

After today, you should be able to... ...use tree terminology ...write recursive tree functions

Checkout BinarySearchTree from SVN

#### Pay careful attention to the ACM Code of Ethics essay

- Part of Homework 3
  - Examine the Code of Ethics of the ACM
    - Focus on property rights
  - Write a reaction (1 page single-spaced)
  - Details are in the assignment
- Context for writing efficient code
  - Correct and maintainable, does it need to be fast?
  - Other constraints like space
  - Completing your work ethically
  - Be a team player (next)

## Thoughts on Teaming

## Two Key Rules

- No prima donnas
  - Working way ahead, finishing on your own, or changing the team's work without discussion:
    - harms the education of your teammates
- No laggards
  - Coasting by on your team's work:
    - harms your education
- Both extremes
  - are selfish
  - may result in a failing grade for you on the project

## **Grading of Team Projects**

- I'll assign an overall grade to the project
- Grades of individuals will be adjusted up or down based on team members' assessments
- At the end of the project each of you will:
  - Rate each member of the team, including yourself
  - Write a short Performance Evaluation of each team member with evidence that backs up the rating
    - Positives
    - Key negatives

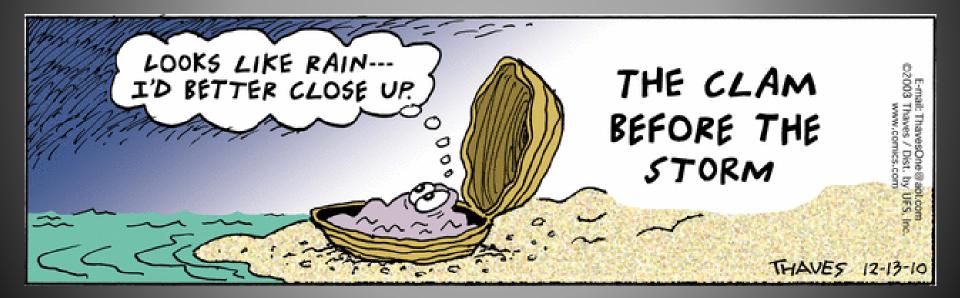
## Ratings

- Excellent—Consistently went above and beyond: tutored teammates, carried more than his/her fair share of the load
- Very good—Consistently did what he/she was supposed to do, very well prepared and cooperative
- Satisfactory—Usually did what he/she was supposed to do, acceptably prepared and cooperative
- Ordinary—Often did what he/she was supposed to do, minimally prepared and cooperative
- Marginal—Sometimes failed to show up or complete tasks, rarely prepared

**Deficient**—Often failed to show up or complete tasks, rarely prepared

- Unsatisfactory—Consistently failed to show up or complete tasks, unprepared
- Superficial—Practically no participation
- No show—No participation at all





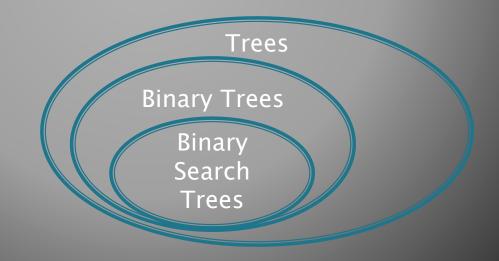
#### Next:

• an implementation that offers interesting benefits, but is more complex to code than arrays...

... Trees!

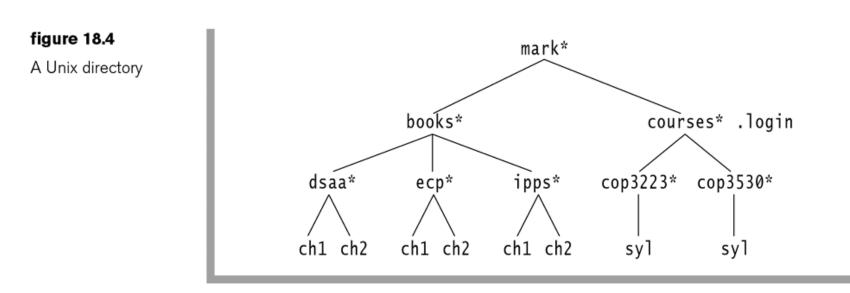
#### Trees

# Introduction and terminology for three types



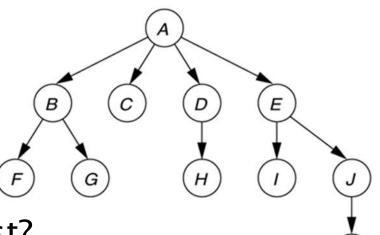
### Trees in everyday life

Class hierarchy tree (single inheritance only)
Directory tree in a file system



## A General Tree—Global View

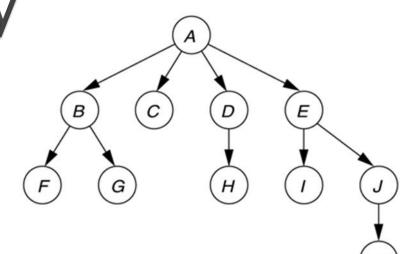
- A collection of nodes
- Nodes are connected by directed edges.
  - One special root node has no incoming edges
  - All other nodes have exactly one incoming edge
- One way that Computer Scientists are odd is that our trees usually have their root at the top!



- How are trees like a linked list?
- How are they different?

## Tree Terminology

- Parent
- Child
- Grandparent
- Sibling
- Ancestors and descendants
- Proper ancestors, proper descendants
- Subtree
- Leaf, interior node
- Depth and height of a node
- Height of a tree



#### Node height and depth examples

#### figure 18.1

A tree, with height and depth information

The height of a tree is the height of its root node.

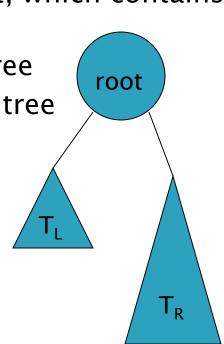
Which is larger, the sum of the heights or the sum of the depths of all nodes in a tree?

B F	G	c			E	Ŀ
		Node	Height	Depth		. ↓
		Α	3	0		$(\mathbf{r})$
		В	1	1		$(\kappa)$
		С	0	1		
		D	1	1		
		E	2	1		
of		F	0	2		
		G H	0 0	2		
the		п 1	0	2 2		
ree?		, J	1	2		
		к	0	3		

#### Binary Tree: Recursive definition

#### A Binary Tree is either

- **empty**, or
- consists of:
  - a distinguished node called the root, which contains an element, and
  - A left subtree T<sub>L</sub>, which is a binary tree
  - A right subtree T<sub>R</sub>, which is a binary tree
- Binary trees contain at most 2 children



## Binary Search Trees (BST)

- Q: What property enables us to search BSTs efficiently?
- A: Every element in the left subtree is smaller than the root, and every element in the right subtree is larger than the root. And this is true at every node, not just the root.

## **Connections with Linked Lists**

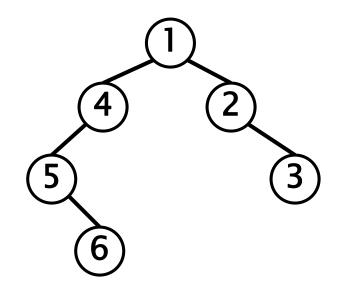
#### Write size() for linked list

- Non-recursively
- Recursively
- Write size() for a tree
  - Recursively
  - Non-recursively (later)

### **Growing Trees**

Let's start the BinarySearchTrees assignment: implement a BinaryTree<T> class

Test tree:



A single tiny recursive method for size will touch every node in the tree. Let's write, then watch in debugger.