

473: Instructor Notes from Day 10 slides:

Slide 4: Where are we now?

Do the test for k randomly-generated values of $a < N$.

Probability of error is $< (1/2)^k$

If $k=100$, dasGupta says the probability of error is less than the probability of a cosmic ray flipping some bits and messing up your computer's computation

Slide 6: The algorithm (modified)

Note that this algorithm may produce a "false prime", but the probability is very low.

Slide 7: Miller-Rabin test

u is odd?

Or should I say " u are odd". To most of the world outside Rose-Hulman, if you would take this course or any 400-level MA/CSSE course, u must be odd!

Note that this factorization of $N-1$ can be fast. Just count how many bits at the end of $N-1$ are 0 to get t , and then bit-shift $N-1$ to get u .

ON BOARD: Note that $a^{N-1} = a^{u(2^t)} = (\dots (a^u)^2 \dots)^2$ square t times

Slide 11: Example (first Carmichael number)

Work through another example with the students. $N = 105$.

Suppose we first try $a = 8$. (Use the modexp interactive program).

Enter 8, 104, 105: Get 1. So it passes the Fermat test.

What is u ? (13). Do $8^{13} (8)$, $8^{26} (64)$, $8^{52} (1)$

Then $29^{104} = 1$. $29^{13} = 29$, $29^{26} = 1$