

3: (6 pts.) Let X be the number of kings in a 5-card hand drawn from a well-shuffled deck of cards. Derive an expression for $P(0 < X < 2)$ but do not simplify it.

$$\begin{aligned}
 P(0 < X < 2) &= P(X=1) \\
 &= P_X(1) = \frac{\binom{4}{1} \binom{48}{4}}{\binom{52}{5}}
 \end{aligned}$$

4: (4 pts.) Let W be a continuous RV with density function

$$f_W(w) = \begin{cases} c/w^2, & w \geq 1 \\ 0, & \text{elsewhere} \end{cases}$$

Prove or disprove: $E[W^2]$ exists.

$$E[W^2] = \int_1^{\infty} w^2 \cdot \frac{c}{w^2} dw = \int_1^{\infty} c dw = c w \Big|_1^{\infty} = \infty$$

$\therefore E[W^2]$ does not exist.

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