## Signal Conditioning Problems

## Conceptual



Fig. P9.1

1. $T / F$ Circuit on left: $R_{f}=10 \mathrm{k} \Omega, \mathrm{R}_{\text {in }}=5 \mathrm{~K} \Omega, \mathrm{C}=0.01 \mu \mathrm{~F}$. The circuit is a high-pass filter with a high-frequency gain of 2 and a break frequency of $2\left(10^{4}\right) \mathrm{Hz}$.
2. $T / F$ Circuit in middle: $R_{f}=20 \mathrm{k} \Omega, \mathrm{R}_{\text {in }}=4 \mathrm{~K} \Omega, \mathrm{C}_{\text {in }}=0.1 \mu \mathrm{~F}, \mathrm{C}_{\mathrm{f}}=10 \mathrm{pF}$. For $\mathrm{V}_{\text {in }}=20 \cos \left(10^{5} \mathrm{t}\right)$ $\mathrm{mV},\left|\mathrm{V}_{\mathrm{o}}\right|$ is approximately 100 mV .
3. $T / F$ Circuit on right:. $R_{f}=10 k \Omega, R_{i n}=5 K \Omega, C=0.1 \mu F$. The circuit is a low-pass filter with a lowpass gain of 2 and a break frequency of $1000 \mathrm{r} / \mathrm{s}$.
4. T/F Time and frequency domain. Lowering the time constant of a $1^{\text {st }}$-order low-pass filter will result in a lower break frequency.
5. T/F Time and frequency domain. Lowering the break frequency of a low-pass filter will allow it, in its time-domain response to a step function input, to reach its steady-state value more quickly.
6. T/F A low-pass filter with $\omega_{b}=1000 \mathrm{r} / \mathrm{s}$ and a DC gain of 10 has a transfer function of $10 /(\mathrm{s}+1000)$ and its time-domain response to an input of $1 u(\mathrm{t}) \mathrm{V}$ is $10\left(1-e^{-1 / 1000}\right) \mathrm{V}$. Why or why not?

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Fig. P9. 2
7. An ideal op-amp is used to measure strain as shown above. Given a nominal $1 \mathrm{k} \Omega$ resistance for the strain gage, and a strain gage factor of $2, \mathrm{v}_{\text {out }}=4.004 \mathrm{~V}$ if the strain, $\varepsilon=0.001$.
8. Given the same strain gage, $\mathrm{v}_{\text {out }}=4 \cos 10 \mathrm{tmV}$ if the strain, $\varepsilon=0.001 \cos (10 \mathrm{t})$.

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Fig. P9. 3
9. T/F Time-domain response. Increasing C will lower the magnitude of the static gain coefficient.
10. T/F Time-domain response. Increasing $R_{f}$ will increase the time constant.
11. $\mathbf{T} /$ F Frequency-domain response. Lowering $R_{\text {in }}$ will lower the break frequency.
12. $\mathbf{T} / \mathbf{F}$ Frequency-domain response. Increasing $R_{f}$ will increase magnitude of the $D C$ gain.

For the next two questions, $\operatorname{TF}(\mathrm{s})=\frac{\mathrm{V}_{0}(\mathrm{~s})}{\mathrm{V}_{\mathrm{in}}(\mathrm{s})}=\frac{1000}{\mathrm{~s}+20}$
13. $\mathbf{T} / \boldsymbol{F}$ If $v_{\text {in }-1}=5 \cos (10 \mathrm{t}) \mathrm{V}$ and $\mathrm{v}_{\text {in- }-2}=50 \cos (100 \mathrm{t}) \mathrm{V}$, the steady-state amplitude of $\mathrm{v}_{\text {out-1 }}$ will be greater than $v_{\text {out-2. }}$. Why or why not?
14. $T / F$ If $v_{\text {in- }-1}=1000 \cos \left(10^{4} t\right) V$ and $v_{\text {in- }-2}=10 \cos (500 t) \mathrm{V}$, the steady-state amplitude of $v_{\text {out }-2}$ is greater than $\mathrm{v}_{\text {out-1 }}$. Why or why not?

15. $\quad \mathbf{T} / \boldsymbol{F}$ Increasing C in the high-pass filter will lower its break frequency.
16. $\mathbf{T} / \boldsymbol{F}$ Increasing $\mathrm{R}_{\text {in }}$ in the bandpass filter has no effect on its lower break frequency .
17. $\mathbf{T} / \boldsymbol{F}$ Increasing $C$ in the high-pass filter has no effect on its high-frequency gain.
18. $\mathbf{T} / \boldsymbol{F}$ Increasing $\mathrm{C}_{\text {in }}$ in the bandpass filter has no effect on its passband gain.
19. $\mathbf{T} / \boldsymbol{F}$ The gain of an op-amp amplifier is independent of frequency.
20. $\boldsymbol{T} / \boldsymbol{F}$ An amplifier have a gain of G is needed. Using identical op-amps, a two-stage amplifier (each stage having a gain of $\sqrt{ } \mathrm{G}$ ) will maintain its gain at higher frequencies than a singlestage amplifier.
21. $\mathbf{T} / \mathbf{F} \quad \mathbf{1}^{\text {st }}$-order low-pass filter has a high-frequency slope of $-20 \mathrm{~dB} / \mathrm{dec}$, and a $2^{\text {nd }}$-order filter would have a high-frequency slope of $-40 \mathrm{~dB} / \mathrm{dec}$.
22. T/F The voltage at which an op-amp circuit saturates increases as the power supply voltage, $\mathrm{V}_{\mathrm{cc}}$, increases.
23. T/F An op-amp buffer circuit is useful when a signal source has a very high Thevenin impedance. Why or why not?
24. T/F An instrumentation amplifier can be described as a differential amplifier with buffered inputs.


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Fig. P9. 5
25. $\boldsymbol{T} / \boldsymbol{F}$ The gain, $\left|\mathrm{V}_{\mathrm{o}} / \mathrm{V}_{\mathrm{s}}\right|$, for the circuit on the left varies with $\mathrm{R}_{\mathrm{s}}$.
26. $\mathbf{T} / \boldsymbol{F}$ The gain, $\left|V_{0} / V_{s}\right|$, for the circuit on the right is not a function of $R_{s}$.
27. $\mathbf{T} / \boldsymbol{F}$ The gain, $\left|V_{o} / V_{s}\right|$, for the circuit on the left cannot be less than one, whereas the gain for the circuit on the right can be less than one.

## Workout

1. i) Classify the amplifier model shown below.
ii) Express $\mathrm{V}_{0}$ as a function of $\mathrm{V}_{\mathrm{s}}$.
iii) Given $\mathrm{V}_{\mathrm{s}}$, what is the maximum possible amplification?
iv) To obtain the amplification given in iii), what how must $R_{i}$ be related to $R_{s}$ ? How must $R_{0}$ be related to $R_{L}$ ?


Fig. P9. 6
2. i) Classify the amplifier model shown below.
ii) Express $\mathrm{V}_{0}$ as a function of $\mathrm{V}_{\mathrm{s}}$.
iii) Given $\mathrm{V}_{s}$, what is the maximum possible amplification?
iv) To obtain the amplification given in iii), what how must $R_{i}$ be related to $R_{s}$ ? How must $\mathrm{R}_{0}$ be related to $\mathrm{R}_{\mathrm{L}}$ ?


Fig. ${ }^{-1} \overline{9} . \overline{7}$
3. i) Classify the amplifier model shown below.
ii) Express $\mathrm{V}_{0}$ as a function of $\mathrm{V}_{s}$.
iii) Given $\mathrm{V}_{\mathrm{s}}$, what is the maximum possible amplification?
iv) To obtain the amplification given in iii), what how must $R_{i}$ be related to $R_{s}$ ? How must $R_{0}$ be related to $R_{L}$ ?

4. i) Classify the amplifier model shown below.
ii) Express $\mathrm{V}_{0}$ as a function of $\mathrm{V}_{\mathrm{s}}$.
iii) Given $\mathrm{V}_{\mathrm{s}}$, what is the maximum possible amplification?
iv) To obtain the amplification given in iii), what how must $R_{i}$ be related to $R_{s}$ ? How must $R_{0}$ be related to $R_{L}$ ?


Fig. P9.9
5. The example below uses a photoconductor as part of an optical detector. Assume the photoconductor's resistance, $\mathrm{R}_{\mathrm{pc}}$, varies as shown. A current source is intended to convert changes of resistance into changes of voltage.
i) Design an amplifier circuit which amplifies $\mathrm{V}_{\mathrm{pc}}$ so that, when the light power is 100 mW , the output voltage is 10 V .
ii) Design the amplifier to have a very high input resistance ( $\mathrm{i}_{\text {in }}$ very small).

Explain why this is desirable.
iii) Give the overall sensitivity of the detector (photoconductor circuit + amplifier in $\mathrm{V} / \mathrm{mW}$ ).

photoconductor
transfer characteristic

photoconductor circuit
Fig. P9. 10
6. Choose $R_{1}, R_{2}, R_{3}$, and $R_{4}$ so that:
i) $\mathrm{V}_{\text {o-1st stage }}=0.4 \mathrm{~V}$ when the temperature is $1250^{\circ} \mathrm{C}$.
ii) $V_{0-2 n d \text { stage }}=-8 \mathrm{~V}$ when the temperature is $1250^{\circ} \mathrm{C}$.
iii) Plot $\mathrm{V}_{\mathrm{o}-2 \text { nd stage }}$ as a function of temperature for $500^{\circ} \mathrm{C}<$ temp $<1250^{\circ} \mathrm{C}$.

Use resistance value between $1 \mathrm{k} \Omega$ and $100 \mathrm{~K} \Omega$.


Fig. P9. 11
7. A system for monitoring the effectiveness of a process in removing a compound from a product stream. Design for $\mathrm{V}_{0}$ to vary from -5 V to 5 V as the concentration difference C1-C2 varies between -200 and 200 ppm.

Find:
i) The sensitivity of the sensor probes (in $\mathrm{mV} / \mathrm{ppm}$ ).
ii) The values for the resistances (choose between $2 \mathrm{k} \Omega$ and $200 \mathrm{k} \Omega$ ).
iii) The sensitivity of the resulting detector (in $\mathrm{mV} / \mathrm{ppm}$ ).


Fig. P9. 12
8. In the circuit below, $R=R_{0}+\Delta R$ is the resistance of a resistive sensor.
i) Show that $V_{0}$ may be expressed as $V_{s}(-\Delta R) /\left(R_{1}+R_{0}\right)$.
ii) Find the sensitivity of $V_{0}$ with respect to $\Delta R$. That is, find $d V_{0} / d \Delta R$
iii) In a practical op-amp circuit, could $R$ be a $120 \Omega$ strain gage? Why or why not?


Fig. P9. 13
9. Using the ideal op-amp model, find $\mathrm{i}_{\mathrm{o}}$.


Fig. P9. 14
10. Find $V_{0}$.


Fig. P9. 15
11. Using an op-amp in the inverting configuration, design a low-pass filter with a break frequency of $1000 \mathrm{rad} / \mathrm{sec}$ and a low-pass gain magnitude of 10 . Use $\mathrm{R}_{\mathrm{in}}=10 \mathrm{kO}$.
i) Sketch the circuit showing the calculated values of $R_{f}$ and $C$.
ii) Given the transfer function.
iii) Using semilog paper, give the straight-line Bode magnitude plot
12. When a given load is placed on a four-active arm cantilever load cell, $\varepsilon=0.0004$.
i) What is $V_{b}$ ?
ii) Specify $R_{b}$ in the amplifier below to give an output of $V_{0}=60 \mathrm{mV}$. Use $R_{a}=2 \mathrm{k} \Omega$ and
assume $\mathrm{S}=2, \mathrm{~V}_{\mathrm{s}}=15 \mathrm{~V}$, and $\mathrm{R}_{1}, \mathrm{R}_{2}, \mathrm{R}_{3}$, and $\mathrm{R}_{4}$ to all be $350 \Omega$ strain gages.


Fig. P9. 16
iii) A filtering stage is needed. Design an active bandpass filtering stage to filter $\mathrm{V}_{0}$ with $\omega_{L}=100 \mathrm{r} / \mathrm{s}, \omega_{\mathrm{L}}=5000 \mathrm{r} / \mathrm{s}$ and a gain at resonance of 10 . Use $\mathbf{R}_{\mathrm{in}}=10 \mathrm{k} \Omega$.
Neatly add this stage to the above schematic.
iii) Using semilog paper, neatly sketch the straight line Bode magnitude plot for $\left|V_{\text {out-bp filter }} / V_{b}\right|$


Fig. P9. 17
13. i) Design a low-pass filtering stage to the amplifier below so that the overall system transfer function has a DC gain of 100 and a break frequency of $10000 \mathrm{r} / \mathrm{s}$.
ii) Neatly sketch the LP filtering stage in the space provided below. For the filter use $R_{f}=$ $100 \mathrm{k} \Omega$.


Fig. P9. 18
iii) Give the overall transfer function in Bode form.
iv) Using semilog paper, plot the straight-line Bode magnitude plot for the overall system.


Fig. P9. 19
14. A force measurement transducer has a voltage output and has an underdamped $2^{\text {nd }}$ order response $\left(K_{s}=4 \mathrm{mV} / \mathrm{N}, \zeta=0.2, \omega_{\mathrm{n}}=100 \mathrm{r} / \mathrm{s}\right)$.

$$
\frac{1}{\omega_{n}^{2}} \frac{d^{2} v}{\mathrm{dt}^{2}}+\frac{2 \zeta}{\omega_{\mathrm{n}}} \frac{\mathrm{dv}}{\mathrm{dt}}+\mathrm{v}=\mathrm{K}_{\mathrm{s}}
$$

Use phasor analysis to determine the actual steady-state force, $\mathrm{f}(\mathrm{t})$, when the measured steady-state voltage is $\mathrm{v}(\mathrm{t})=[20+50 \cos (150 \mathrm{t})] \mathrm{mV}$.
Hint: Review system dynamics.
15. The TC voltage plot below results when a thermocouple sensing junction, at $\mathrm{t}=4$ seconds, is transferred from a temperature of $20^{\circ} \mathrm{C}$ to $100^{\circ} \mathrm{C}$. (For a temperature of $0^{\circ} \mathrm{C}$, the steadystate voltage is OW
Given that the TC behaves as a $1^{\text {st- }}$-order system, extract the system parameters and give the differential equation that relates the input TC temperature and output TC voltage.

$$
\tau \frac{\mathrm{dv}}{\mathrm{dt}}+\mathrm{v}=\mathrm{K}_{\mathrm{s}} \mathrm{~T}
$$

Hint: Review system dynamics.


Fig. P9. 20
16. A thermocouple is used to measure temperature. The output voltage for $\mathrm{T}=0^{\circ} \mathrm{C}$ is 0 V . The plot below is taken as the thermocouple is taken from $400^{\circ} \mathrm{C}$ to $0^{\circ} \mathrm{C}$ at $\mathrm{t}=2 \mathrm{~s}$. Assume the TC behaves as a $1^{\text {st }}$-order system.

$$
\tau \frac{\mathrm{dv}}{\mathrm{dt}}+\mathrm{v}=\mathrm{K}_{\mathrm{s}} \mathrm{~T}
$$

i) Find the approximate differential equation relating input temperature to thermocouple voltage. Identify the time constant, $\tau$, and the static gain coefficient, K.

Don't forget units.
ii) For the same thermocouple, give the thermocouple voltage, in steady-state, if its surrounding temperature, in ${ }^{\circ} \mathrm{C}$, is $\mathrm{T}=400+20$ cos t.


Fig. P9. 21
17. i) Find the transfer function, $\mathrm{V}_{0} / \mathrm{V}_{\mathrm{s}}$, of the circuit shown below.
ii) Sketch the Bode magnitude plot for the circuit shown below given $R_{1}=1 \mathrm{k} \Omega, R_{2}$ $=100 \Omega, C=0.1 \mu \mathrm{~F}$, and $\mathrm{L}=10 \mu \mathrm{H}$.
iii) What is $v_{0}(t)$, in steady-state, given $v_{s}(t)=10 \cos 10^{4} t V$.
iv) What is $v_{0}(t)$, in steady-state, given $v_{s}(t)=10 \cos 10^{6} t V$.
v) What is $v_{0}(t)$, in steady-state, given $v_{s}(t)=10 \cos 10^{8} t V$.


Fig. P9. 22
17. Let $\mathrm{V}_{\mathrm{s}}$ be a sinusoidal signal ( 2 V amplitude, with a frequency of $4000 \mathrm{r} / \mathrm{s}$ ) corrupted by high frequency noise ( 1 V amplitude, frequency $32 \mathrm{kr} / \mathrm{s}$ ).
i) What is the signal-to-noise ratio of $\mathrm{V}_{\mathrm{s}}$.
ii) Design an active first-order low-pass filter using an op-amp in the inverting configuration. Let the low-frequency gain be 1 and the break frequency be $8000 \mathrm{r} / \mathrm{s}$. Use $\mathrm{R}_{\text {in }}=10 \mathrm{k} \Omega$.
iii) If $\mathrm{V}_{\mathrm{s}}$ is input to the op-amp circuit design in ii), what is the signal-to-noise ratio at the output?
iv) Design an active second-order Sallen-Key low-pass filter. Let the lowfrequency gain be 1 and the break frequency be $8000 \mathrm{r} / \mathrm{s}$. Choose $\zeta=0.7$.
v) If $\mathrm{V}_{\mathrm{s}}$ is input to the op-amp circuit in iv), what is the signal-to-noise ratio at the output?
vi) Compare the filtering effectiveness of the $1^{\text {st }}$-order filter to the $2^{\text {nd }}$-order filter.
18. Let $\mathrm{V}_{\mathrm{s}}$ be a sinusoidal signal ( 2 V amplitude, with a frequency of 5 kHz ) corrupted by low frequency noise ( 1 V amplitude, frequency 60 Hz ) and by high frequency noise ( 5 V amplitude, frequency 40 kHz ).
i) Design an active Sallen-Key band-pass filter. Let the center frequency be 5 kHz and let the quality factor be 10 . Choose $R=10 \mathrm{k} \Omega$.
ii) Let $\mathrm{V}_{\mathrm{s}}$ be input to the circuit designed in i). Compare the signal-to-noise ratios at the input to those at the output.
19. Let $\mathrm{V}_{\mathrm{s}}$ be a sinusoidal signal ( 2 V amplitude, with a frequency of 5 kHz ) corrupted by low frequency noise ( 1 V amplitude, frequency 60 Hz ) and by high frequency noise ( 5 V amplitude, frequency 40 kHz ).
i) Design an active Sallen-Key band-pass filter. Let the center frequency be 5 kHz and let the quality factor be 10 . Choose $\mathrm{R}=10 \mathrm{k} \Omega$.
ii) Let $\mathrm{V}_{\mathrm{s}}$ be input to the circuit designed in i). Compare the signal-to-noise ratios at the input to those at the output.
20. Let $\mathrm{V}_{\mathrm{s}}$ be a sinusoidal signal ( 2 V amplitude, with a frequency of 6 kHz ) corrupted by low frequency noise ( 1 V amplitude, frequency 60 Hz ) and by high frequency noise ( 5 V amplitude, frequency 40 kHz ).
i) Design an active band-pass filter as described in Design Example 6.7.1. Let $f_{b}$ $=1.5 \mathrm{kHz}, \mathrm{f}_{\mathrm{u}}=12 \mathrm{kHz}$, and the passband gain $=2$. Choose $\mathrm{R}_{\mathrm{in}}=100 \mathrm{k} \Omega$.
ii) Let $\mathrm{V}_{\mathrm{s}}$ be input to the circuit designed in i). Compare the signal-to-noise ratios at the input to those at the output.
21. For each of the areas below, discuss the associated limitations of op-amps.
i) Current limitations of op-amps. What limits does this place on the resistances connected at the output of op-amps?
ii) Limits for op-amp output voltages.
iii) Limits associated with finite op-amp gain-bandwidth products.
22. i) Design an inverting amplifier, shown in Fig. with a |gain| of 10. Use $\mathrm{R}_{\text {in }}=7.5 \mathrm{k} \Omega$.
ii) Given $\mathrm{V}_{\mathrm{cc}}=9 \mathrm{~V}$, sketch $\mathrm{V}_{0}$ given the input is a 1 kHz triangle wave with a peak-to-peak amplitude of $1 / 2 \mathrm{~V}$.
iii) Given $\mathrm{V}_{\mathrm{cc}}=9 \mathrm{~V}$, sketch $\mathrm{V}_{0}$ given the input is a 1 kHz triangle wave with a peak-to-peak amplitude of 2 V .
iv) Given $\mathrm{V}_{\mathrm{cc}}=15 \mathrm{~V}$, sketch $\mathrm{V}_{0}$ given the input is a 1 kHz sinusoid with an RMS voltage of 5 V .


Fig. P9. 23
23. Using the amplifier shown in Fig., which shows the model accounting for finite gainbandwidth product and non-ideal input-output op-amp resistances, determine $\mathrm{v}_{0}(\mathrm{t})$ and the |gain| for the following frequencies.
i) $\quad \mathrm{DC}(\mathrm{f}=0)$
ii) $f=1000 \mathrm{~Hz}$
iii) $f=10 \mathrm{kHz}$
iv) $f=100 \mathrm{kHz}$
v) $f=1 \mathrm{MHz}$


Fig. P9. 24
24. Find $\mathrm{v}_{0}(\mathrm{t})$ and the signalto-noise ratio (the noise is the high frequency component) at the output. Design a first-order low-pass filter having a DC gain of 25 and a break frequency of $2 \omega$. Use the ideal op-amp model and choose $\mathrm{R}_{\mathrm{in}}=10 \mathrm{k} \Omega$.


Fig. P9. 25
i) $\quad D C(\omega=0)$
ii) $\omega=1000 \mathrm{r} / \mathrm{s}$
iii) $\omega=10 \mathrm{kr} / \mathrm{s}$
iv) $\omega=100 \mathrm{kr} / \mathrm{s}$
v) $\omega=1 \mathrm{Mr} / \mathrm{s}$
vi) $\omega=10 \mathrm{Mr} / \mathrm{s}$

Now, using the component values determines in i) - iv), and using the amplifier model shown in Fig. , which accounts for finite gain-bandwidth product and nonideal input-output op-amp resistances, determine $\mathrm{v}_{0}(\mathrm{t})$ and the signa-to-noise ratio at the output for the same values of $\omega$.


Fig. P9. 26


Fig. P9. 27

