MA/CSSE 474 Day 35 Summary

1) An example of a program for which it is difficult to tell whether it always halts.

2) **The language H** = {<*M*, *w*> : TM *M* halts on input string *w*} Is H decidable?
   a) Of course we can decide halting for specific simple TMs. Or can we? (Collatz conjecture, 1937, still no proof).
   b) It's easy to see that H is semidecidable.
      M'_H(<*M*, *w*>) =
         1. Run *M* on *w*.
         2. Accept.
      i) M'_H accepts <*M*, *w*> iff M halts on input w.
      ii) *So* M'_H semidecides H
      iii) Can there be a TM that decides H?
3) The language H = {<*M*, *w*> : TM *M* halts on input string *w*} is not decidable.
   a) Proof

   b) This proof can be viewed as a diagonalization argument
4) If H were in D, then SD would equal D

5) Every CF language is in D.

6) D is closed under complement

7) SD is *not* closed under complement.

8) A language L is in D iff both L and its complement are in SD.

9) The language
$\neg H = \{\langle M, w\rangle$: TM M does not halt on input string $w\}$
is not in SD.

10) A language is **Turing-enumerable** iff there is a Turing machine that enumerates it.
    a) Another term that is often used is **recursively enumerable**.

11) A language is SD iff it is Turing-enumerable.

12) A language is in D iff it is lexicographically Turing-enumerable.