



# Lecture 4-1

Switch on the Light:  
Simple Sensors

Sonar and Laser:  
Complex Sensors

*The Robotics Primer (Ch. 8, 9)*



# Course Announcements

- ⦿ Bring your laptop and robot everyday
- ⦿ Bring a calculator for Tuesday's Quiz on **Complex Sensors/Perception** (open notes)
- ⦿ Lab 3 demo due **Thursday, 4/02/09**
- ⦿ Lab 3 memo and code due by midnight on **Friday, 4/03/09**
- ⦿ Upload memo and code to Angel
- ⦿ Memo and Code grades on Angel by **Friday, 4/03/09**



# Quote of the Week

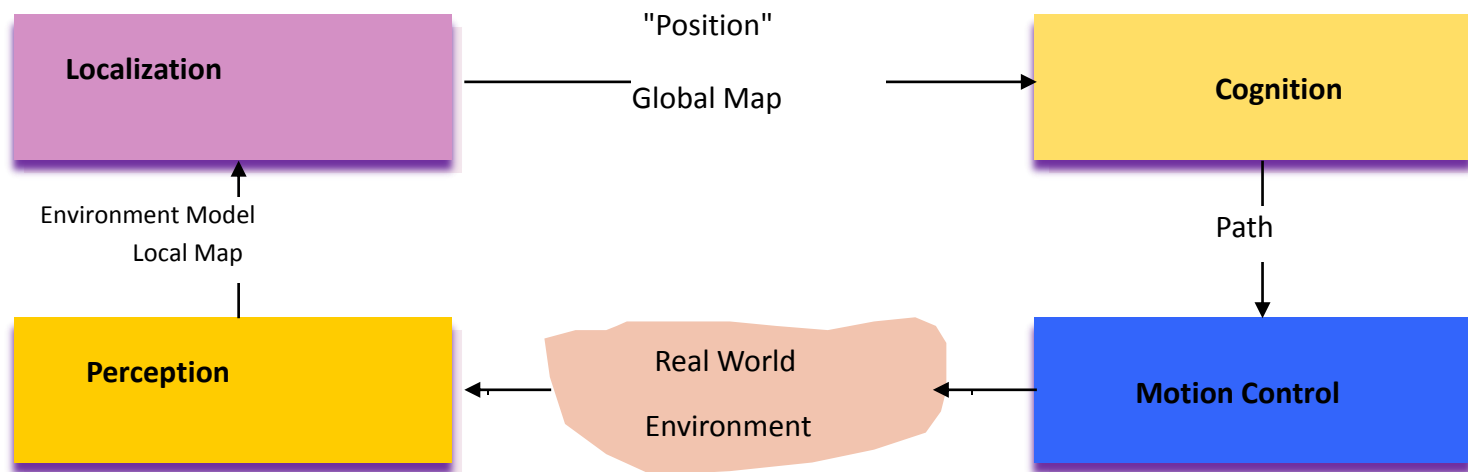
*“A common mistake people make when trying to design something completely foolproof is to underestimate the ingenuity of complete fools.”*

D. Adams



# Perception

One of the most important tasks of an autonomous mobile robot is *perception*. Perception is used for the robot to acquire knowledge from its environment. Perception involves taking measurements using various sensors and extracting meaningful information.





# More Simple Sensors



# Shaft Encoders

- ⦿ One of the most common break beam sensors is a **shaft encoder** on a motor
- ⦿ Shaft encoders measure the angular rotation of a shaft or an axle
- ⦿ They provide position and/or velocity information about the shaft they are connected to (i.e. speedometer and odometer)
- ⦿ An encoder can also be used in the reflectance configuration by painting a disk with contrasting colors



# Feedback from Encoders

- ⦿ Position and velocity information from encoders can be used to drive the robot a certain distance or turn a certain angle.
- ⦿ These movements will not be precise because of slip and slide and backlash in the gearing mechanism
- ⦿ The encoder can correct for odometry error but some error is still avoidable
- ⦿ There is no perfect sensor and there will always be some uncertainty



# Quadrature shaft encoding

- ◉ Quadrature shaft encoding measures the direction of rotation of a motor shaft. This technology is used in a ball-type computer mouse
- ◉ There are 2 encoders aligned 90 degrees out of phase so by comparing the output of the state change to the previous step it is possible to tell if the direction changed
- ◉ When the shaft moves one direction the counter increments and decrements for the opposite direction



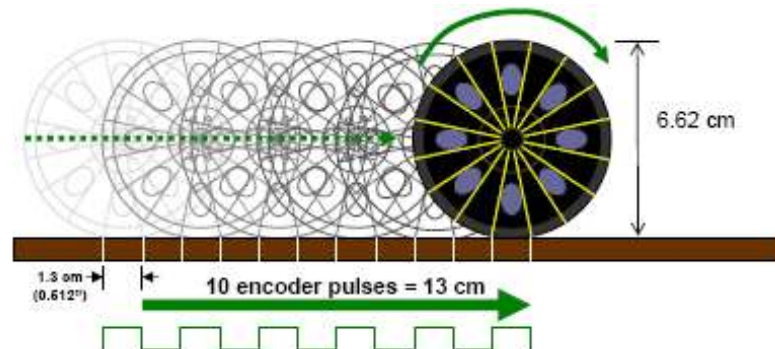


# Encoders:

## Measuring wheel distance

- Relative position estimation is dependent on the measurement of the robot's velocity
- Optical encoders can be used on each wheel to measure angular position and or velocity
- If the robot moves straight ahead, you can count encoder pulses to determine its new location
- If 10 encoder pulses = 13 cm then distance can have an error up to 1.3 cm
  - This can be serious for short distances
  - Accumulated error can cause problems

$$\begin{aligned} \text{Distance traveled per pulse:} &= \frac{(\text{Wheel Circumference})_{\text{cm}}}{16 \text{ pulses}} \\ &= \frac{6.62_{\text{cm}} \pi}{16} \\ &= 1.299_{\text{cm}} \end{aligned}$$





# Encoders: Measuring spin angle

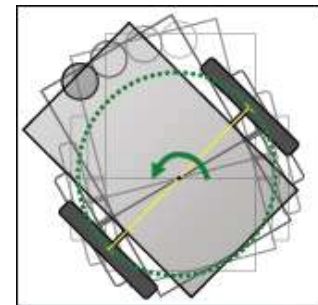
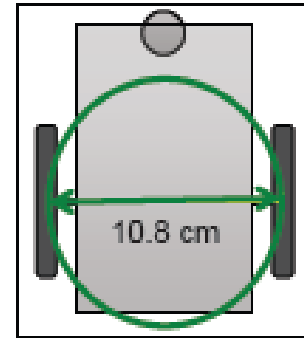
- Assuming the robot turns around its center

$$(v_1 = -v_2)$$

- If the robot has a diameter of 10.8 cm, the circumference is  $\pi d = \pi(10.8) = 33.93 \text{ cm}$

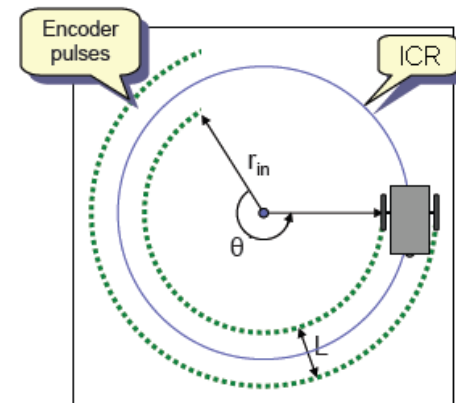
- If each encoder pulse indicates a travel distance of 1.3 cm

$$(1.3 \text{ cm/pulse}) / (33.93 \text{ cm})(360^\circ) =$$
$$13.79^\circ/\text{pulse}$$





# Encoders: Measuring turn angle



When the wheel velocities are not equal

- Each wheel traces out a circle with a different circumference
- The diameter of the robot  $L = 10.8$  cm and a resolution of 1.3 cm per pulse
- Length of the inner arch  $\rightarrow s_2 = r_{in} \theta$
- Length of the outer arch  $\rightarrow s_1 = (r_{in} + L)\theta = s_2 + L \theta$
- So  $\theta = (s_1 - s_2)/L$
- The length of the arcs can be described in terms of the encoder pulses for the right ( $p_1$ ) and left ( $p_2$ ) wheels.
- the difference in the encoder pulses,  $p_{\Delta} = p_1 - p_2$



# Encoders:

## Measuring turn angle, cont.

- ◉  $\theta = (s_1 - s_2)/L$

- ◉ Using  $p_{\Delta}$  to find the change in the angle

$$\begin{aligned}\theta &= (p_{\Delta})(1.3 \text{ cm/pulse})/10.8 \text{ cm} \\ &= 0.12037 p_{\Delta} \text{ radians} = (6.897) p_{\Delta}^{\circ}\end{aligned}$$

- ◉ Note that when the pulses of both wheels are equal (i.e. same velocity),  $\theta = 6.897 p_{\Delta}^{\circ} = (6.897)(2p_1) = 13.79 p_1^{\circ}$
- ◉ To find the  $(x, y)$  position of the robot substitute encoder pulses for velocities in the forward kinematic equations



# Heading Sensors

- ◉ Heading sensors can be *proprioceptive* (gyroscope, inclinometer, accelerometers) or *exteroceptive* (compass)
- ◉ They are used to determine the robots orientation and inclination
- ◉ They may be used with appropriate velocity information to integrate the movement to a position estimation (i.e. *dead reckoning* (ship navigation) )



# Compass

- ⦿ A **compass** uses the earth's magnetic field to determine absolute measure for robot orientation.
- ⦿ Large variety of solutions to measure the earth magnetic field
  - mechanical magnetic compass
  - direct measure of the magnetic field
- ⦿ Major drawbacks:
  - weakness of the earth field
  - easily disturbed by magnetic objects or other sources
  - Bandwidth limitation of electronic compasses and susceptibility to vibration
  - not feasible for indoor environments (conceivably could provide useful local orientation)



# Inertial Sensors

## ◎ Gyroscopes

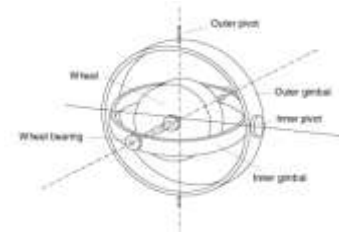
- Measure the rate of rotation independent of the coordinate frame
- Uses the principle of conservation of angular momentum
- Common applications:
  - Heading sensors, Full Inertial Navigation systems (INS)

## ◎ Accelerometers

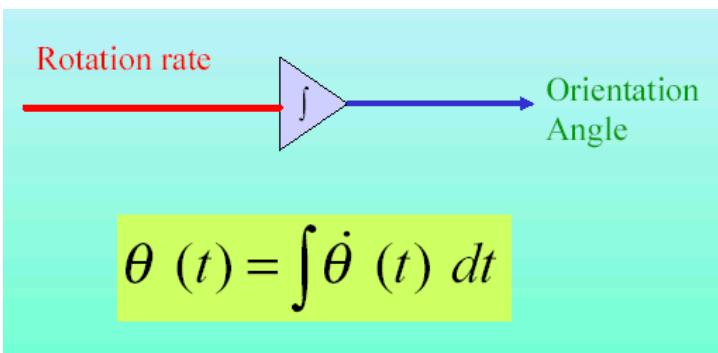
- Measure accelerations with respect to an inertial frame
- Common applications:
  - Tilt sensor in static applications, Vibration Analysis, Full INS Systems



# Gyroscopes



- ◉ These devices return a signal proportional to the rotational velocity.
- ◉ There is a large variety of gyroscopes that are based on different principles
- ◉ **Gyroscopes** are heading sensors, that keep their orientation in relation to a fixed frame
  - Provide an absolute measure for the heading of a mobile robot
  - There are *mechanical* and *optical* gyroscopes



- ◉ **Mechanical Gyroscopes**

- Standard gyro - relies on standard properties of a fast-spinning rotor
- Rated gyro – measures angular speeds instead of absolute orientation
- If the spinning axis is aligned with the north-south meridian, the earth's rotation has no effect on the gyro's horizontal axis
- If the spinning axis points east-west, the horizontal axis reads the earth rotation

- ◉ **Optical Gyroscopes**

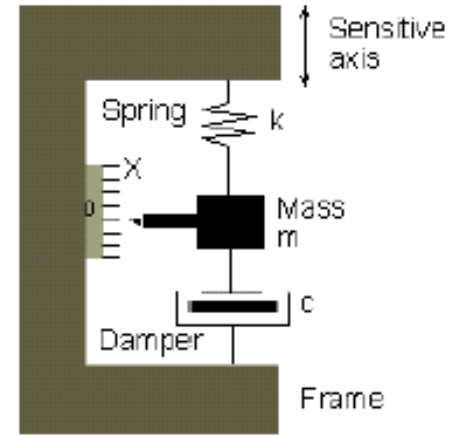
- Use light beams or lasers instead of mechanical parts
- Measures angular speed





# Accelerometers

- They measure the inertia force generated when a mass is affected by a change in velocity.
- This force may change
  - The tension of a string
  - The deflection of a beam
  - The vibrating frequency of a mass
- Main elements are a mass, suspension mechanism and sensing element
- High quality accelerometers include a servo loop to improve linearity of the sensor



$$F = m \frac{d^2 x}{d^2 t} + c \frac{dx}{dt} + kx$$



*The Robotics Primer*, Matarić, Chapter 9

# Complex Sensors

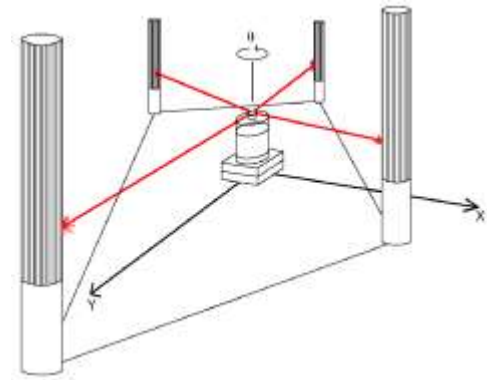


# Complex Sensors

- ⦿ These sensors require a great deal of processing compared to simple sensors
- ⦿ Additionally after processing, the information they provide is much more varied and useful than simple sensors

# Ground-Based Beacons

- ◉ An elegant way to solve the localization problem in mobile robotics is to use *active* or *passive* beacons
- ◉ **Beacons** are signaling guiding devices with a precisely known position
- ◉ The *Global Positioning System* (GPS) revolutionized modern navigation technology
  - Extremely effective and one of the key sensors for outdoor mobile robotics
  - 24 GPS satellites available at all times for civilian navigation
  - Passive, exteroceptive sensors
  - Triangulation of 3 data points helps the receiver infer its own position
  - For indoor robots GPS is not applicable
- ◉ Major drawback with the use of beacons indoor:
  - Beacons require changes in the environment
  - Limit flexibility and adaptability to changing environments.

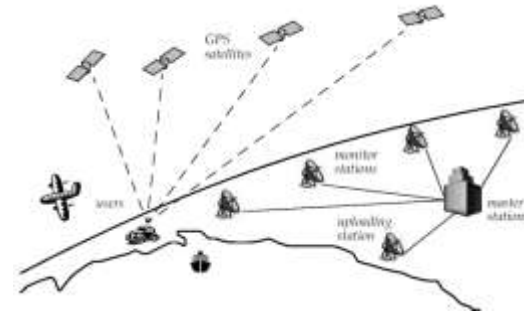


## Space Segment





# Global Positioning System



Technical challenges:

- ⦿ Satellite transmissions are extremely low-power and successful reading requires a direct line-of-sight communication
- ⦿ It requires Time synchronization between the individual satellites and the GPS receiver
- ⦿ Real time update of the exact location of the satellites
- ⦿ Precise measurement of the time of flight
- ⦿ Interference with other signals
- ⦿ GPS uses pseudorange and performs at a resolution of 15 meters
- ⦿ *Differential GPS* (DGPS) uses a second receiver that is static at a known position (corrects error with the reference)
- ⦿ The bandwidth has a 200 – 300 ms latency or no better than 5 Hz GPS updates (a problem on fast-moving mobile robots)



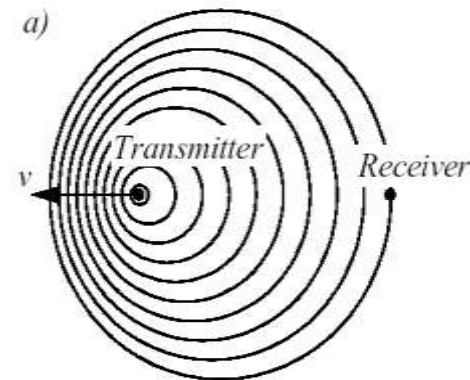
# Motion/Speed Sensors



# Motion/speed sensors

- ◉ *Motion or Speed sensors*  
measure directly the relative motion between the robot and its environment
- ◉ For fast moving robots, Doppler-based motion sensors detect the obstacle by measuring frequency shift
- ◉ A transmitter emits an electromagnetic sound wave with a frequency  $f_t$
- ◉ It is reflected from an object and measured by a receiver

- ◉ The measured frequency  $f_r$  at the receiver is a function of the relative speed  $v$  between the transmitter and receiver (*Doppler frequency*)



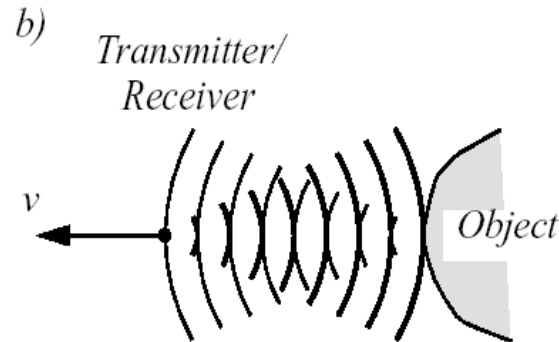
$$f_r = f_t (1 + v/c)$$



# Motion Sensor :

## Doppler Effect Based (Radar or Sound)

- ⦿ The reflected wave is typically measured by the *Doppler shift*,  $\Delta f$
- ⦿ The *Doppler shift* can be used to find the relative speed



$$f_r = f_t \frac{1}{1 + v/c}$$

$$\Delta f = f_t - f_r = \frac{2f_t v \cos \theta}{c}$$

$$v = \frac{\Delta f \cdot c}{2f_t \cos \theta}$$

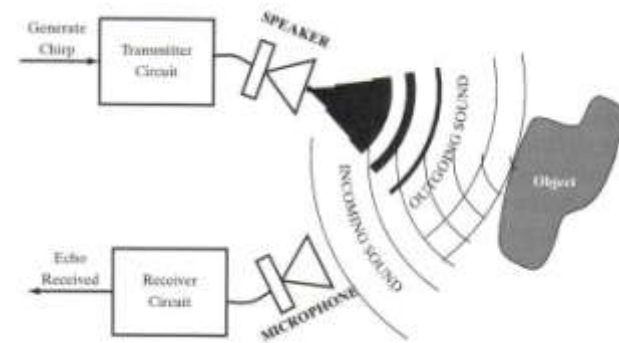




# SONAR



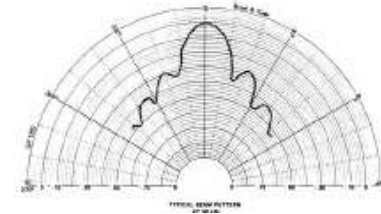
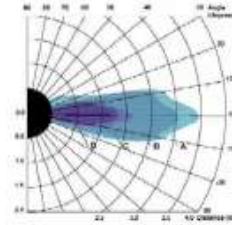
# SONAR



- **Ultrasound (sonar)** refers to the range of frequencies of sound that are beyond human hearing
- The process of finding your location based upon sonar is **echolocation**
- Sonar are active sensor that emit a chirp or ping and use time of flight to determine distance
- A **transducer** is a device that transforms one form of energy into another
- The transducer on a sonar emits the chirp/ping and receives the sound (echo) that comes back.
- Mechanical energy is converted into sound as the membrane on the transducer flexes to produce a ping



# SONAR



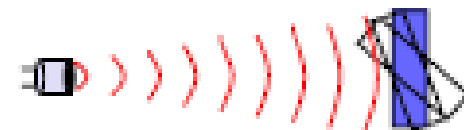
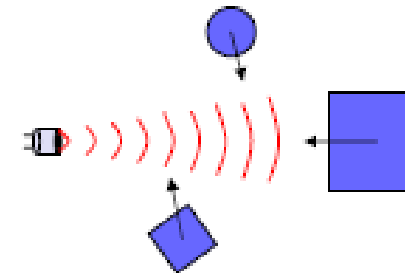
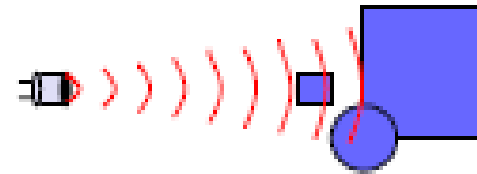
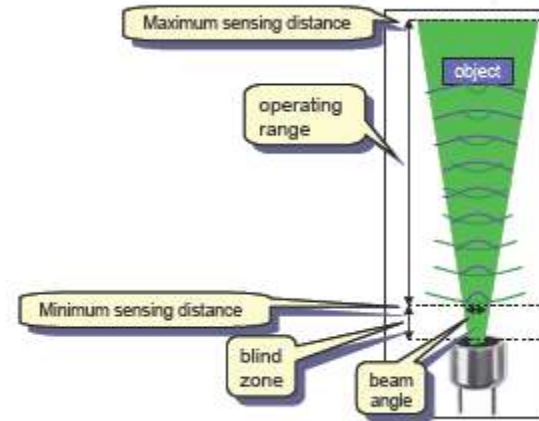
## ◎ *Sound Navigation and Ranging (SONAR)*

- bounce sound off of objects
  - measure time for reflection to be heard - gives a range measurement
  - It measures change in frequency and gives the relative speed of the object (Doppler effect)
  - bats and dolphins use it with amazing results
  - robots use it with less than amazing results
- ◎ Wider objects near the center of the beam result in better accuracy



# Sonar: Reliability

- ◉ **Blind zone** is when an echo arrives before the transducer is ready to receive and objects are not detected reliably
- ◉ Sensor readings vary based upon:
  - Distance to object(s)
  - Angle that object makes with respect to sensor axis
  - Direction that objects enter sensing range

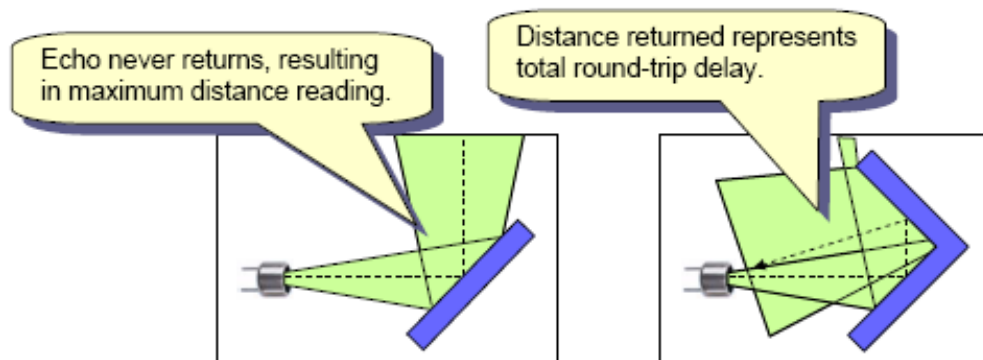




# Sonar:

## Specular Reflection

- Specular reflection can cause reflected sound to
  - Never return to the transducer
  - Return to the transducer too late
- The result is that the distance measurement is too large and inaccurate

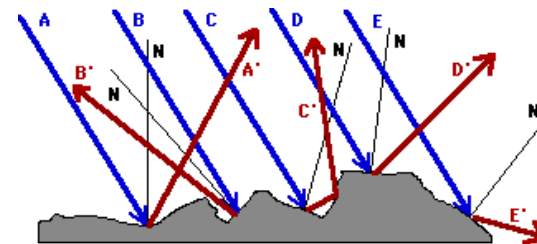
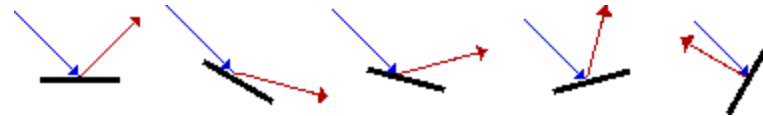
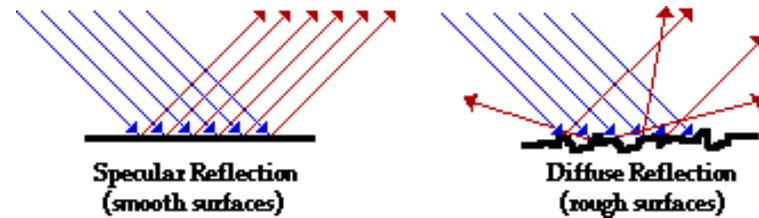




# SONAR:

## Specular Reflectance

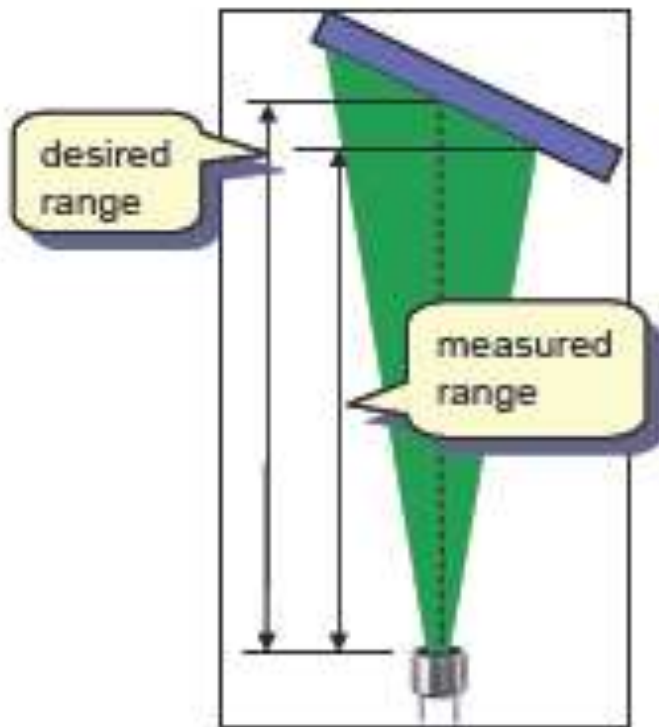
- Brightness depends on
  - reflectance of the surface patch
  - position and distribution of the light sources in the environment
  - amount of light reflected from other objects in the scene onto the surface patch
- Two types of reflection
  - Specular (smooth surfaces)
  - Diffuse (rough surfaces)
- Necessary to account for these properties for correct object reconstruction  $\Rightarrow$  complex computation



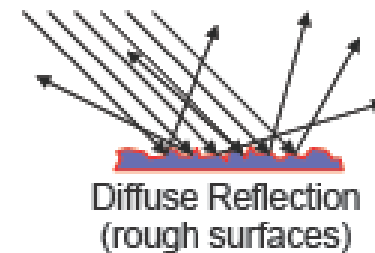
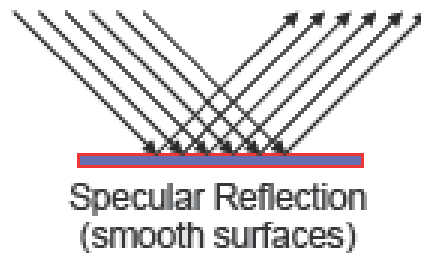


# Sonar:

## Sensitivity



- ◉ *Sensitivity* to obstacle angle can result in improper range readings
- ◉ When the beam angle of incidence falls below a certain critical angle *specular reflection* errors occur

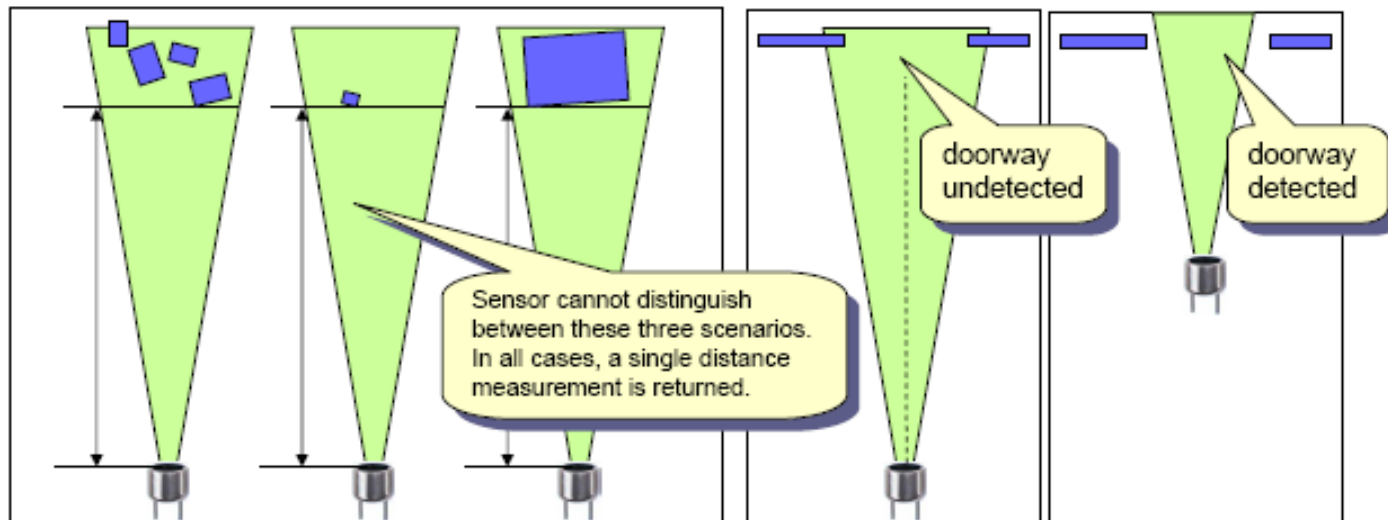




# SONAR:

## Resolution

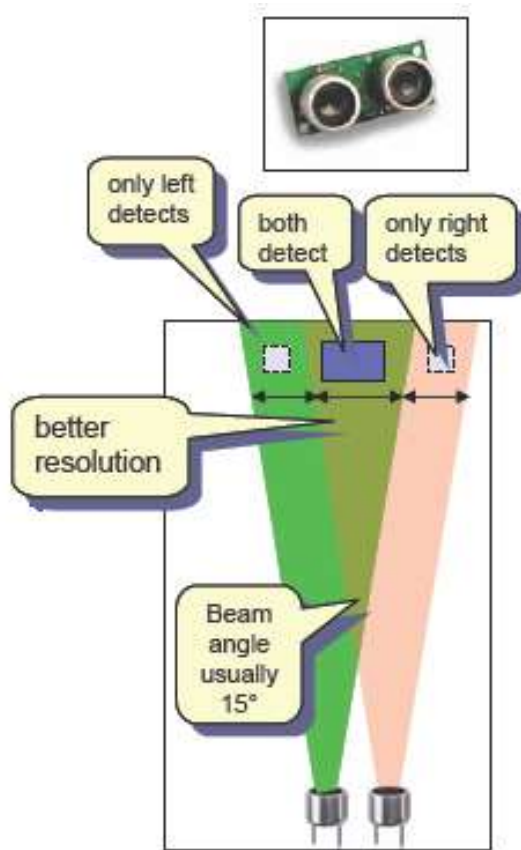
- Distance and angular resolution decreases as objects become further from the sensor
  - Multiple close objects cannot be distinguished
  - Gaps such as doorways cannot be detected







# Ultrasonic Range Sensors: Redundancy

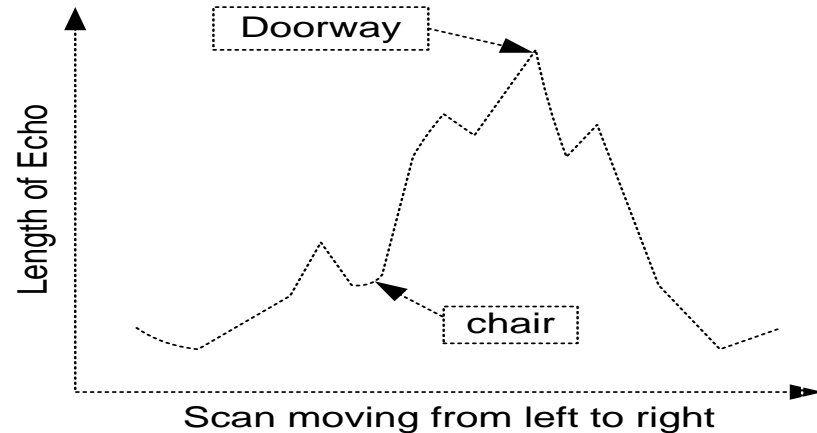
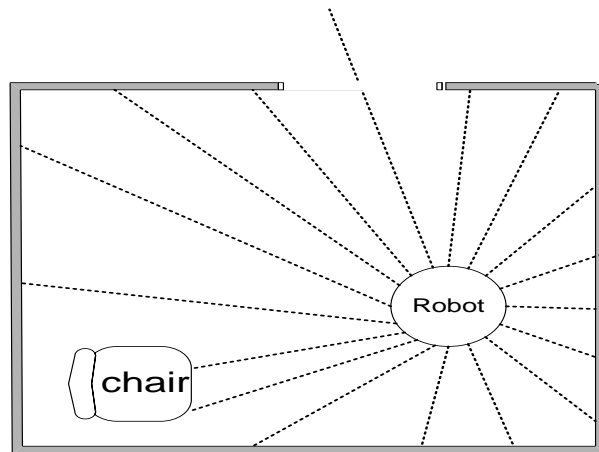


- To increase beam width (*resolution*), two sensors are used together
- Detection in either or both sensors allows for increased resolution



# Ultrasonic Range Sensors: Applications

- Distance Measurement
- Mapping*: Rotating proximity scans (maps the proximity of objects surrounding the robot)
  - Scanning at an angle of  $15^\circ$  apart can achieve best results





# Ultrasonic Range Sensors: Mapping

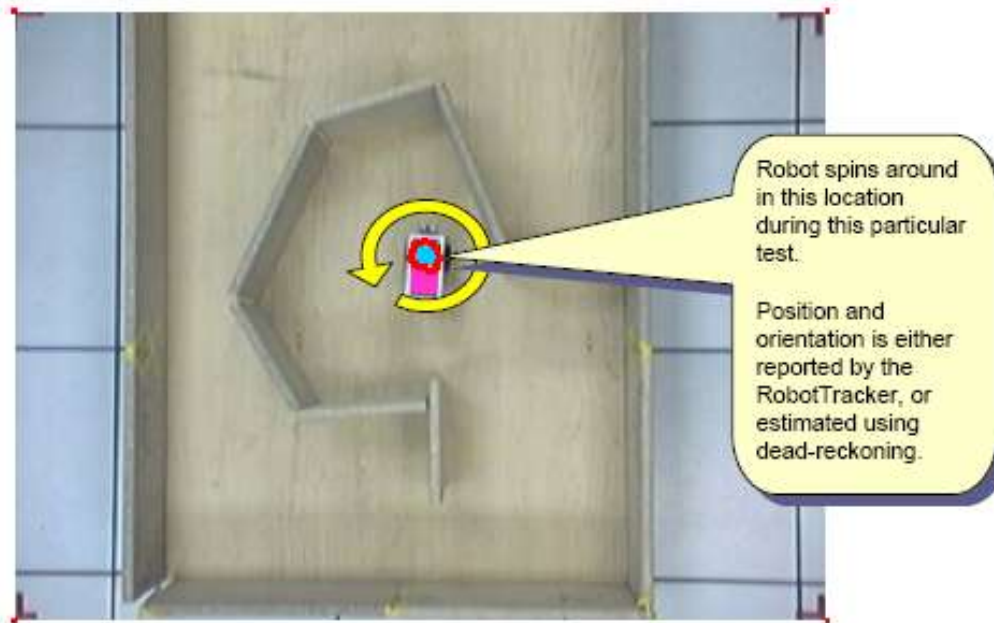
- To perform mapping take multiple readings:
  - Rotate the sensors
  - Rotate the robot chassis
  - Use multiple sensors at fixed positions on chassis





# Ultrasonic Range Sensors: Mapping Example

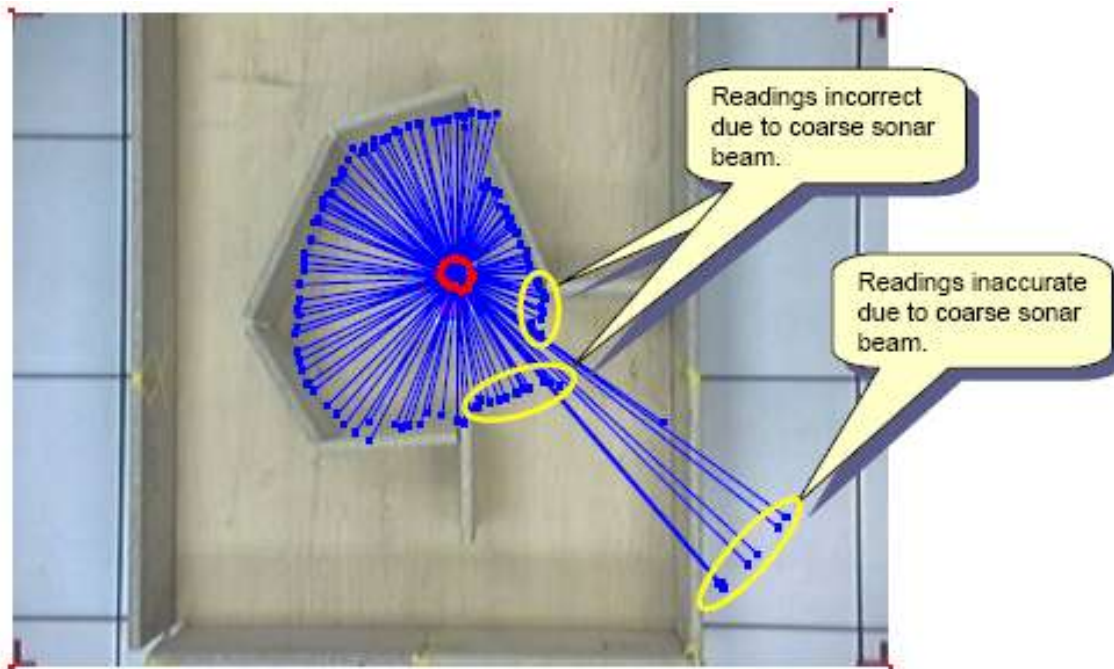
Use sonar mounted to the front of a robot to compute the ranges to obstacles from a location in the environment





# Ultrasonic Range Sensors: Mapping Example

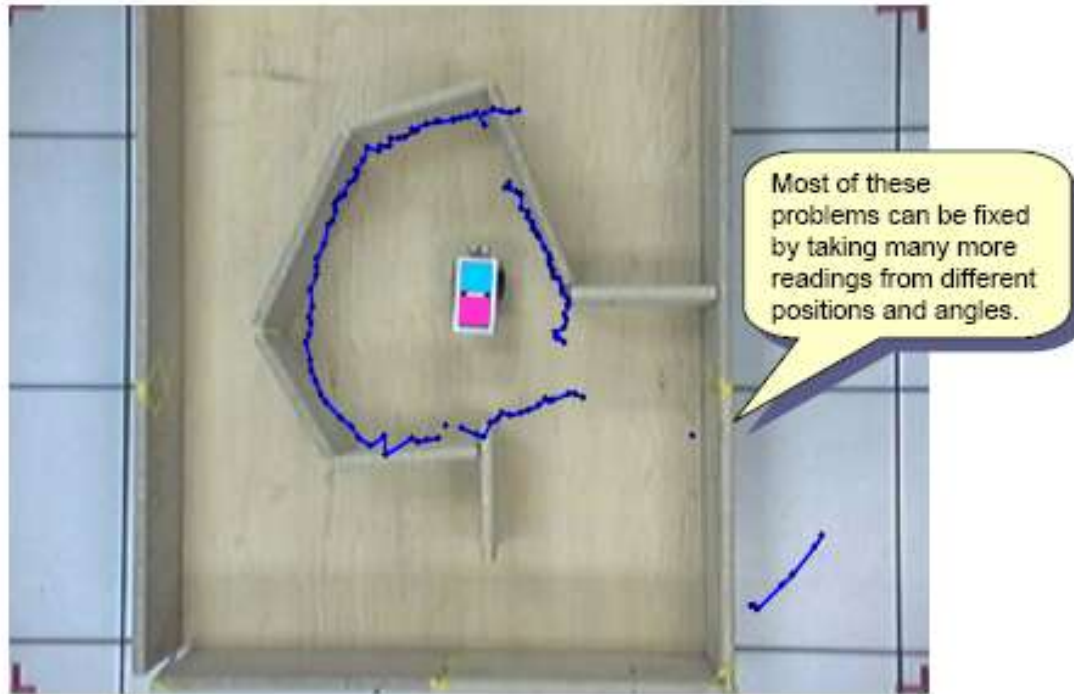
Blue lines show sonar readings detected from the robot's position  $(x, y)$  to the obstacle position  $(x_o, y_o)$





# Ultrasonic Range Sensors: Mapping Example

The sonar data produces a 'rough' outline of the environment with some inaccurate readings

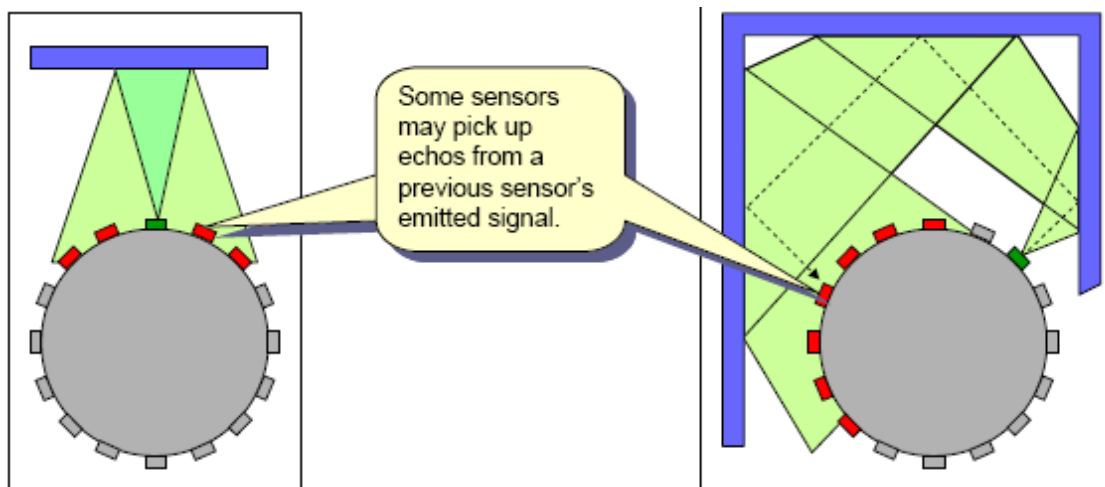




# Ultrasonic Range Sensors:

## Crosstalk

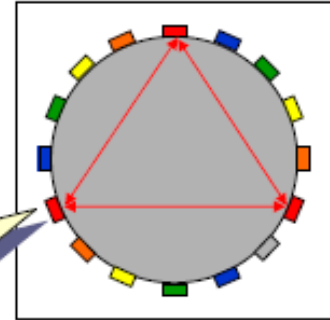
- ⦿ Using multiple fixed sensors can lead to *crosstalk*
- ⦿ *Crosstalk* is interference in which echoes emitted from one sensor are detected by others





# Ultrasonic Range Sensors: Crosstalk Solution

Group sonars into small groups that are allowed to emit signals at the same time.

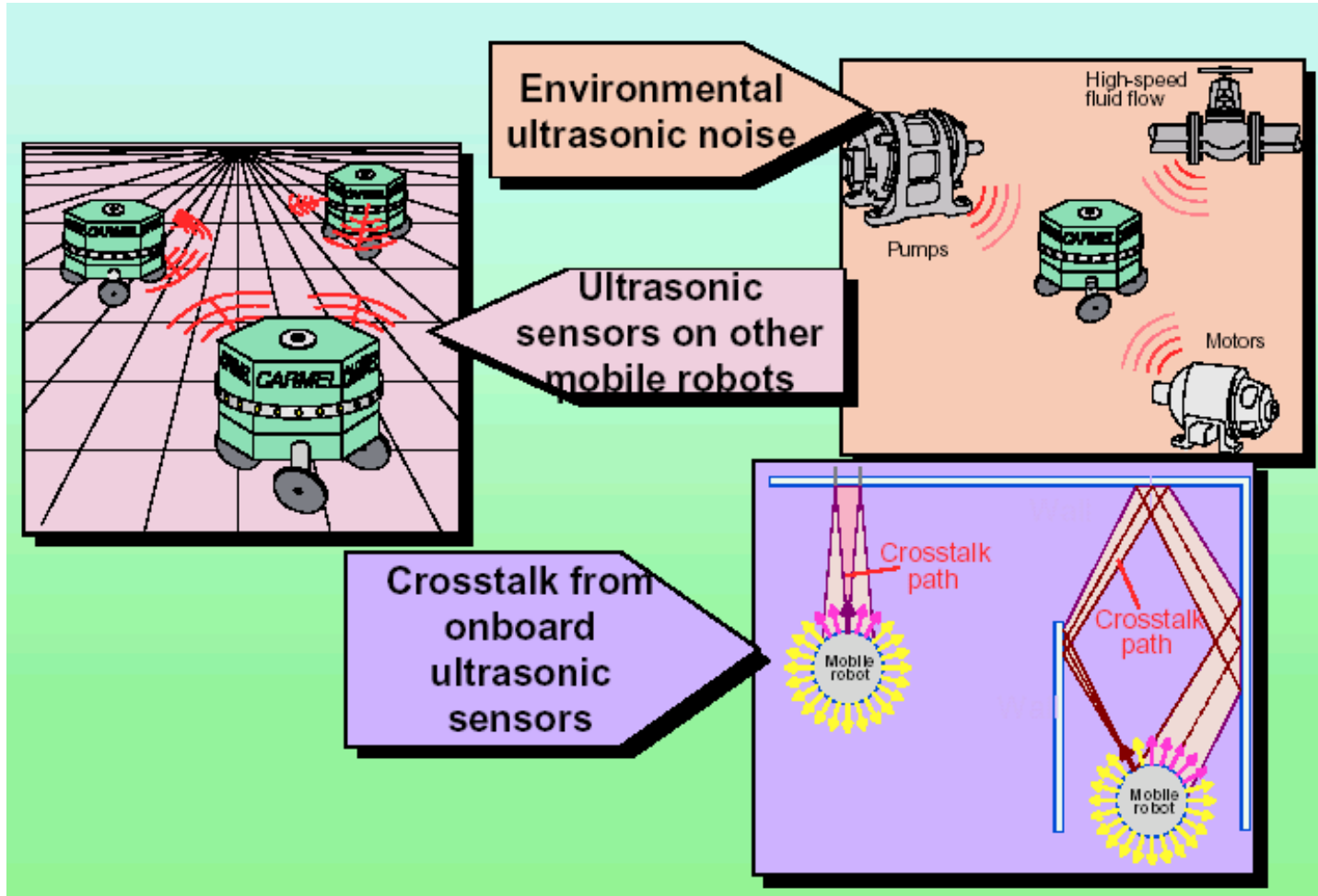


- ⦿ Crosstalk signals are impossible to detect unless signals are unique (coded)
- ⦿ Crosstalk can be reduced by carefully timing the emitting of signals
  - Emit from one and wait for a time interval
  - Emit from a select few that may not have interference
- ⦿ Emit adjacent sensors at different frequencies





# Ultrasonic Range Sensors: Noise Issues





# Ultrasonic Range Sensors:

## Advantages and Disadvantages

### ⦿ Advantages

- Reliable with good precision
- Not as prone to outside interference
- Good maximum range
- Inexpensive

### ⦿ Disadvantages

- Sensitive to smoothness
- Sensitive to angle to obstacles (*specular reflection*)
- Poor resolution
- Prone to self-interference from echoes
- Cannot detect obstacles too close
- Soft surfaces absorb sound energy
- Bandwidth



# Laser Range Finders



# Laser Sensors

- ◉ Unlike sonar sensors, lasers are not very susceptible to specular reflection
- ◉ However, there are some trade-offs as well as a significant cost to using lasers
- ◉ Lasers emit highly amplified and coherent radiation at one or more frequencies
- ◉ It may or may not be in the visible spectrum
- ◉ Lasers also use the time of flight principle
- ◉ They are much faster than sonar because the speed of light is much faster than the speed of sound



# Laser Range Finders



- ◉ Some laser use phase-shift rather than time of flight distance measurement
- ◉ Laser are the most accurate sensors for measuring distance
- ◉ Similar to IR, light is emitted and detected
- ◉ Unlike sonar, light is projected in a beam rather than a cone
- ◉ Sensors are **LIDAR** (Light Detection and Ranging) Systems
- ◉ LIDAR systems use one of 3 techniques
  - Pulsed modulation
  - Amplitude modulation continuous wave (AMCW)
  - Frequency modulation Continuous Wave (FMCW)



# Laser Range Finders:

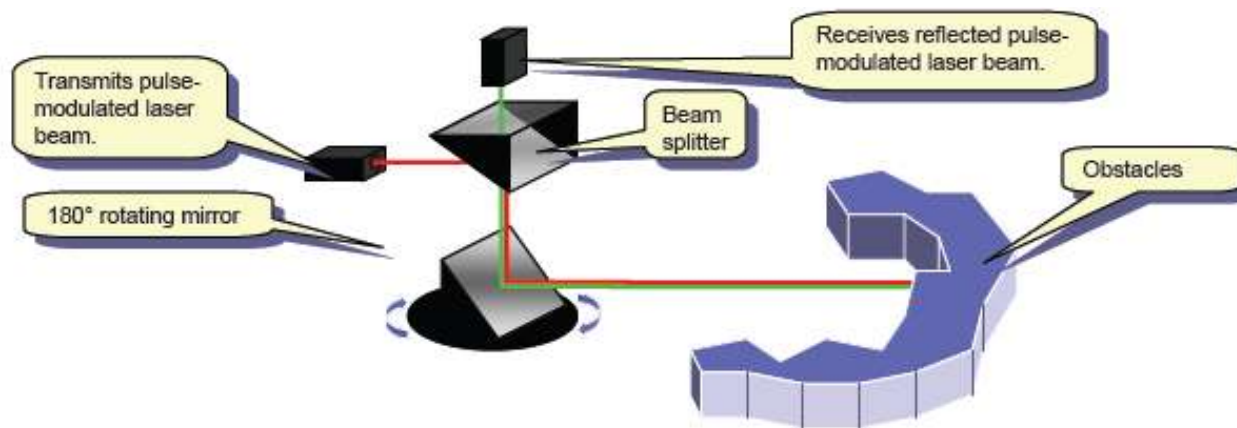
## Range Calculation

- ⊙ Range calculated as  $d = ct/2$ , where
  - $t$  = time taken for light to return
  - $c$  = speed of light  $\approx 3 \times 10^8$  m/s
- ⊙ Must have fast processing because the return times are small
- ⊙ Makes the sensor expensive ( $\approx \$10k$ )
- ⊙ Tradeoff for the price is high resolution ( $180^\circ$  at  $0.5^\circ$  resolution)



# Laser Range Finders: Pulsed Modulation

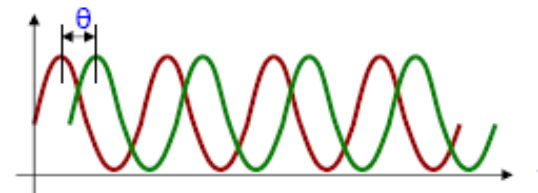
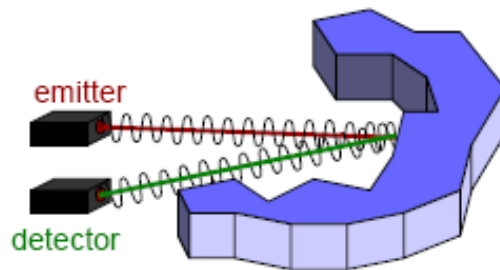
- ⦿ A Pulsed Modulation LIDAR system (i.e. Sick sensor)
  - Emits a pulsed laser light beam
  - Reflected light returned to the detector
  - Rotating mirrors are used to direct
  - Outgoing and incoming light perform 180° scan





# Laser Range Finders: Amplitude Modulation

- ◉ Emitter sends out a continuous modulated laser signal
  - Intensity of beam is modulated using a wave pattern (i.e. sinusoid)
  - Detected light has the same amplitude but is phase shifted
  - Difference in phase shift indicates the range
  - Range calculated is  $r = \theta c / (4\pi f)$ , where
    - $f$  = frequency of the modulated signal
    - $\theta$  = phase shift



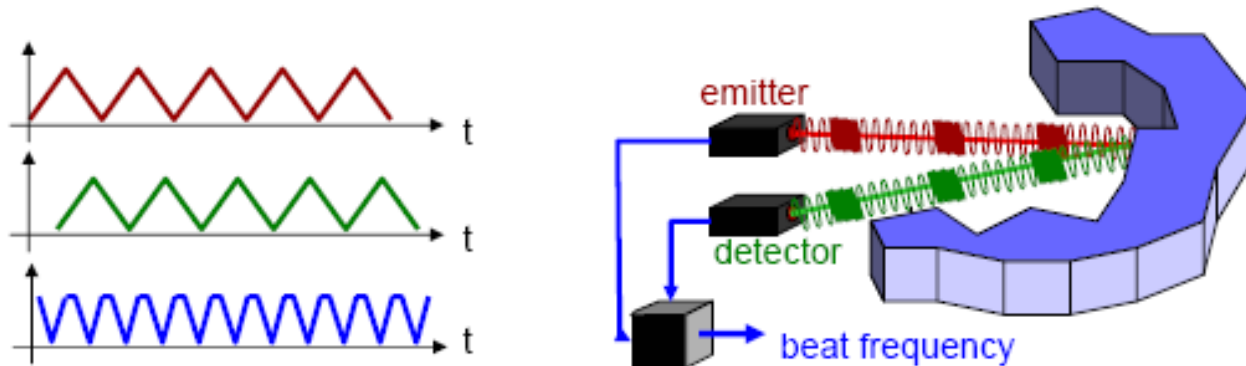
Range calculated as  $r = \theta c / 4\pi f$  where  
 $\theta$  = phase shift  
 $f$  = frequency of modulated signal





# Laser Range Finders: Frequency Modulation

- ⦿ Amplitude modulation is simpler and hence lower cost laser
- ⦿ Resolution is limited by modulating frequency
- ⦿ Frequency modulation sensors emit a continuous laser beam, but is modulated by *frequency*
  - Emitted signal is mixed with the reflected signal
  - The result is a difference in frequency



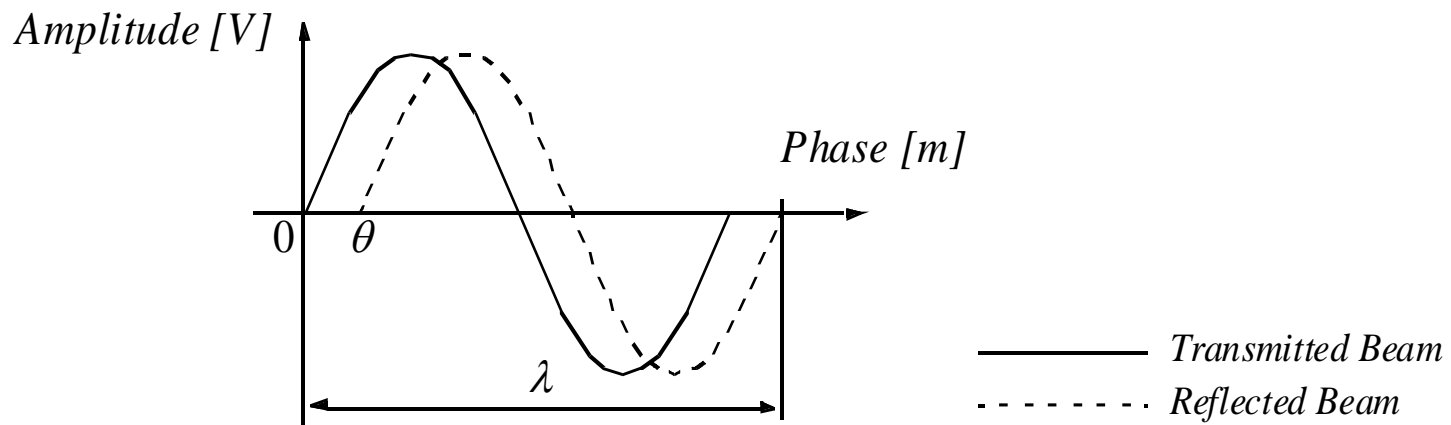


# Laser Range Sensor

$D$  is the distance between the beam splitter and the target

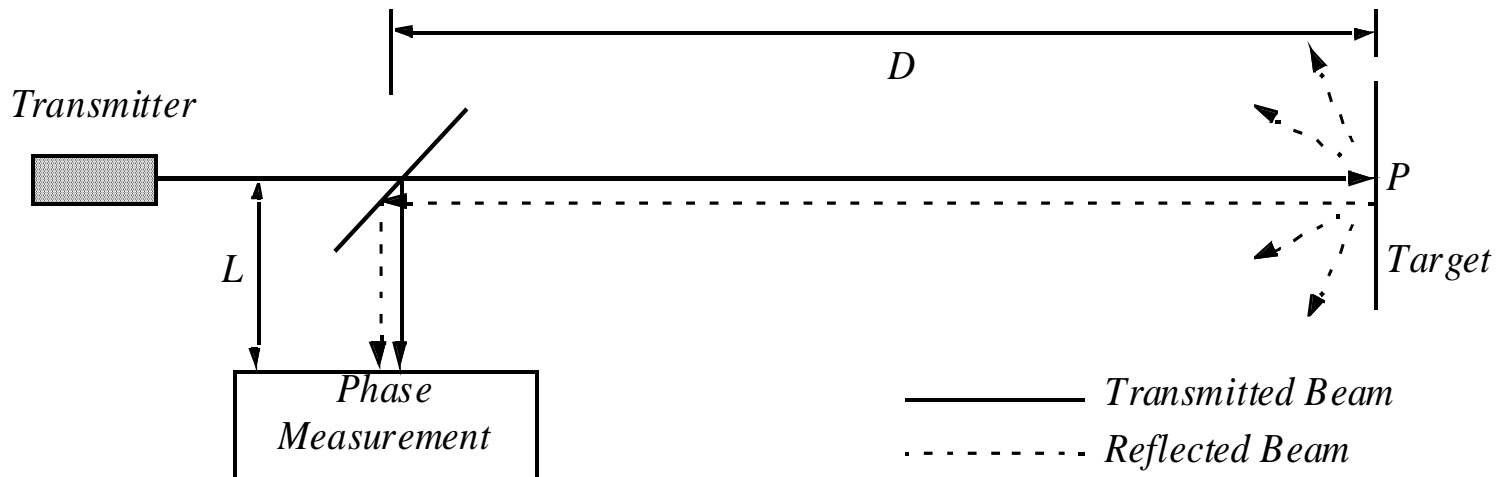
$$D = \lambda\theta / (4\pi)$$

where  $\theta$  is the phase difference between the transmitted signal





# Laser Range Sensor: Phase-Shift Measurement



where  $\lambda = c/f$ ,  $D' = L + 2D = L + \theta\pi/(2\pi)$

$c$  = is the speed of light

$f$  = the modulating frequency

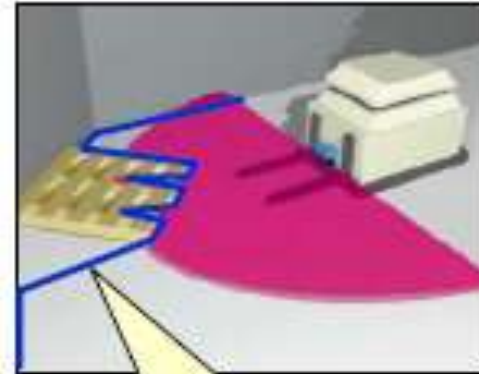
$D'$  = covered by the emitted light is

for  $f = 5$  Mhz (as in the A.T&T. sensor),  $\lambda = 60$  meters



# Laser Range Finders: Accuracy

- Accuracy
  - ±1.5 cm in short range (1m – 8m)
  - ±4.0 cm in long range (8m – 20m)
- Typically measures ranges up to 50m
- Scanning at multiple heights, produces contour lines that can be stacked to form a model



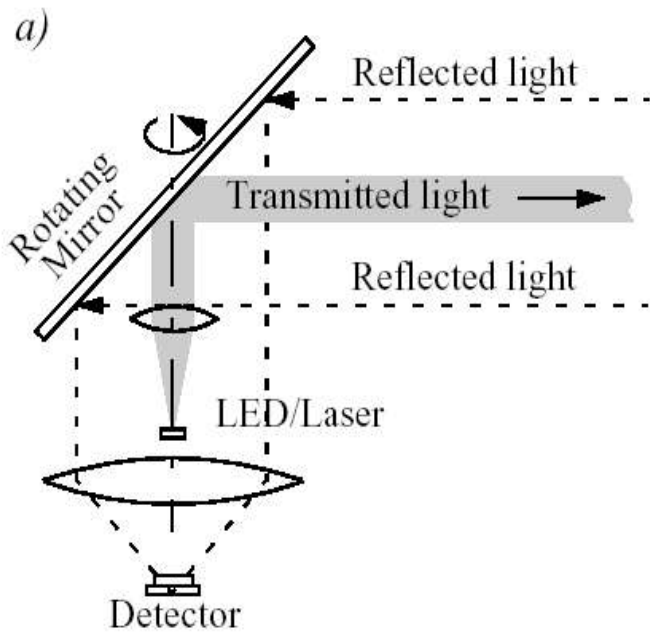
Result of scan at single height level is a *visibility polygon*





# Laser Range Sensor: 3 types

Scanning range sensor



Laser with rotating mirror

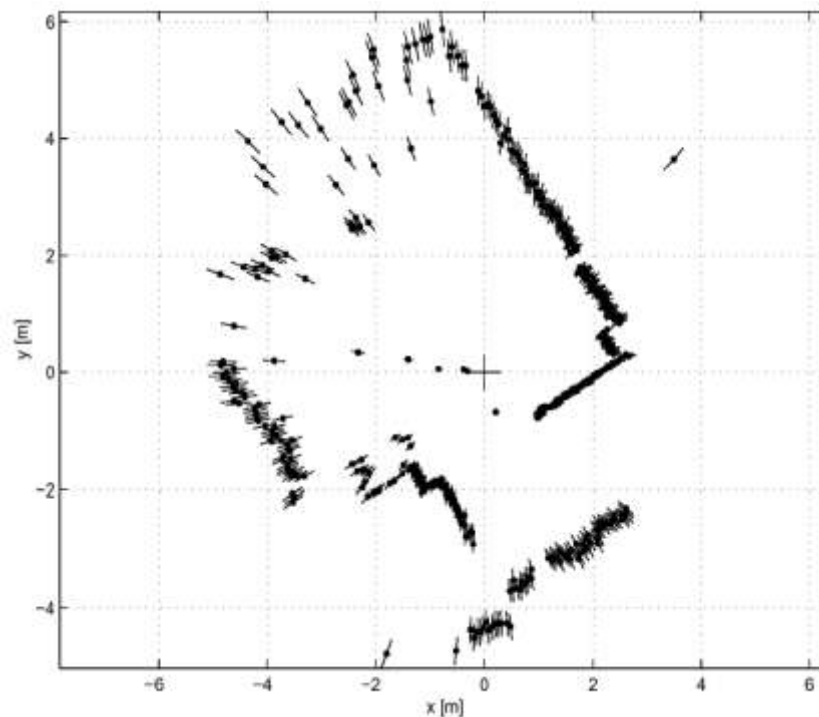


180° laser range sensor



# Laser Range Sensor

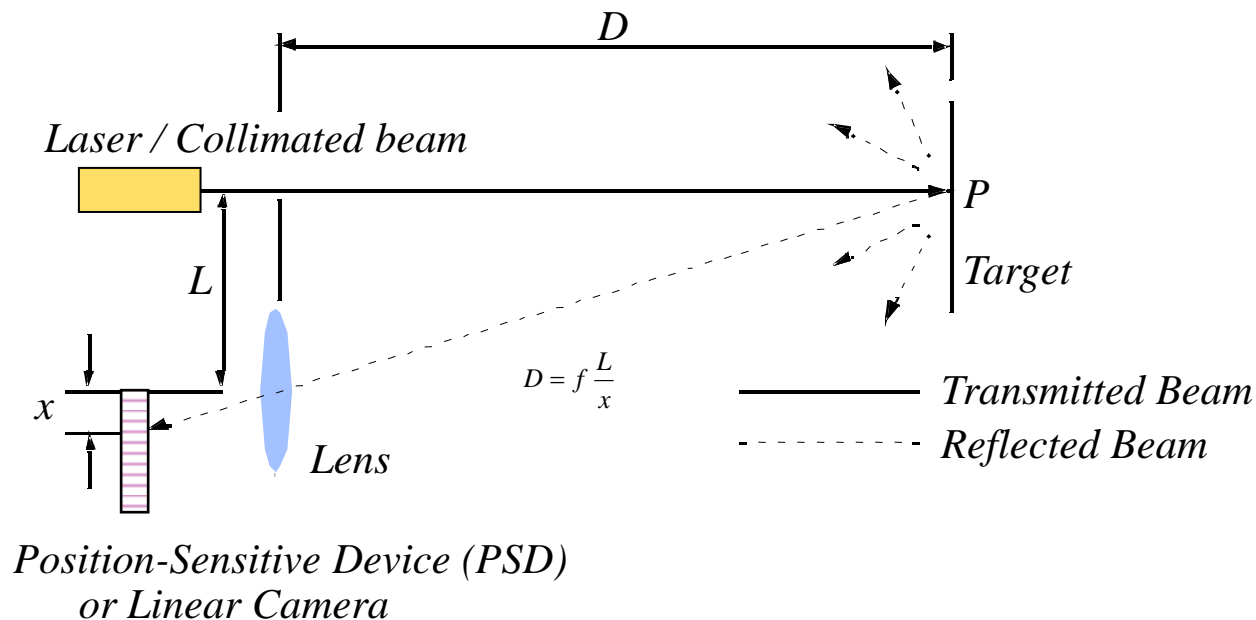
Typical range image of a 2D laser range sensor with a rotating mirror. The length of the lines through the measurement points indicate the uncertainties.





# Optical Triangulation (1D Sensor)

- ◉ *Triangulation-based* ranging sensors use geometric properties to measure the distance to objects
- ◉  $D = f \cdot L/x$
- ◉ Sensor resolution is best for close objects





# Laser Range Finders:

## Advantages and Disadvantages

### ⦿ Advantages

- Better resolution than ultrasonic, infrared, and cameras
- Very reliable
- Not as sensitive to lighting conditions as cameras and infrared
- For mapping, lasers are high quality 3D versions of IR sensors

### ⦿ Disadvantages

- Cannot identify mirrors and/or glass
- More expensive than all other sensors
- Larger and heavier than all other sensors