

4: A poker hand consists of 5 cards drawn at random from a deck of 52 cards having 13 denominations and 4 suits. Compute the probability of drawing a "full house" hand. A "full house" hand consists of three cards from one denomination, e.g., three eights and two jacks. Derive an expression for this probability but do not simplify or evaluate it.

$$\begin{aligned}
 P(\text{"full house"}) &= \frac{13 \cdot 12 \cdot \binom{4}{3} \binom{4}{2}}{\binom{52}{5}} \quad \left. \vphantom{\frac{13 \cdot 12 \cdot \binom{4}{3} \binom{4}{2}}{\binom{52}{5}}} \right\} 1 \\
 &= \frac{{}^{13}P_2 \cdot 4C_3 \cdot 4C_2}{52C_5}
 \end{aligned}$$

5: A group of friends take a road trip together. They travel in 4 cars. Each car will stop for gas only once during the trip. There are 7 gas stations along the route. Derive - but do not simplify - an expression for the probability that two or more cars stop at the same gas station.

$$\begin{aligned}
 P(\text{"2 or more"}) &= 1 - P(\text{"no 2 cars at same station"}) \\
 &= 1 - \frac{7 \cdot 6 \cdot 5 \cdot 4}{7^4}
 \end{aligned}$$