474 HW 6 problems (highlighted problems are the ones to turn in)

| Some problems were moved to | Describe in English, as briefly as possible, the language defined by each of these regular expressions: a. (b ∪ ba) (b ∪ a)* (ab ∪ b). b. (((a*b*)*ab) ∪ ((a*b*)*ba))(b ∪ a)*. Write a regular expressions to describe each of the following languages: a. {w ∈ {a, b}* : every a in w is immediately preceded and followed by b}. | 6.2: For the "to-turn-in" parts of 6.2, aim for as simple a regular expression as you can come up with. Some of the credit may be |
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| HW5 | b. $\{w \in \{a, b\}^* : w \text{ does not end in ba}\}.$ c. $\{w \in \{0, 1\}^* : \exists y \in \{0, 1\}^* (xy \text{ is even})\}.$ | for simplicity. If your expression is very |
| 6.2e 1 (3) 6.2h | d. {w ∈ {0,1}* : w corresponds to the binary encoding, without leading 0s, of natural numbers that are evenly divisible by 4}. e. {w ∈ {0,1}* : w corresponds to the binary encoding, without leading 0s, of natural numbers that are powers of 4}. Claude Anderson f. {w ∈ {0-9}* : w corresponds to the decimal encoding, without leading 0s, of | complicated, some annotation may help the grader to know whether it is correct. The "burden of |
| 2(3) 6.2l (el) | an odd natural number}. g. {w ∈ {0, 1}* : w has 001 as a substring}. h. {w ∈ {0, 1}* : w does not have 001 as a substring}. i. {w ∈ {a, b}* : w has bba as a substring}. j. {w ∈ {a, b}* : w has both aa and bb as substrings}. | did not require some of the more complex parts of this problem due to difficulties with grading, but you |
| <mark>3 (3)</mark> | k. {w ∈ {a, b}* : w has both aa and aba as substrings}. l. {w ∈ {a, b}* : w contains at least two b's that are not followed by an a}. m. {w ∈ {0, 1}* : w has at most one pair of consecutive 0s and at most one pair of consecutive 1s}. n. {w ∈ {0, 1}* : none of the prefixes of w ends in 0}. o. {w ∈ {a, b}* : #_a(w) ≡₃ 0}. | should try some of them. Note for part c: The x is a typo, should be w . wy means "the length of |
| <mark>6.3bcd</mark> <mark>4 (3-3-3)</mark> | p. {w∈ {a,b}*: #_a(w) ≤ 3}. q. {w∈ {a,b}*: w contains exactly two occurrences of the substring aa}. r. {w∈ {a,b}*: w contains no more than two occurrences of the substring aa}. s. {w∈ {a,b}* - L}, where L = {w∈ {a,b}*: w contains bba as a substring}. t. {w∈ {0,1}*: every odd length string in L begins with 11}. u. {w∈ {0.9}*: w represents the decimal encoding of an odd natural number without leading 0s. v. L₁ - L₂, where L₁ = a*b*c* and L₂ = c*b*a*. w. The set of legal United States zip codes □. x. The set of strings that correspond to domestic telephone numbers in yo country. 3. Simplify each of the following regular expressions: a. (a ∪ b)* (a ∪ e) b*. b. (Ø*∪ b) b*. c. (a ∪ b)*a*∪ b. d. ((a ∪ b)*)*. f. a ((a ∪ b)(b ∪ a))* ∪ a ((a ∪ b)a)* ∪ a ((b ∪ a) b)*. 4. For each of the following expressions E, answer the following three questio and prove your answer: i. Is E a regular expression? ii. If E is a regular expression, give a simpler regular expression. | string wy" r ur ns |
| | a. $((a \cup b) \cup (ab))^*$. b. $(a^+ a^n b^n)$. c. $((ab)^* \emptyset)$. d. $(((ab) \cup c)^* \cap (b \cup c^*))$. e. $(\emptyset^* \cup (bb^*))$. | |

