#### **CSSE463: Image Recognition**

Day 31

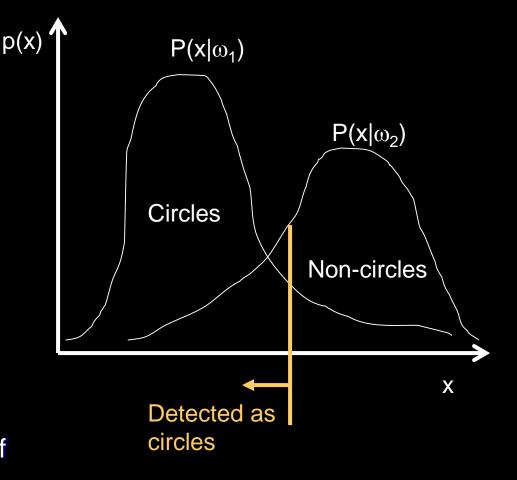
- Today: Bayesian classifiers
- Tomorrow: project meetings.
- Questions?

# Exam 3 Thursday

- Closed book, notes, computer
  - BUT you may bring notes (index card or 1-side of paper)
  - You may also want a calculator.
- Pdf of review questions ?
- Not cumulative: focus is k-means and later.
- More hints tomorrow?

# **Bayesian classifiers**

- Use training data
  - Assume that you know P probabilities of each feature.
- If 2 classes:
  - Classes  $\omega_1$  and  $\omega_2$
  - Say, circles vs. non-circles
  - A single feature, x
  - Both classes equally likely
  - Both types of errors equally bad
- Where should we set the threshold between classes?
  Here?
- Where in graph are 2 types of errors?

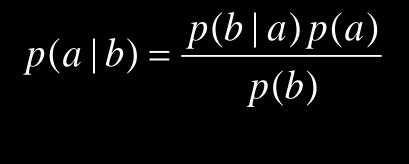


#### What if we have prior information?

 Bayesian probabilities say that if we only expect 10% of the objects to be circles, that should affect our classification

# Bayesian classifier in general

- Bayes rule:
  - Verify with example
- For classifiers:
  - x = feature(s)
  - $\omega_i = class$
  - $P(\omega|x) = posterior probability$
  - P(ω) = prior
  - P(x) = unconditional probability
  - Find best class by maximum a posteriori (MAP) priniciple. Find class i that maximizes P(ω<sub>i</sub>|x).
    Denominator doesn't affect calculations
  - Example:
    - indoor/outdoor classification



Learned from examples (histogram)

 $p(\omega_i \mid x) =$ 

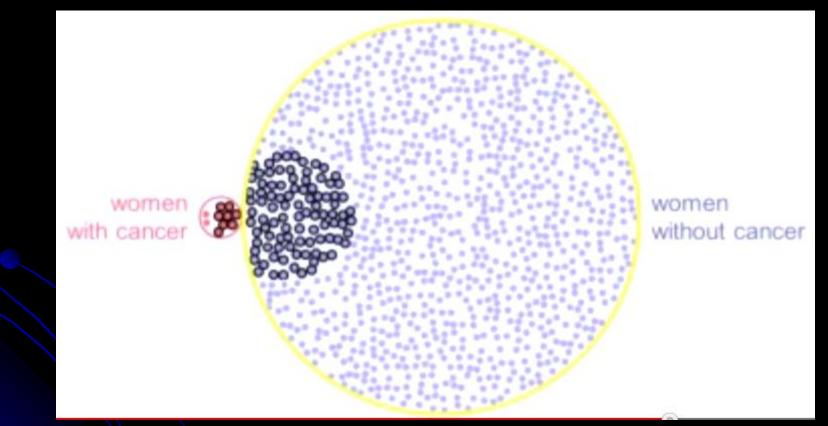
Learned from training set (or leave out if unknown)

 $p(x \mid \omega p(\omega_i))$ 

p(x)

Fixed

#### Bayes rule is used in prediction of disease



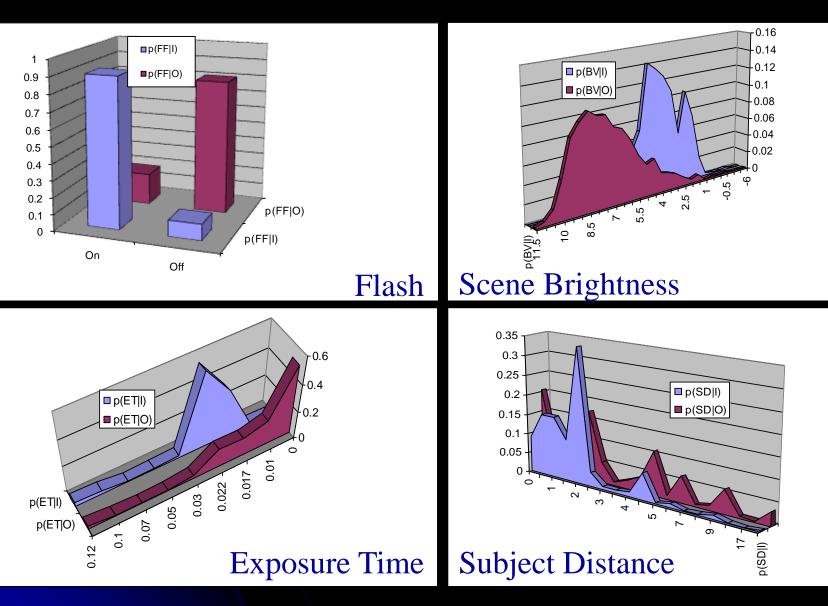
http://www.youtube.com/watch?v=D8VZqxcu0I0

Can you verify the approximation they found?

# Indoor vs. outdoor classification

- I can use low-level image info (color, texture, etc)
- But there's another source of really helpful info!

## **Camera Metadata Distributions**



# Why we need Bayes Rule

#### **Problem:**

We know conditional probabilities like P(flash was on | indoor)

We want to find conditional probabilities like P(indoor | flash was on, exp time = 0.017, sd=8 ft, SVM output)

Let  $\omega$  = class of image, and x = all the evidence. More generally, we know P( x |  $\omega$  ) from the training set (why?) But we want P( $\omega$  | x)

$$p(\omega_i \mid x) = \frac{p(x \mid \omega_i) p(\omega_i)}{p(x)}$$

Using Bayes Rule  $P(\omega|x) = P(x|\omega)P(\omega)/P(x)$ The denominator is constant for an image, so  $P(\omega|x) = \alpha P(x|\omega)P(\omega)$  Using Bayes Rule  $P(\omega|x) = P(x|\omega)P(\omega)/P(x)$ The denominator is constant for an image, so  $P(\omega|x) = \alpha P(x|\omega)P(\omega)$ 

We have two types of features, from image metadata (M) and from low-level features, like color (L)
 Conditional independence means P(x|ω) = P(M|ω)P(L|ω)

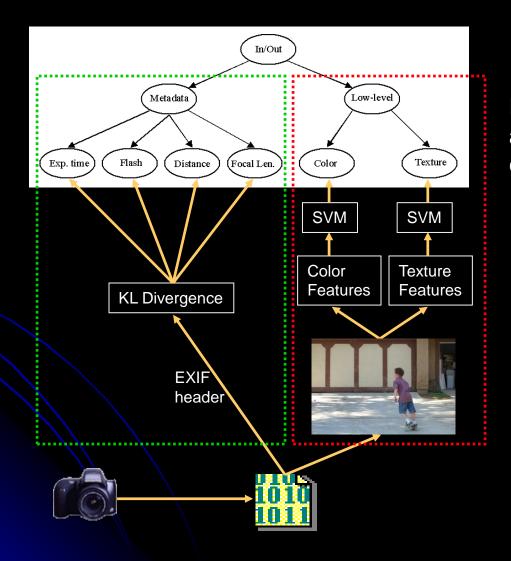
# $P(\omega|X) = \alpha P(M|\omega) P(L|\omega) P(\omega)$

From histograms From SVM (initial bias)

## **Bayesian network**

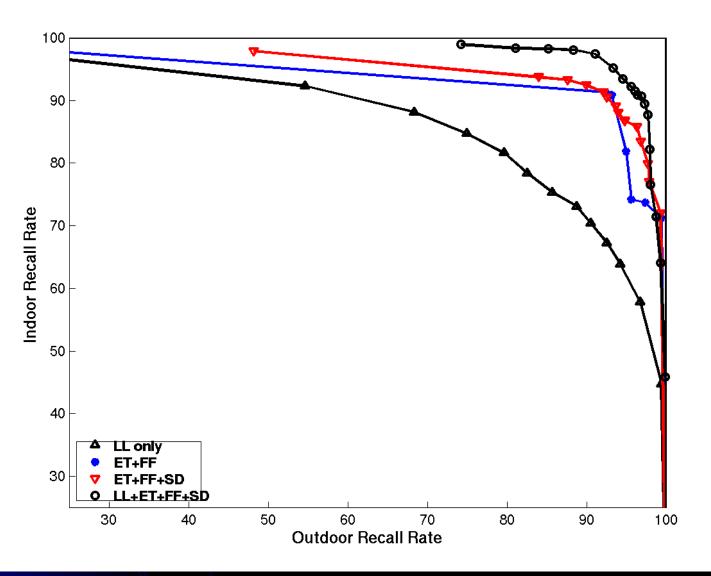
- Efficient way to encode conditional probability distributions and calculate marginals
- Use for classification by having the classification node at the root
  - Examples
    - Indoor-outdoor classification
    - Automatic image orientation detection

# Indoor vs. outdoor classification



Each edge in the graph has an associated matrix of conditional probabilities

## Effects of Image Capture Context



Recall for a class C is fraction of C classified correctly

# **Orientation detection**

- See IEEE TPAMI paper
  - Hardcopy or posted
- Also uses single-feature Bayesian classifier (answer to #1-4)
- Keys:
  - 4-class problem (North, South, East, West)
  - Priors really helped here!

 You should be able to understand the two papers (both posted)