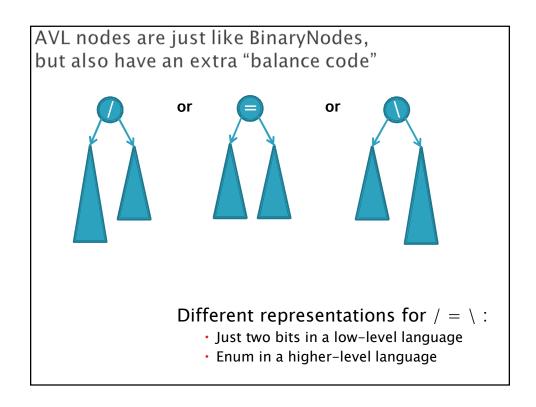
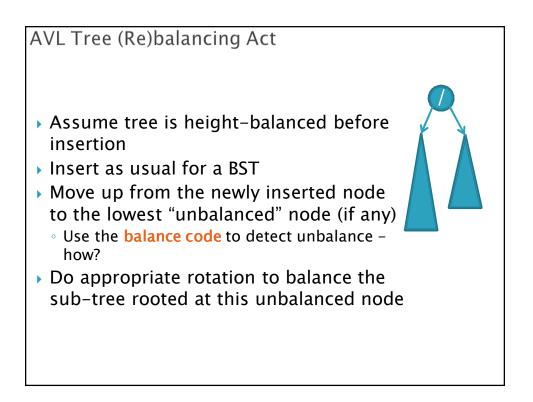
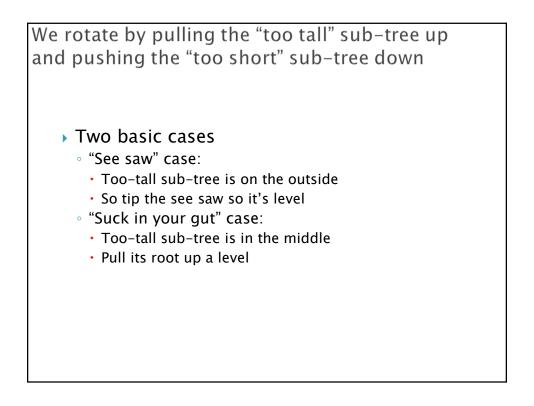


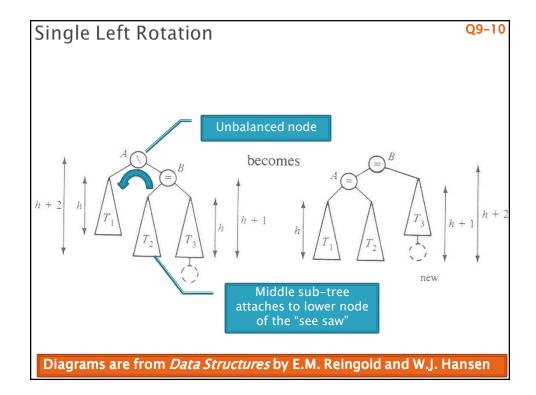
Summary of last class (plus a little more: Sec 02)

- The height of the tallest height-balanced tree with N nodes is O(log n).
- Specifically, max. height of an AVL tree with N nodes is: H < 1.44 log (N+2) - 1.328
 - Note: This formula is NOT the way to do problem 4 on WA5. Use the Fibonacci tree idea from yesterday.
- Thus insert, delete, and find are all O(log n).
- An AVL tree is a height-balanced BST that maintains its balance by using various "rotations".
- Named for authors of original paper, Adelson-Velskii and Landis (1962).
- Remaining question: How can we rebalance after an insertion or deletion (in log n time)?

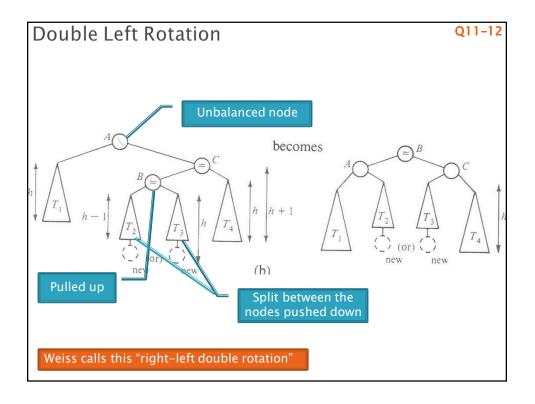


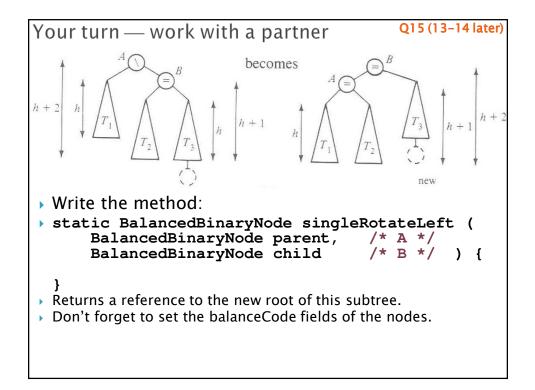


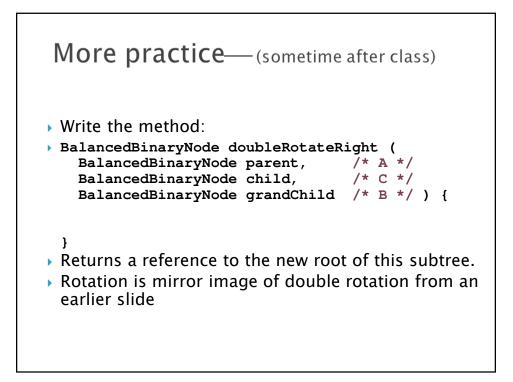




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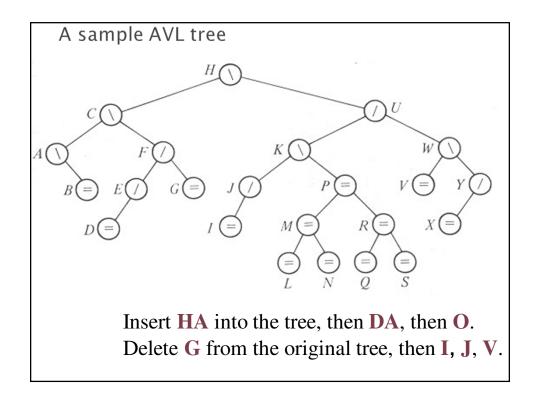


D(log N)?	Q13-14, 16-17	Submit Quiz 13
Both kinds of rotation le as before the insertion!	ave height tl	ne same
Is insertion plus rotation	n cost really (O(log N)?
Insertion/deletion	0	(log n)
in AVL Tree:		(log n) (log n)
· ·	any): O	(log n) (log n) (1)
in AVL Tree: Find the imbalance point (if a	any): O(O((log n)

Which kind of rotation to do after an insertion?

Depends on the first two links in the path from the lowest node that has the imbalance (A) down to the newly-inserted node.

First link (down from A)	Second link (down from A's child)	Rotation type (rotate "around A's position")
Left	Left	Single right
Left	Right	Double right
Right	Right	Single left
Right	Left	Double left



1 - 4



- Add elements in the following order; do the appropriate rotations when needed.
 1 2 3 4 5 6 11 13 12 10 9 8 7
- How should we rebalance if each of the following sequences is deleted from the above tree?
 - · (10 9 7 8) (13) (1 5)
 - For each of the three sequences, start with the original 13-element tree. E.g. when deleting 13, assume 10 9 8 7 are still in the tree.

Work with your Doublets partner. When you finish, work on Doublets or Threaded. Or write the rotateDoubleRight code from a previous slide