

Name: \_\_\_\_\_ Key \_\_\_\_\_

Grade: \_\_\_\_\_ <-- instructor use

1. A DFSM  $M$  is a 5-tuple  $(K, \Sigma, \delta, s, A)$ . What do each of the symbols represent?



$K$  **set of states**

$\Sigma$  **alphabet**

$\delta$  **transition function**

$$\delta: ( K \times \Sigma ) \rightarrow K$$

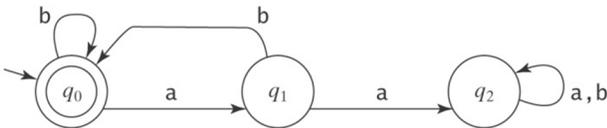
$s$  **start state (an element of  $K$ )**

$A$  **accepting states (subset of  $K$ )**

2. In the notation of problem 1, what is the initial configuration if  $M$  is to process the input string  $w$ ?

3.  $(q, w) \vdash_M (q', w')$  iff  $\delta(q, a) = q'$  [The  $\vdash_M$  symbol is read “yields in machine  $M$ ” or simply “yields”] where  $w = aw'$

4. For the following FSM, show the computation (sequence of configurations) if the input string is  $abaab$ .



$(q_0, abaab) \vdash (q_1, baab)$   
 $\vdash (q_0, aab)$   
 $\vdash (q_1, ab)$   
 $\vdash (q_2, b)$   
 $\vdash (q_2, \epsilon)$

5. What does it mean for a DFSM to “accept” a string?

**Computation on that string ends in accepting state**

6. Prove: Every DFSM  $M$ , in configuration  $(q, w)$ , halts after  $|w|$  transitions.

**Base case:** If  $w$  is  $\epsilon$ , it halts in 0 steps.

**Induction step:** Assume true for strings of length  $n$  and show for strings of length  $n+1$ .

Let  $w \in \Sigma^*$ ,  $|w| = n+1$  for some  $n \in \mathbb{N}$ .

Then  $w$  is  $ax$  for some  $a \in \Sigma$ ,  $x \in \Sigma^*$ ,  $|x| = n$ .

Let  $q'$  be  $\delta(q, a)$ . Then  $(q, w) \vdash_M (q', x)$

By induction, from configuration  $(q', x)$ ,  $M$  halts in  $n$  steps.

So, starting from the original configuration,  $M$  halts in  $n+1$  steps.

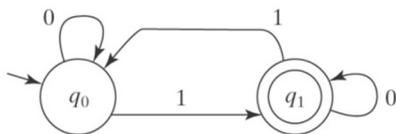
7. Is the following problem decidable? Given a DFSM  $M$  and a string  $w \in \Sigma_M^*$ , is  $w \in L(M)$ ? **Yes** No

Explain briefly. **The FSM  $M$  is a decision procedure. It always halts, and (by definition of  $L(M)$ ) gives the correct answer.**

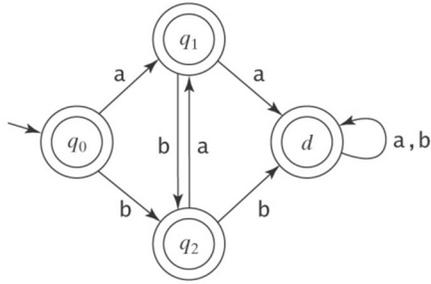
8. A language  $L$  is *regular* iff **it is  $L(M)$  for some DFSM  $M$ .**

9. Draw the transition diagram (or transition table) for a DFSM that accepts

$OddParity = \{w \in \{0, 1\}^* : w \text{ contains an odd number of 1s}\}$



10. Draw the transition diagram (or transition table) for a DFMSM that accepts  $\{w \in \{a, b\}^* : \text{no two consecutive characters are the same}\}$ .



11. In terms of the formal definitions, what is the major difference between the five components of a DFMSM and a NDFMSM?

**For a DFMSM, a "return value" of the transition function is a state.**

**For an NDFMSM, a "return value" of the transition function is a set of states.**

12. What are the two sources of nondeterminism in a NDFMSM diagram?

**An  $\epsilon$ -transition.**

**Two transitions out of the same state on the same input symbol.**

13. Tell your instructor about anything from today's session (or from the course so far) that you found confusing or still have a question about. If none, please write "None". **Must have an answer**