## Python's range expression

Recall that a range expression generates integers that can be used in a FOR loop, like this: $\qquad$

## for $k$ in range( $n$ ):

... k ...

In that example, $\boldsymbol{k}$ takes on the values $0,1,2, \ldots n-1$, as the loop runs. That is:

$$
\begin{array}{ll}
\text { range(n) } \quad \begin{array}{l}
\text { generates } n \text { integers starting at } \boldsymbol{\theta} \\
\text { (and hence ending at } \boldsymbol{n}-\mathbf{1} \text { ). }
\end{array} .
\end{array}
$$

Python allows two other forms of the range expression, for your convenience. You never have to use these forms (the singleargument form is sufficient), but they are often handy.

```
range(m, n) generates integers starting at m,
    ending at n-1 (and hence
    generates }\boldsymbol{n}\mathrm{ -m integers if }\boldsymbol{n}\geq\boldsymbol{m}\mathrm{ ).
```

For example, the loop shown below to the left generates the output shown below to the right.


Caution: range $(m, n)$ generates NO integers if $n \leq m$. For example, the loop for $\mathbf{k}$ in range $(9,5)$ : runs NO times:
for $k$ in range(9, 5): $\longrightarrow \quad$ (no output)
print(k)

The third form of the range expression works like this:

```
range(m, n, j) generates integers starting at m,
    in "steps" of j,
```

stopping when the generated integer would be greater than or equal to $\boldsymbol{n}$ (if $\boldsymbol{j}$ is positive) or when the generated integer would be less than or equal to $\boldsymbol{n}$ (if $\boldsymbol{j}$ is negative).

For example, the loops below generate the output shown to the right.

$\triangle$
Caution: In all three forms, the generated numbers start at the first number and stop just before reaching the "stop" number:

| for $k$ in range(30): | does not include 30 |
| :--- | :--- |
| for $k$ in range(3, 56): | does not include 56 |
| for $k$ in range (10, 40, 5): | does not include 40 |
| for $k$ in range (40, 10, -5$)$ : does not include 10 |  |

So the example to the right does NOT generate 5, 4, 3, 2, 1, 0, as the student hoped. (Figure out why and then look at the next page.)
for $k$ in range(5, 0, -1): print(k)

Answer: the loop to the right stops just before it reaches 0 , so it generates 5, 4, 3, 2, 1 (which may or may not be what you intend).


## Summary:

| range $(n) \quad$generates $n$ integers starting at $\boldsymbol{\theta}$ <br> (and hence ending at $\boldsymbol{n - 1})$. |
| :--- | :--- |
| range $(m, n) \quad$generates integers starting at $m$, <br> ending at $n-\mathbf{1} \quad$ (and hence <br> generates $n-m$ integers if $n \geq m)$. |
| range ( $m, n, j$ ) $\quad$generates integers starting at $m$, <br> in "steps" of $\boldsymbol{j}$, |
| stopping when the generated integer would be greater than <br> or equal to $n$ (if $\boldsymbol{j}$ is positive) or when the generated integer <br> would be less than or equal to $n$ (if $\boldsymbol{j}$ is negative). |

Don't hesitate to use the two and three-argument forms when they clarify the code, but be aware of the pitfalls that may arise.

