

CSSE 220

Recursion

Checkout *InClassRecursion* project from SVN

Recursion

- A solution technique where the same computation **occurs repeatedly** as the problem is solved

recurs

- Examples:
 - Sierpinski's Triangle
 - Towers of Hanoi:
<http://www.mathsisfun.com/games/towerofhanoi.html>
or search for Towers of Hanoi

An example – Triangle Numbers

- If each red block has area 1, what is the *area A(n)* of the Triangle whose *width* is n?

– Answer:

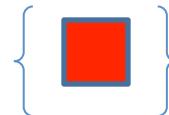
$$A(n) = n + A(n-1)$$

- The above holds for which n ? What is the answer for other n ?

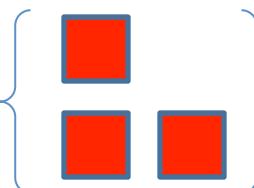
– Answer: The recursive equation holds for $n \geq 1$.

For $n = 0$, the area is 0.

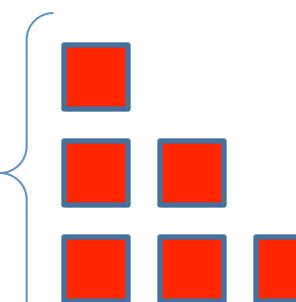
Triangle with width 1



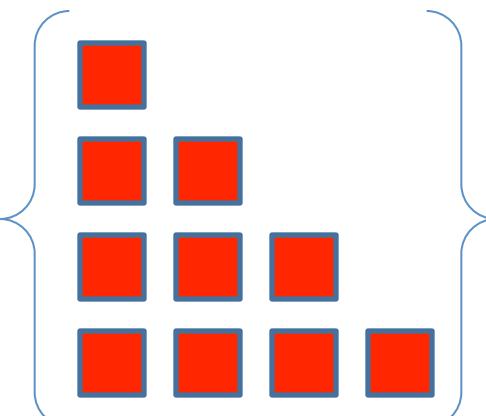
Triangle with width 2



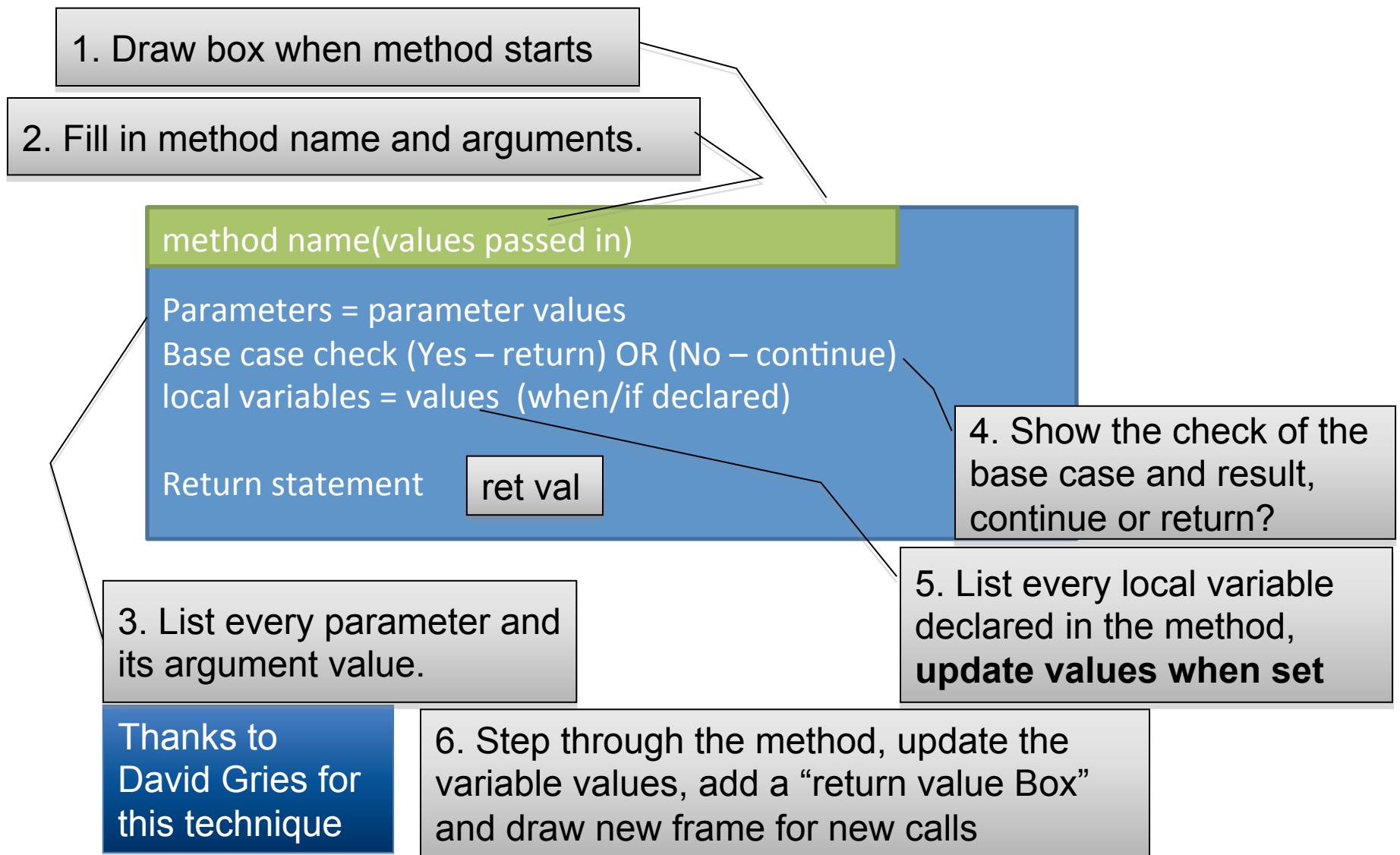
Triangle with width 3



Triangle with width 4



Frames for Tracing Recursive Code



Examples

- Let's look at the first two examples in the code and on the quiz

Q1-Q2

Key Rules to Using Recursion

- ▶ Always have a **base case** that **doesn't recurse**
- ▶ Make sure recursive case always **makes progress**, by **solving a smaller problem**
- ▶ **You gotta believe**
 - Trust in the recursive solution
 - Just consider one step at a time

Programming Problem

- Let's look at SimplePalindrome. There are a couple ways to approach this

Recursive Helpers

- ▶ Our `isPalindrome()` makes lots of new `String` objects (using `substring`)
- ▶ We can make it better with a “recursive helper method”
 - ▶ Many recursive problems require a helper method

```
public boolean isPalindrome() {  
    return isPalindrome(0, this.text.length() - 1);  
}  
Position of first letter of the  
remaining String to check  
Position of last letter of the  
remaining String to check
```

And the rest...

- Let's look at the remaining examples in the quiz and in eclipse.

Practice Practice Practice

- Head to <http://codingbat.com/java/Recursion-1> and solve 5 problems. I personally like bunnyEars, bunnyEars2, count7, fibonacci, and noX
- Get help from me if you get stuck
- Then take a look at the recursion homework