

## CSSE 230 Day 6

### Intro to Trees

After today, you should be able to...  
...use tree terminology  
...write recursive tree functions

Checkout [BinarySearchTree](#) from SVN

## Announcements

- ▶ Review Day 5's quizzes on Java Collections and Data Structures
- ▶ Preview of HW3: includes an essay

## Observation about Stacks and Queues Infix → Postfix problem

- ▶ It must be  $O(n)$ , so you can't grow your strings character-by-character:
  - Strings are immutable, so characters must be copied. `s += "*"`  is as slow growing an array using the `+` scheme
- ▶ Solution? Use a `StringBuilder`!
  - They have internal capacity, which doubles when full!
- ▶ See the example at the end of Warmup and Stretching's `ShapeText.java` for an example.

## Exam 1

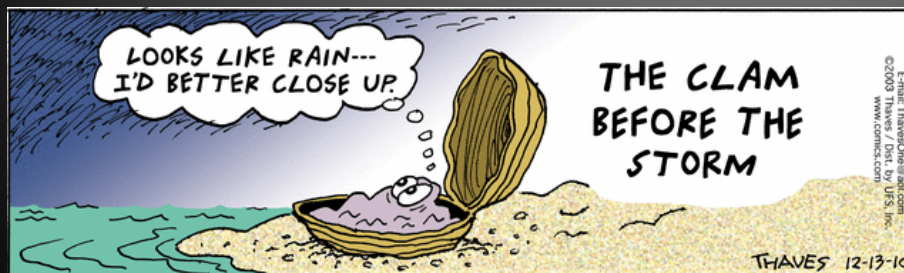
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- ▶ Exam 1 – Day 8: 7–9 pm
  - Coverage:
    - Everything from reading and lectures, Sessions 1–7
    - Programs: Warmup, Stacks and Queues
    - Homeworks 1–2
  - Allowed resources:
    - Written part:  $\frac{1}{2}$  of one side of 8.5 x 11 paper
      - Goal: to let you use formulas but force you to summarize.
    - Programming part:
      - Textbook
      - Eclipse (including programs you wrote in your repos)
      - Course web pages and materials on Moodle
      - Java API documentation
    - Two previous 230 Exam 1's are available in Moodle

## Exam 1 Possible Topics

- Written (50–70%):
  - Growable Arrays
  - MCSS
  - big  $O/\theta/\Omega$ : true/false, using definitions, limits, code analysis
  - Binary search
  - ADT/Collections
  - Choosing an ADT to solve a given problem
- Programming (30–50%):
  - Implementing an ADT using an array, nodes, or another ADT
  - Writing an efficient algorithm to solve a simple array-based problem

## Questions?



## Next:

- ▶ an implementation that offers interesting benefits, but is more complex to code than arrays or lists...
- ▶ ... Trees!

# Trees

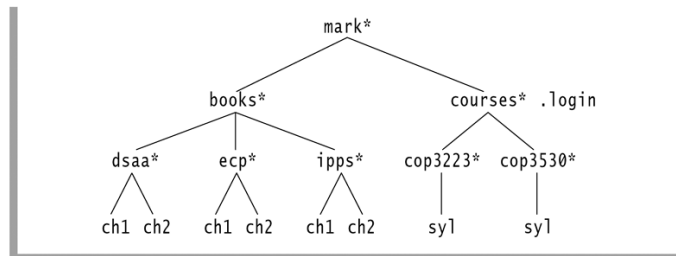
Introduction and terminology  
for three types



## Trees in everyday life

- ▶ Class hierarchy tree (single inheritance only)
- ▶ Directory tree in a file system

**figure 18.4**  
A Unix directory



## Traverse a Directory Tree

```

import java.io.File;

public class TraverseFiles {

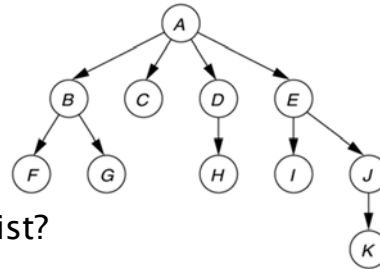
    public static void main(String... args) {
        File[] files =
            new File("C:/EclipseWorkspaces/csse230-2014/BST2").listFiles();
        showFiles(files, 0);
    }

    public static void showFiles(File[] files, int indent) {
        for (File file : files) {
            if (file.isDirectory()) {
                System.out.println("        " + file.getName() +
                    ".substring(0,indent) +
                    "Directory: " + file.getName());
                showFiles(file.listFiles(), indent+1); // Calls method again.
            } else {
                System.out.println("        " + file.getName() +
                    ".substring(0,indent) +
                    "File: " + file.getName());
            }
        }
    }
}

```

## A General Tree—Global View

- ▶ A collection of **nodes**
- ▶ Nodes are connected by **directed edges**.
  - One special **root node** has no incoming edges
  - All other nodes have exactly one incoming edge
- ▶ One way that Computer Scientists are odd is that our trees usually have their root at the top!

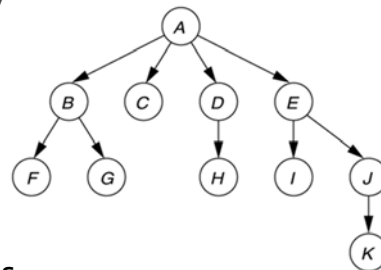


- ▶ How are trees like a linked list?
- ▶ How are they different?

## Tree Terminology

Q1, 2

- ▶ Parent
- ▶ Child
- ▶ Grandparent
- ▶ Sibling
- ▶ Ancestors and descendants
- ▶ Proper ancestors, proper descendants
- ▶ Subtree
- ▶ Leaf, interior node
- ▶ Depth and height of a node
- ▶ Height of a tree

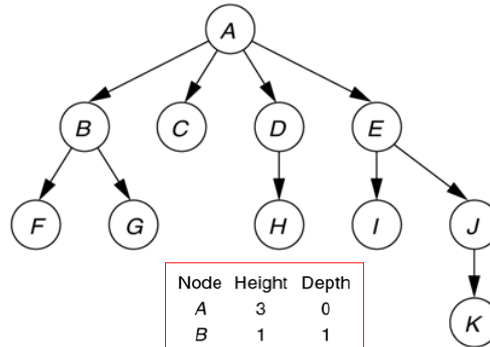


Q3-6

## Node height and depth examples

**figure 18.1**

A tree, with height and depth information



Node	Height	Depth
A	3	0
B	1	1
C	0	1
D	1	1
E	2	1
F	0	2
G	0	2
H	0	2
I	0	2
J	1	2
K	0	3

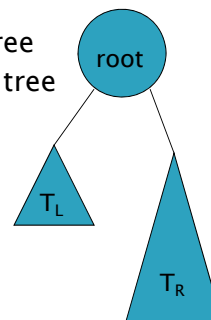
The height of a tree is the height of its root node.

Which is larger, the sum of the heights or the sum of the depths of all nodes in a tree?

## Binary Tree: Recursive definition

- ▶ A **Binary Tree** is either
  - **empty**, or
  - **consists** of:
    - a distinguished node called the root, which contains an element, and
    - A left subtree  $T_L$ , which is a binary tree
    - A right subtree  $T_R$ , which is a binary tree

- ▶ **Binary trees** contain at most 2 children



Q7-9

## Binary Search Trees (BST)

- ▶ Q: What property enables us to search BSTs efficiently?
- ▶ A: Every element in the left subtree is smaller than the root, and every element in the right subtree is larger than the root. And this is true at **every node**, not just the root.

## Connections with Linked Lists

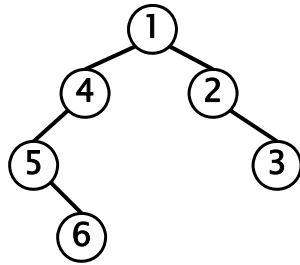
- ▶ Write `size()` for linked list
  - Non-recursively
  - Recursively
- ▶ Write `size()` for a tree
  - Recursively
  - Non-recursively (later)



## Growing Trees

- ▶ Let's start the BinarySearchTrees assignment: implement a `BinaryTree<T>` class

Test tree:



A single tiny recursive method for size will touch **every node in the tree**. Let's write, then watch in debugger.