = 0 .. 5, *u* = 0 .. 5)

Same plot but with solution curves through initial conditions $u(2) = 1$ and $u(4) = 2$:

> *pp2* := *DEplot*(*de*, *u*(*t*), *t* = 0 .. 5, *u* = 0 .. 5, [[*u*(2) = 1], [*u*(4) = 2]], *linecolor* = *black*)

>