CSSE 304 Day 11

- 1. Question from the previous class: Another procedures that can be shorter if written using list-recur. Instructor's example.
- 2. Question from the previous class: Which of the 5 procedures that we wrote using list-recur is a bad idea to write that way? Why?
- 3. Consider the following Scheme transcript (from which I have removed part of the definition) Fill in the missing part. You might want to try it in Scheme to see if your code works.

Recall: Grammar for lambda-calculus expresions:

```
 \begin{array}{lll} <& LcExpr> ::= & <& identifier> | & variable use \\ & ( & lambda ( <& identifier> ) <& LcExpr> ) | & abstraction \\ & ( & <& LcExpr> <& LcExpr> ) & application \\ \end{array}
```

4. Use this grammar to derive ((lambda (x) (x y)) z)

Variable x occurs free in the LcExp e iff one of the following is true:

F1. e is a variable, and e is the same as x.

- **F2.** e is an abstraction (λ (y) e'), where y is different from x and x occurs free in e'.
- **F3.** e is an application (e₁ e₂), where x occurs free in e₁ or in e₂. Variable x occurs bound in the LcExp e iff one of the following is true:
 - **B1.** e is an abstraction (λ (y) e'), where x occurs bound in e', or x and y are the same variable and x occurs free in e'.
 - **B2.** e is an application (e₁ e₂) where x occurs bound in e₁ or in e₂.
- 5. Free and bound occurrences of variables. Formal definitions of occurs free and occurs bound (in box above)
- 6. **Examples:**In each of the following expressions, does *x* occur free and/or occur bound?
 - X
 - t
 - (x t)
 - (lambda (x) (x t))
 - ((lambda (x) x) x)
 - (lambda (x) (lambda (t) (t x)))

Follow the grammar. **occurs-free?** is defined in EoPL

(define (occurs-bound? sym exp)

- 7. The **lexical depth** of a bound occurrence of a variable is the number of levels of nested lambdas and lets between this occurrence and the variable's definition. In (lambda (x) (lambda (y) (x y))), the occurrence of y has depth 0 and the occurrence of x has depth 1.
- 8. The **lexical address** of a bound occurrence of a variable is a pair (d p), where d is that occurrence's lexical depth, and p is the variable's position within its "declaration list". The lexical address of a free variable includes the variable's name and an indication that it is free.
- 9. Example:

```
In (lambda (x z)
(lambda (y)
((x y) z)))
```

The occurrence of x has depth 1 and position 0.

The occurrence of y has depth 0 and position 0.

The occurrence of z has depth 1 and position 1.

10. Example of output from the lexical-address procedure that you will write:

11. **Exercise:** What is the output from:

Note: We are only looking at syntactic properties now.

Don't worry about whether this code has a useful meaning in Scheme.