## 473 HW1

- 1.
- 11. Locker doors There are n lockers in a hallway, numbered sequentially from 1 to n. Initially all the locker doors are closed. You make n passes by the lockers, each time starting with locker #1. On the ith pass,  $i = 1, 2, \ldots, n$ , you toggle the door of every ith locker: if the door is closed, you open it; if it is open, you close it. For example, after the first pass every door is open; on the second pass you only toggle the even-numbered lockers (#2, #4, ...) so that after the second pass the even doors are closed and the odd ones are open; the third time through, you close the door of locker #3 (opened from the first pass), open the door of locker #6 (closed from the second pass), and so on. After the last pass, which locker doors are open and which are closed? How many of them are open?

2.

1.3.9

4.

1.4.4

5

1.4.5

1, 4,10

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- 2. New World puzzle There are four people who want to cross a bridge; they all begin on the same side. You have 17 minutes to get them all across to the other side. It is night, and they have one flashlight. A maximum of two people can cross the bridge at one time. Any party that crosses, either one or two people, must have the flashlight with them. The flashlight must be walked back and forth; it cannot be thrown, for example. Person 1 takes 1 minute to cross the bridge, person 2 takes 2 minutes, person 3 takes 5 minutes, and person 4 takes 10 minutes. A pair must walk together at the rate of the slower person's pace. For example, if person 1 and person 4 walk across first, 10 minutes have elapsed when they get to the other side of the bridge. If person 4 returns the flashlight, a total of 20 minutes have passed and you have failed the mission. (Note: According to a rumor on the Internet, interviewers at a well-known software company located near Seattle have given this problem to interviewees.)
- 9. Design an algorithm for the following problem: Given a set of n points in the Cartesian plane, determine whether all of them lie on the same circumference.
  - **4. a.** Let A be the adjacency matrix of an undirected graph. Explain what property of the matrix indicates that
    - i. the graph is complete.
    - ii. the graph has a loop, i.e., an edge connecting a vertex to itself.
    - iii. the graph has an isolated vertex, i.e., a vertex with no edges incident to it.
    - **b.** Answer the same questions for the adjacency list representation.
- 5. Give a detailed description of an algorithm for transforming a free tree into a tree rooted at a given vertex of the free tree.

10. Anagram checking Design an algorithm for checking whether two given words are anagrams, i.e., whether one word can be obtained by permuting the letters of the other. (For example, the words tea and eat are anagrams.)