

CSSE 230 Day 19

Tree Variations:
EBTs & Tries

Reminders/Announcements

- ▶ Use the new Eclipse project for EditorTrees Milestone 2.
- ▶ **Milestone 2 grading:** You must pass *all* Milestone 1 tests in order to get any credit for Milestone 2.
- ▶ **Exam 2:** Tuesday May 8, 7:00 PM
- ▶ **Final Exam:** Tuesday May 22: 8:00 AM
- ▶ Scrabble project team preference survey: by Wednesday 5 PM
- ▶ **Consider applying to be a CSSE TA for the Fall term** (look for an email in the next week or two)
 - In the fall, we mainly hire work-study or work-opportunity students.
- ▶ **Reminder:** EditorTrees Milestone 2 is much more complex than Milestone 1.
 - If your team is not yet debugging "delete", you probably need to pick up the pace a bit.

What questions do you have?

Editor Trees
Anything else

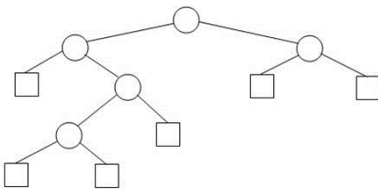
Agenda

- ▶ Extended Binary Trees (EBT), including a proof by induction.
- ▶ Digital search trees (tries)
- ▶ Directed Acyclic Graphs (DAG)
- ▶ EditorTrees work time

Tree Variations

- » Extended Binary trees
- Digital Search Trees
- Directed Acyclic Graphs

Extended Binary Tree (EBT) is just a different way to view binary trees: *null* external nodes as leaves 1-2



The diagram illustrates an Extended Binary Tree (EBT). It consists of a root internal node (circle) with two children. The left child is an internal node (circle) with two children: a left external node (square) and a right internal node (circle). This right internal node has two children: a left internal node (circle) and a right external node (square). The left internal node has two children: a left external node (square) and a right external node (square). The right child of the root is an internal node (circle) with two children: a left external node (square) and a right external node (square).

- ▶ An **Extended Binary Tree** is either
 - an **external node**, or
 - an (**internal**) root node and two EBTs T_L and T_R .
- ▶ We draw internal nodes as circles and external nodes as squares
 - Generic picture and detailed picture
- ▶ EBT: An alternative way of viewing binary trees, in which the external nodes represent different “places” where an unsuccessful search can end or an element can be inserted
- ▶ Internal nodes are used (later) in calculating average time for successful search
- ▶ External nodes in calculating average time for unsuccessful search.

3-10

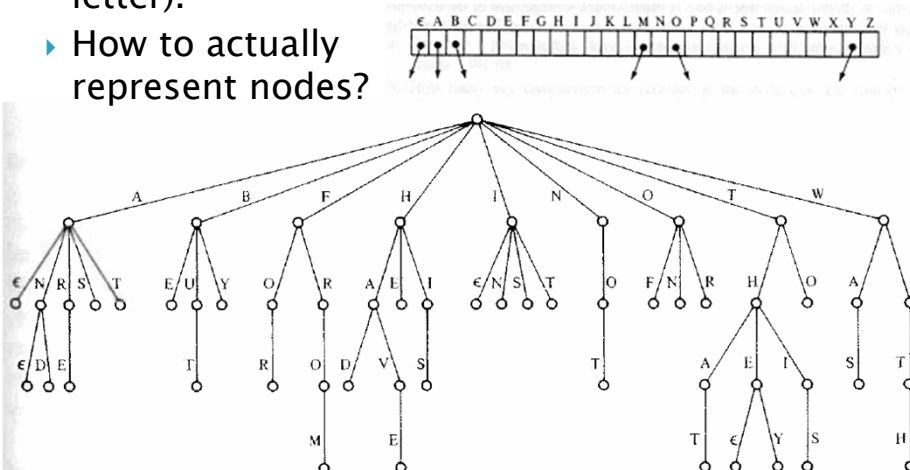
A property of EBTs

- ▶ **Property** P(N): For any $N \geq 0$, any EBT with N internal nodes has _____ external nodes.
- ▶ **Proof by strong induction**, based on the recursive definition.
 - A notation for this problem: $IN(T)$, $EN(T)$
 - Note that, like a lot of other simple examples, this one can be done without induction.
 - But one purpose of this exercise is practice with strong induction, especially on binary trees.
- ▶ What is the crux of any induction proof?
 - Finding a way to relate the properties for larger values (in this case larger trees) to the property for smaller values (smaller trees). **Do the proof now.**

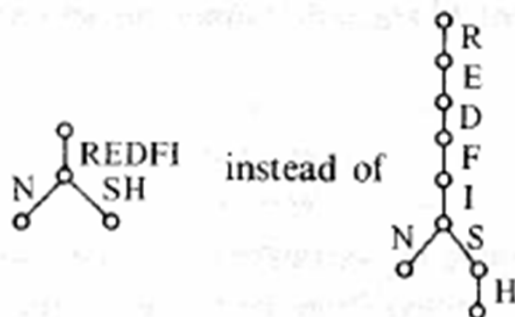
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Another approach to search trees

- ▶ Digital search tree (trie).
- ▶ We store the data digit-by-digit (or letter by letter).
- ▶ How to actually represent nodes?

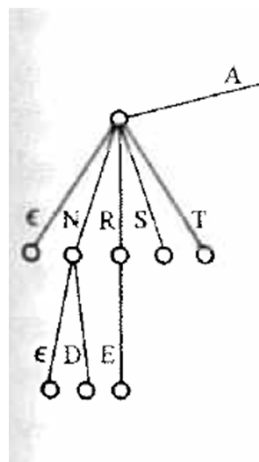


We can collapse single-branch paths to save space

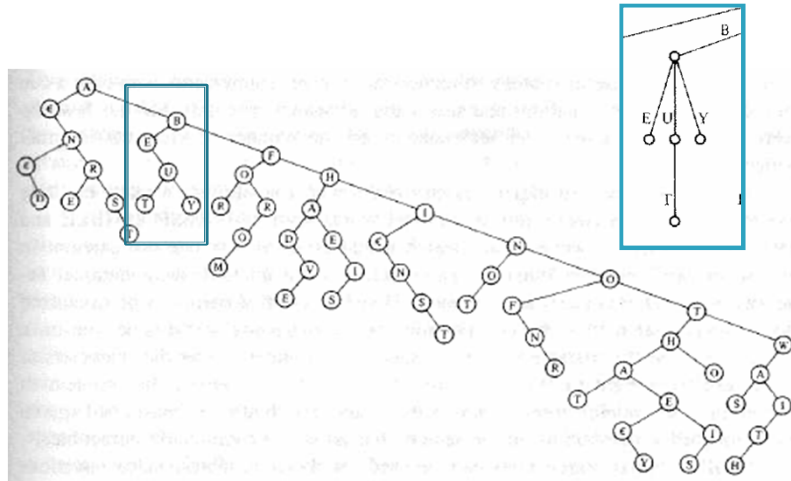


We can share a single static "ε-node" to save space

- ▶ The epsilon nodes aren't null; they just show the end of a word.
- ▶ There can still be null pointers at each level where there are missing letters



Representing a Trie as a binary tree saves even more space



For many more details on Tries, see <http://en.wikipedia.org/wiki/Trie>

You can try to create an interesting trie using this applet

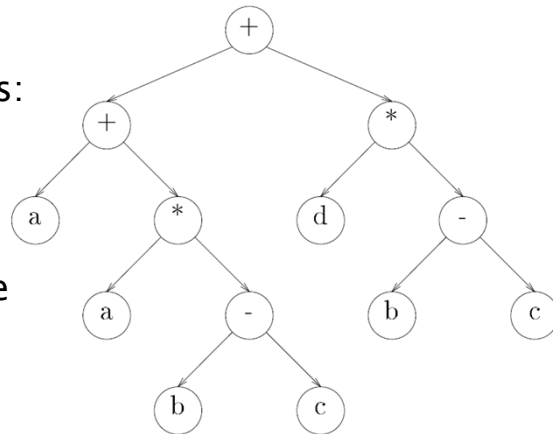
- ▶ <http://blog.ivank.net/trie-in-as3.html>

Expression Tree Variation

- ▶ Consider a tree that represents this expression: $a + a * (b - c) + (b - c) * d$

- ▶ Notice the common sub-expressions: a and $(b - c)$

- ▶ The value of each of those only needs to be computed once



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Directed Acyclic Graph (DAG)

- ▶ A useful representation for common sub-expressions: $a + a * (b - c) + (b - c) * d$

- ▶ A DAG is like a tree with sharing
 - Directed graph
 - No cycles
 - A distinguished root
 - Looks like a tree when doing a traversal, but saves space.

