

## Notes on Day 2 slides:

Slide 10: Analysis of the recursive algorithm

Where does the 3 come from? Two comparisons plus a sum.

Conclusion:  $T(N) \geq F(N)$  Q4

$$F(N) = \frac{1}{\sqrt{5}} \left( \left( \frac{1 + \sqrt{5}}{2} \right)^N - \left( \frac{1 - \sqrt{5}}{2} \right)^N \right)$$

$(1 + \sqrt{5})/2 \approx 1.618$ , so it is exponential.  $1.618^N = 2^{(0.694 * N)}$

How long would it take to compute  $F(200)$ ?  $T(200) \geq F(200) \geq 2^{138}$ .

Last question  $2^{(138-18)} = 2^{120}$  seconds.

How many seconds in a year? (less than  $2^{22}$ ).

So time for  $F(200)$  is at least  $2^{98}$  years!

**What is this document?** I have simply copied the instructor notes from the slides that have them, and pasted them in here.

These are some of the things I would say and/or write on the board during class time

Slide 11: A Polynomial-time algorithm

This algorithm is clearly linear.

Or is it?

Addition is NOT a constant-time operation unless there is a limit on the size of the numbers involved.

Slide 12: A more efficient Algorithm

The file **fib3.py** has the solution, and **fib3-incomplete.py** has it partially completed.

Solution for matrix\_power:

```
def matrix_power(m, n):
    result = identity_matrix
    power = x
    while n > 0:
        if n % 2 == 1:
            result = matrix_multiply(result, power)
        power = matrix_multiply(power, power)
    # print "In loop:", n, power, result
    n = n / 2
    return result
```

Slide 12: Why so complicated?

Because we'd have to use decimal approximation of the square roots, and that would be very messy. More so than the matrix version.

Slide 17: Multiplication: The running time of the algorithm is  $O(n^2)$