

After today, you should be able to... ...use tree terminology ...write recursive tree functions

Checkout BinarySearchTree from SVN

Announcements

 Review yesterday's quizzes on Java Collections and Data Structures

Pay careful attention to the ACM Code of Ethics essay

- Part of Homework 3
 - Examine the Code of Ethics of the ACM
 - Focus on property rights
 - Write a reaction (1 page single-spaced)
 - Details are in the assignment
- Context for writing efficient code
 - Correct and maintainable, does it need to be fast?
 - Other constraints like space
 - Completing your work ethically
 - Be a team player (next)





Next:

• an implementation that offers interesting benefits, but is more complex to code than arrays...

... Trees!

Trees

Introduction and terminology for three types



Trees in everyday life

Class hierarchy tree (single inheritance only)
Directory tree in a file system



A General Tree—Global View

- A collection of nodes
- Nodes are connected by directed edges.
 - One special root node has no incoming edges
 - All other nodes have exactly one incoming edge
- One way that Computer Scientists are odd is that our trees usually have their root at the top!



- How are trees like a linked list?
- How are they different?

Tree Terminology

- Parent
- Child
- Grandparent
- Sibling
- Ancestors and descendants
- Proper ancestors, proper descendants
- Subtree
- Leaf, interior node
- Depth and height of a node
- Height of a tree



Node height and depth examples

figure 18.1

A tree, with height and depth information

The height of a tree is the height of its root node.

Which is larger, the sum of the heights or the sum of the depths of all nodes in a tree?

B F	G	c			E	Ŀ
		Node	Height	Depth		¥
		Α	3	0		
		В	1	1		(\mathbf{k})
		С	0	1		
		D	1	1		
		E	2	1		
\f		F	0	2		
		G	0	2		
the		H	0	2		
·ee?		,	0	2		
		J	1	2		
		ĸ	0	3		

Binary Tree: Recursive definition

A Binary Tree is either

- **empty**, or
- consists of:
 - a distinguished node called the root, which contains an element, and
 - A left subtree T_L, which is a binary tree
 - A right subtree T_R, which is a binary tree
- Binary trees contain at most 2 children



Binary Search Trees (BST)

- Q: What property enables us to search BSTs efficiently?
- A: Every element in the left subtree is smaller than the root, and every element in the right subtree is larger than the root. And this is true at every node, not just the root.

Connections with Linked Lists

Write size() for linked list

- Non-recursively
- Recursively
- Write size() for a tree
 - Recursively
 - Non-recursively (later)

Growing Trees

Let's start the BinarySearchTrees assignment: implement a BinaryTree<T> class

Test tree:



A single tiny recursive method for size will touch every node in the tree. Let's write, then watch in debugger.