

● Announcements:

- SHA due Tuesday
- Last exam Thursday
- Available for project questions this week
- You will evaluate each other's presentations during 10th week.

● Questions?

● Secret sharing

What is *secret splitting*?

- I have a secret M I want to share
- To figure it out, you'll need **teamwork**.

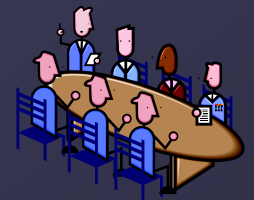
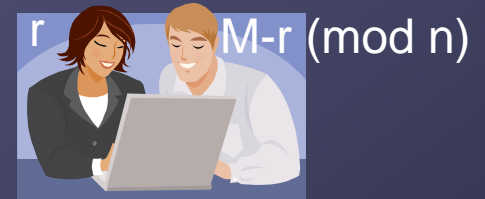
- Simple: use a sum

- Pick large $n > M$
- Pick a random r , $0 \leq r \leq n-1$
- To share between two people:

- Alice r , $M-r \pmod{n}$
- They can work together to sum

- Generalize to k people:

- r_1, r_2, \dots, r_{k-1} , and $M - \sum_{i=1}^{k-1} r_i \pmod{n}$



There are many applications of secret splitting and secret sharing

1. Inheritances
2. Military
3. Government
4. Information security

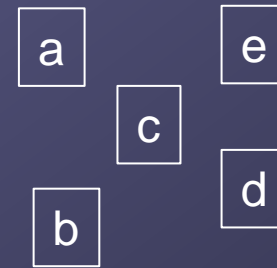
What if I wanted a **subset** of the people to be able to reconstruct the secret?

Secret splitting is trivial

Secret *sharing* is not!

(t,w) -threshold schemes require t people from a set of w to compute the secret

- Knowing t or more pieces makes M easily computable
- $t-1$ or fewer pieces leaves M **completely undetermined**
- If $(3,5)$ threshold scheme:
 - $\{a,d,e\}$ can figure out secret
 - $\{c,e\}$ cannot
 - $\{a,b,c,d\}$ is redundant

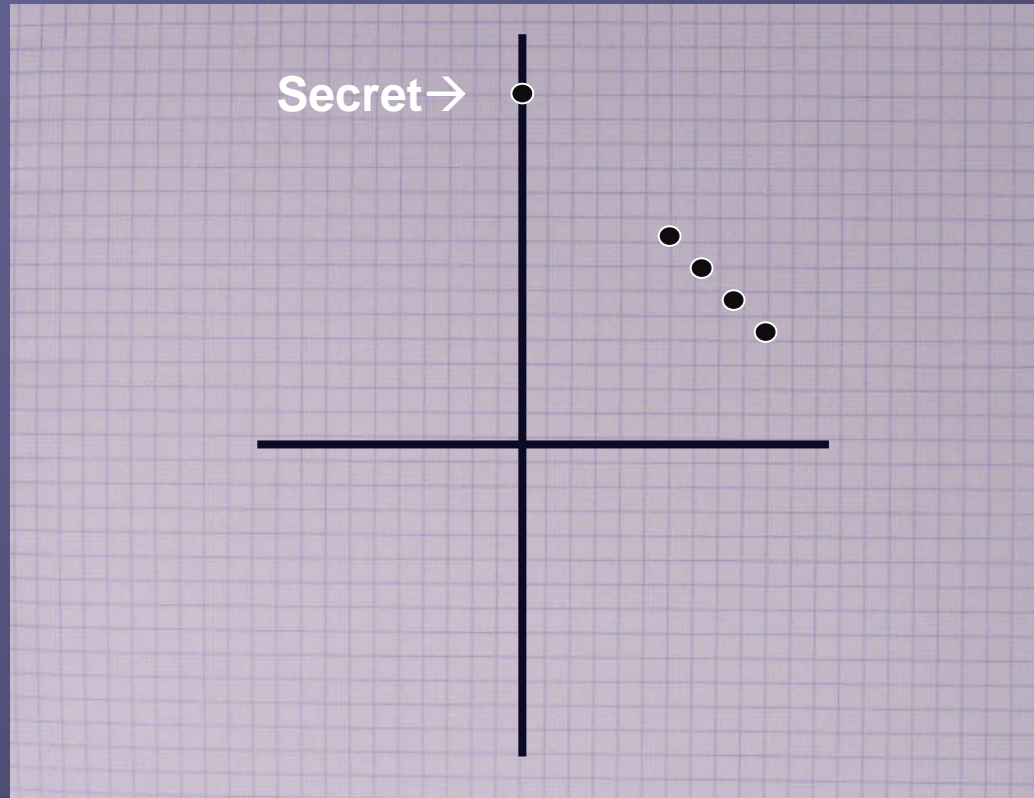


- Secret splitting (all participants required) is just a special case:
 - Let $t = w$

Idea: we can use curve fitting to reconstruct a function, and thus a message

The y-intercept of the line encodes the secret!

Here is a (2,4) scheme:

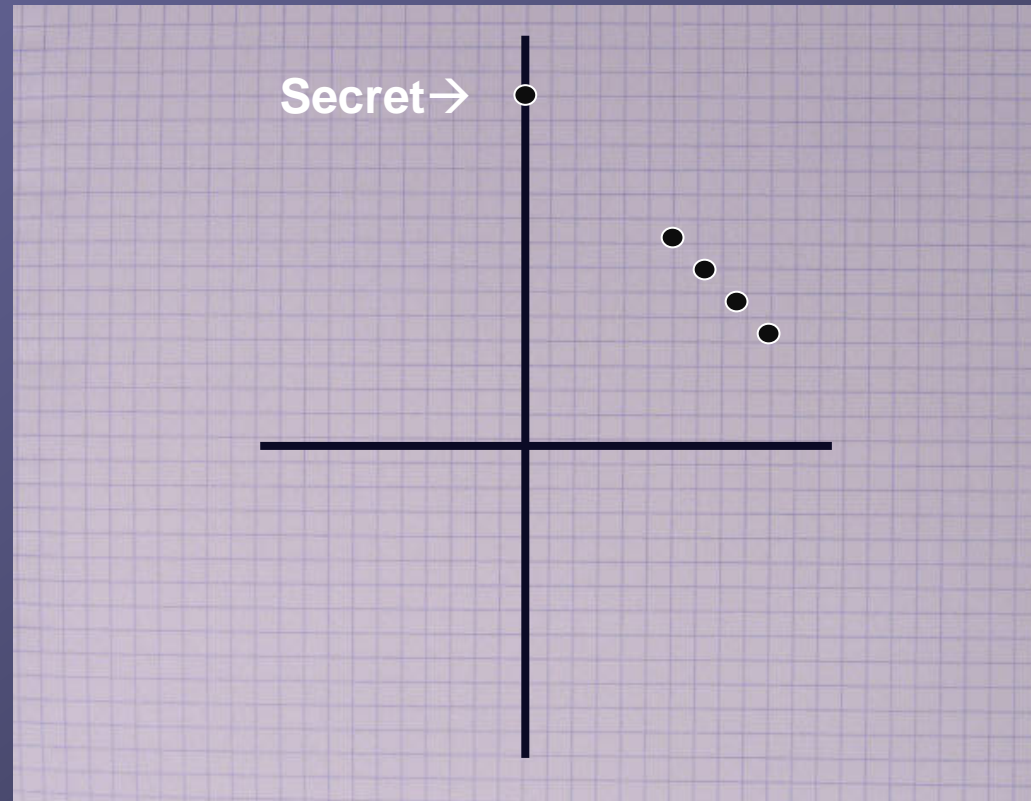


Your quiz question is an example of a (2,3) scheme

The Shamir threshold scheme uses curve-fitting with higher dimensions

The y-intercept of the line encodes the secret!

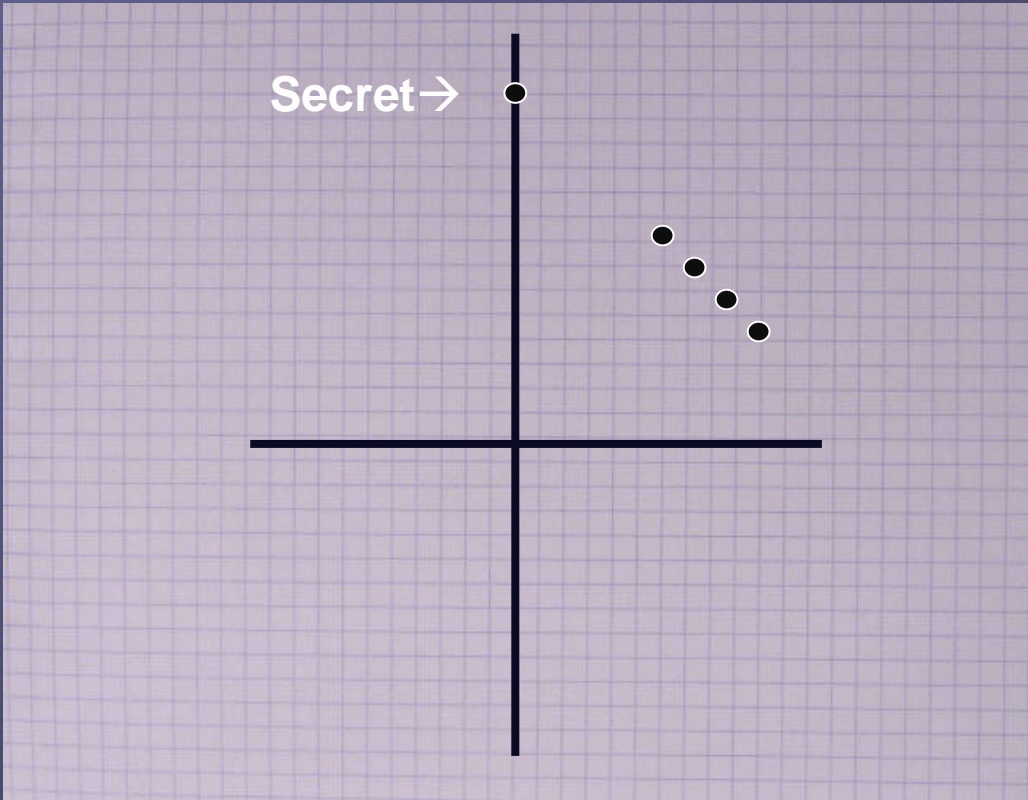
Derivation on board



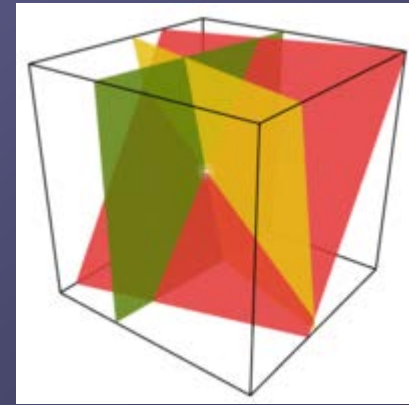
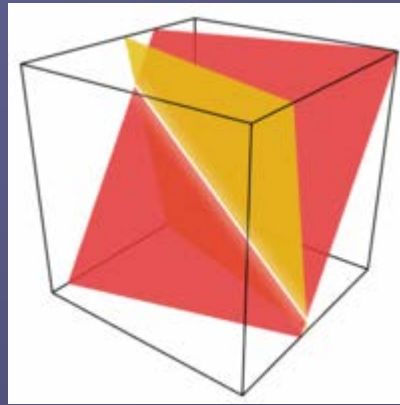
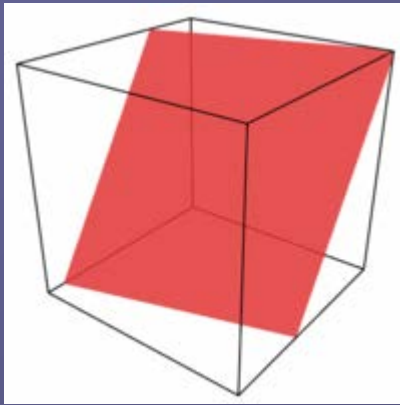
Extensions to Shamir

Multiple shares

Multiple groups of people

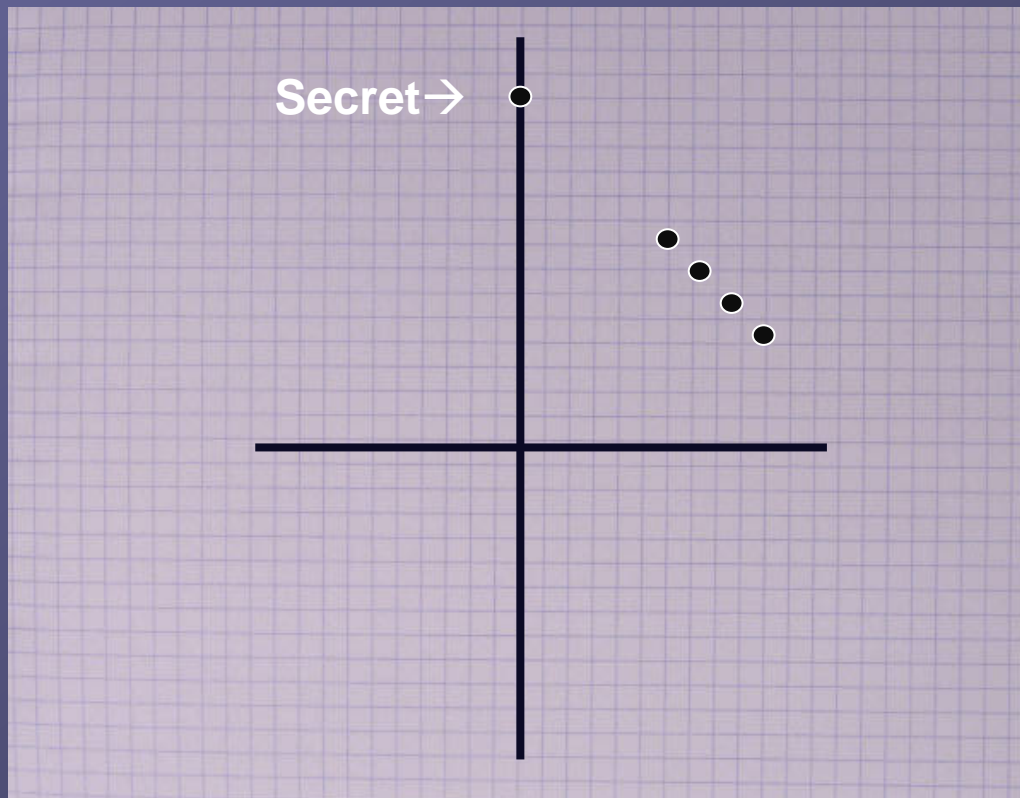


In the Blakely scheme, we represent the secret as the y-coordinate of the intersection of hyperplanes



Back to Shamir

The y-intercept of the line encodes the secret!



Your quiz question is an example of a $(4, 6)$ scheme

Project workday tomorrow: quiz due at 2:00 pm.