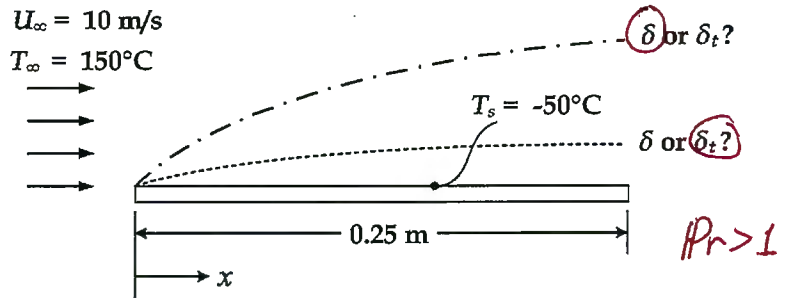


**Problem 1 (11 pts)**

A fluid called Dynalene HC ( $\rho=1200 \text{ kg/m}^3$ ,  $\mu=2.5 \times 10^{-3} \text{ kg/m}\cdot\text{s}$ ,  $k=0.504 \text{ W/m}\cdot^\circ\text{C}$ , and  $Pr=16$ ) flows over a 0.25-m-long flat plate with a velocity of  $U_\infty=10.0 \text{ m/s}$  and temperature  $T_\infty=150^\circ\text{C}$ . The plate is maintained at  $T_s=-50^\circ\text{C}$ . Dimensions are shown in the figure.



(a) [1 pt] At what temperature have the properties of Dynalene HC been evaluated?

$$T_f = \frac{T_s + T_\infty}{2} = \frac{-50^\circ\text{C} + 150^\circ\text{C}}{2} = 50^\circ\text{C}$$

ANS

(b) [2 pts] Boundary layer profiles are shown in the figure. On the figure, circle which boundary layer is the velocity boundary layer thickness ( $\delta_v$ ) and which is the thermal boundary layer thickness ( $\delta_T$ ).

(c) [3 pts] Determine whether the flow is entirely laminar, entirely turbulent or whether it transitions somewhere along the plate (Note: >90% of the plate is sufficient for "entirely.")

$$Re_{cr} = 500,000 = \frac{\rho x_{cr} U_\infty}{\mu}$$

$$x_{cr} = \frac{Re_{cr} \cdot \mu}{\rho U_\infty} = \frac{(500,000)(2.5 \times 10^{-3} \frac{\text{kg}}{\text{m}\cdot\text{s}})}{(1200 \frac{\text{kg}}{\text{m}^3})(10 \frac{\text{m}}{\text{s}})} = 0.10 \text{ m}$$

$$x_{cr} = 0.417 L \rightarrow \text{Combined laminar/turbulent flow}$$

(d) [5 pts] Determine the total average convective heat transfer coefficient between the Dynalene HC and the plate.

- Combined laminar/turbulent
- Flat plate
- $T_s = \text{const BC}$

$$Nu = (0.037 Re^{0.8} - 871) Pr^{1/3}$$

$$Re_L = \frac{\rho U_\infty L}{\mu} = \frac{(1200 \frac{\text{kg}}{\text{m}^3})(10 \frac{\text{m}}{\text{s}})(0.25 \text{ m})}{2.5 \times 10^{-3} \frac{\text{kg}}{\text{m}\cdot\text{s}}} = 1,200,000$$

$$Nu = (0.037 \cdot 1,200,000^{0.8} - 871) 16^{1/3} = 4612$$

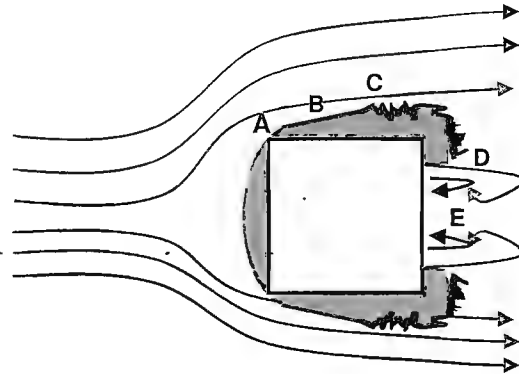
$$h = \frac{k Nu}{L} = \frac{(0.504 \frac{\text{W}}{\text{m}\cdot^\circ\text{C}})(4612)}{0.25 \text{ m}}$$

$$= 9297 \text{ W/m}^2\cdot^\circ\text{C}$$

ANS

**Problem 2** (3 pts)

Consider flow around a rod once again. The figure below shows the flow patterns around such a rod.



Choose the *best* description of what is happening at the given locations in the figure.

(a) Location B

- A. Boundary layer detachment
- B. Boundary layer thickening
- C. Transition to turbulence

(b) Location C

- A. Boundary layer detachment
- B. Boundary layer thickening
- C. Transition to turbulence

(c) Location D

- A. Boundary layer detachment
- B. Boundary layer thickening
- C. Transition to turbulence

**Problem 4** (6 pts)

- (a) **True** |  **False:** Biot number is  $Bi = hL_c/k$  and Nusselt number is  $Nu = hL_c/k$ . They are therefore the same number but used differently in different applications.
- (b)  **True** | **False:** When Nusselt number is one ( $Nu = 1$ ) there is no convection heat transfer.
- (c) **True** |  **False:** Viscous effects can be ignored inside a boundary layer.
- (d)  **True** | **False:** Thin thermal boundary layers produce larger heat transfer coefficients than thick boundary layers.
- (e) **True** |  **False:** For flow around cylinders, both frontal area and surface area can be used to find heat transfer
- (f) **True** |  **False:** Flow at extremely small Reynolds numbers is called "creep" in honor of the band *Radiohead*. (The answer is False, though it is true that small Reynolds number flows are called creep flows)