MA/CSSE 474 – Theory of Computation Quiz and Reading Guide – Preparation for Day 02 class

Name:\_\_\_\_\_\_ Section (circle one): 02 (9:55) 03 (10:45)

This quiz, is due at the beginning of the second day of class. Please either print it and complete it by hand, or complete it electronically and then print it. A lot of this reading material should be familiar; some of Elaine Rich's notation may be different than you have seen before; you need to understand and use her notation. This quiz is mostly about definitions and notation. **Please print 2-sided.** 

Chapter 2.

1. We consistently use the symbol Σ to denote the \_\_\_\_\_\_ from which we compose strings.

According to the textbook's definition, can  $\Sigma$  ever be infinite?

According to the textbook's definition, can a string have infinite length?

 $\Sigma^*$  is the \_\_\_\_\_ of all strings whose symbols come from  $\Sigma$ .

- 2. Let  $\Sigma$  be {a, b, c}, and let  $s \in \Sigma^*$  be abcbcc. What is the value of each of the following expressions?
  - s
  - sa
  - **s**<sup>0</sup>
  - -
  - s<sup>2</sup>
  - SR
  - $\#_b(s)$

How many different proper prefixes does s have?

How many different proper substrings does s have?

3. A (formal) *language* is a \_\_\_\_\_ of strings over an \_\_\_\_\_.

4. Are  $\emptyset$  and  $\{\varepsilon\}$  the same language? Explain briefly.

5. If the ordering of the symbols in  $\{a, b, c\}$  is the order given here, arrange the following strings into lexicographic order, according to the textbook's definition: b ba abc cac  $\epsilon$  ab

6. If  $L_1 = \{a, ba\}$  and  $L_2 = \{a, c, \epsilon\}$ , how many *different* strings are in the language  $L_1L_2$ ?

7. If L =Ø , what is L\*? \_\_\_\_\_ Explain.

8. Give an example of a language L for which  $L^+ \neq L^* - \{\epsilon\}$ . L = \_\_\_\_\_

9. Consider Exercise 2.2 On page 19. List here the letters (a, b, c, d) of the given strings that are in L<sub>1</sub>L<sub>2</sub>:\_\_\_\_\_

10. Can a language (set of strings over an alphabet) ever be uncountably infinite?

11. What are the possibilities for the cardinality of the set of all languages over a given alphabet ?

Answer:	 and

12. What is the relationship between {0}\*{1}\* and {01}\*? (circle one)

=  $\subset$   $\supset$  none of these

Good problems to think about, but not to turn in (not yet anyway, some may be assigned later):

Exercises 2.3, 2.5a, 2.7abde, 2.8