## 474 HW 6 problems (highlighted problems are the ones to turn in)

Some	<ol> <li>Describe in English, as briefly as possible, the language defined by each of these regular expressions:</li> </ol>	6.2: For the "to-turn-in" parts of 6.2, aim for as
problems	a. $(b \cup ba) (b \cup a)^* (ab \cup b)$ .	simple a regular expression
were	<b>b.</b> $(((a*b*)*ab) \cup ((a*b*)*ba))(b \cup a)*$ .	as you can come up with.
moved to	2. Write a regular expressions to describe each of the following languages:	Some of the credit may be
HW5	<ul> <li>a. {w ∈ {a, b}* : every a in w is immediately preceded and followed by b}.</li> <li>b. {w ∈ {a, b}* : w does not end in ba}.</li> </ul>	for simplicity. If your
	c. $\{w \in \{0, 1\}^* : \exists y \in \{0, 1\}^* ( xy  \text{ is even})\}.$	expression is very
<mark>6.2e</mark>	<ul> <li>d. {w ∈ {0, 1}* : w corresponds to the binary encoding, without leading 0s, of natural numbers that are evenly divisible by 4}.</li> </ul>	complicated, some annotation may help the
<mark>1 (3)</mark>	e. {w ∈ {0, 1}* : w corresponds to the binary encoding, without leading 0s, of natural numbers that are powers of 4}. Claude Anderson	grader to know whether it
<mark>6.2h</mark>	f. $\{w \in \{0.9\}^* : w \text{ corresponds to the decimal encoding, without leading 0s, of an odd natural number}\}$ .	is correct. The "burden of correctness" is on you. I
<mark>2(3)</mark>	<b>g.</b> $\{w \in \{0, 1\}^* : w \text{ has 001 as a substring}\}.$	did not require some of the
	h. $\{w \in \{0, 1\}^* : w \text{ does not have 001 as a substring}\}$ .	more complex parts of this
	i. $\{w \in \{a, b\}^* : w \text{ has bba as a substring}\}$ .	problem due to difficulties
<mark>6.2l (el)</mark>	<b>j.</b> $\{w \in \{a, b\}^* : w \text{ has both aa and bb as substrings}\}.$	with grading, but you
<mark>3 (3)</mark>	<b>k.</b> $\{w \in \{a, b\}^* : w \text{ has both aa and aba as substrings}\}.$	should try some of them.
	<b>I.</b> $\{w \in \{a, b\}^* : w \text{ contains at least two b's that are not followed by an a}.$	
	<b>m.</b> $\{w \in \{0, 1\}^* : w \text{ has at most one pair of consecutive 0s and at most one pair of consecutive 1s}.$	Note for part c: The
	<b>n.</b> $\{w \in \{0, 1\}^*$ : none of the prefixes of w ends in 0 $\}$ .	x is a typo, should be w.
	o. $\{w \in \{a, b\}^* : \#_a(w) \equiv_3 0\}.$	wy  means "the length of
	p. $\{w \in \{a, b\}^* : \#_a(w) \le 3\}.$	string wy"
	<b>q.</b> $\{w \in \{a, b\}^* : w \text{ contains exactly two occurrences of the substring aa}\}.$	
	<ul> <li>{w ∈ {a,b}* : w contains no more than two occurrences of the substring aa}.</li> </ul>	
C 2had	s. $\{w \in \{a, b\}^* - L\}$ , where $L = \{w \in \{a, b\}^* : w \text{ contains bba as a substring}\}$ .	
<mark>6.3bcd</mark> 8 (3-3-3)	<ul> <li>t. {w∈ {0,1}*: every odd length string in L begins with 11}.</li> <li>u. {w∈ {0-9}*: w represents the decimal encoding of an odd natural number without leading 0s.</li> </ul>	r
	v. $L_1 - L_2$ , where $L_1 = a^*b^*c^*$ and $L_2 = c^*b^*a^*$ .	
	w. The set of legal United States zip codes ⊒.	
	x. The set of strings that correspond to domestic telephone numbers in yo	ur
	country.	
	3. Simplify each of the following regular expressions:	
	<b>a.</b> $(\mathbf{a} \cup \mathbf{b})^* (\mathbf{a} \cup \varepsilon) \mathbf{b}^*$ .	
	<b>b.</b> $(\emptyset^* \cup \mathbf{b}) \mathbf{b}^*$ .	
	c. $(a \cup b)^*a^* \cup b$ .	
	d. $((a \cup b)^*)^*$ .	
	e. $((a \cup b)^+)^*$ .	
	<ul> <li>f. a ( (a ∪ b)(b ∪ a) )* ∪ a ( (a ∪ b) a)* ∪ a ((b ∪ a) b)*.</li> <li>4. For each of the following expressions E, answer the following three questions and the following three questions are as a construct of the following three questions are as a construct of the following three questions are as a construct of the following three questions are as a construct of the following three questions are as a construct of the following three questions are as a construct of the following three questions are a construct of the following three questions are as a construct of the followin</li></ul>	ne
	and prove your answer:	ns
	i. Is <i>E</i> a regular expression?	
	ii. If E is a regular expression, give a simpler regular expression.	
	iii. Does E describe a regular language?	
	a. $((a \cup b) \cup (ab))^*$ .	
	<b>b.</b> $(a^+ a^n b^n)$ .	
	<b>c.</b> $((ab)^* \emptyset)$ .	
	<b>d.</b> (((ab) $\cup$ c)* $\cap$ (b $\cup$ c*)).	
	<b>e.</b> $(\emptyset^* \cup (bb^*)).$	

