

# ALLOY ANALYSIS

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# GOALS FOR TODAY

- **THINK ABOUT HOW ALLOY WORKS INTERNALLY.  
IT'S JUST ANOTHER PROGRAM AFTER ALL.**
- **CLEAR UP ANY CONFUSION REGARDING THE  
PROJECT**

HOW DOES COMPUTER  
PROGRAMMING WORK?

MAGIC.



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# ALLOY ANALYSIS

A PEEK UNDER THE HOOD

# EQUIVALENT PROBLEMS

- CHECKING ASSERTIONS IS EQUIVALENT TO RUNNING PREDICATES
- FIND SOME ASSIGNMENT OF RELATIONS TO VARIABLES THAT MAKES CONSTRAINTS TRUE
- PREDICATES:  
SIGS + FIELDS + FACTS + **PREDICATE CONSTRAINTS**
- ASSERTIONS:  
SIGS + FIELDS + FACTS + **NOT(ASSERTION CONSTRAINTS)**

# THE PROBLEM

- **ALLOY'S LOGIC IS UNDECIDABLE**
- **IMPOSSIBLE TO BUILD A TOOL THAT CAN CHECK EVERY ASSERTION**
- **MUST MAKE SOME COMPROMISES**

**ANY LOGIC STRONG ENOUGH  
TO MODEL SOFTWARE SYSTEMS  
IS (PROBABLY) UNDECIDABLE**

# TRADITIONAL COMPROMISE

- **USE AUTOMATED THEOREM PROVING**
  - TRIES TO BUILD PROOF THAT ASSERTION HOLDS
  - REQUIRES GUIDANCE FROM USER
- **SUCCESS? – ASSERTION DEFINITELY HOLDS**
- **FAILURE? – ASSERTION MAY OR MAY NOT HOLD**

HARD TO TELL  
WHICH IS THE CASE!

# ALLOY'S COMPROMISE

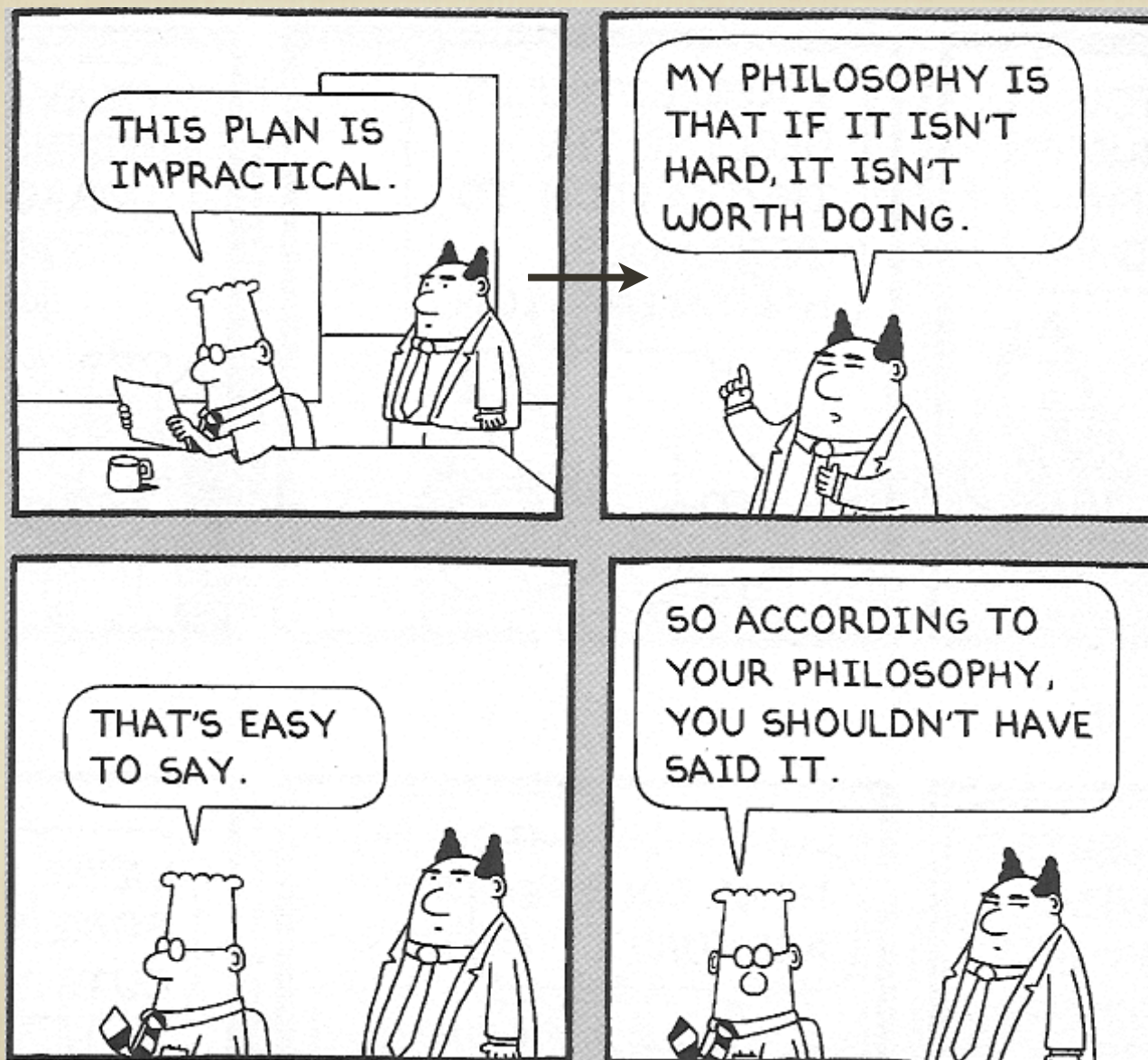
- **USE INSTANCE FINDING**
  - **LOOKS FOR A “REFUTATION” BY CHECKING AGAINST A HUGE SET OF TEST CASES**
- **SUCCESS? – PRODUCES COUNTEREXAMPLE**
- **FAILURE? – ASSERTION MAY HOLD, OR THERE MAY BE A LARGER COUNTEREXAMPLE THAN WAS CHECKED**

# WHY INSTANCE FINDING?

- DURING EXPLORATORY MODELING MOST ASSERTIONS WILL BE INVALID
- SPECIFIC COUNTEREXAMPLES ARE HELPFUL
- INVALID ASSERTIONS CAN BE FOUND QUICKLY

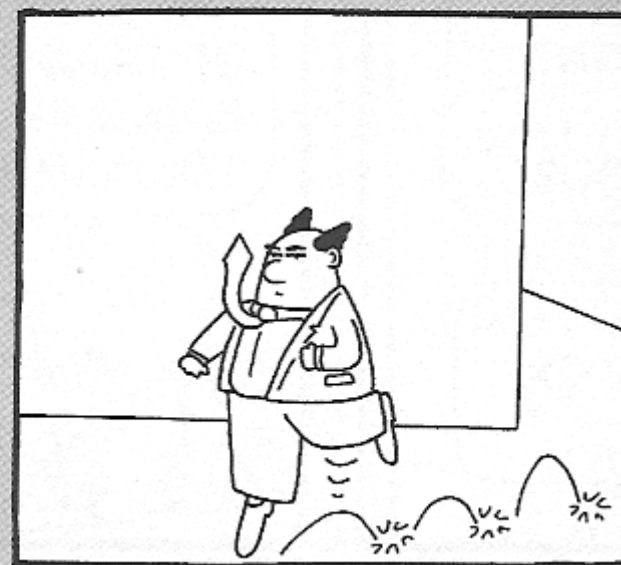
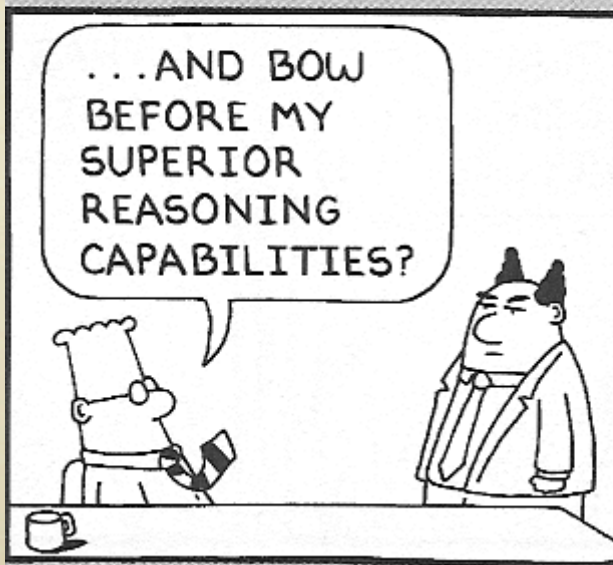
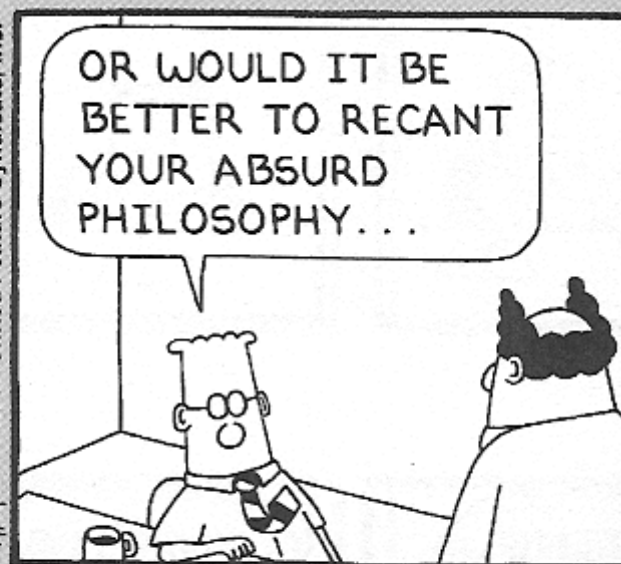
CAN STOP AFTER FIRST  
COUNTEREXAMPLE

# CARTOON OF THE DAY





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# TRACTABLE INSTANCE FINDING

- LIMIT SCOPE OF EACH SIGNATURE TO CONTROL SIZE OF SEARCH SPACE
- STILL HANDLES HUGE NUMBER OF TEST CASES
- MY P1 SOLUTION:
  - 1 LIFT, 5 FLOORS, 25 MOMENTS IN TIME, 2 DIRECTIONS, 2 DOOR STATES:
    - CURRENT FLOOR RELATION: 25 POSSIBILITIES
    - REQUESTS RELATION:  $25 \times 2^5$  POSSIBILITIES
    - DIRECTION INDICATOR RELATION:  $25 \times 3$  POSSIBILITIES
    - PLANNED DIRECTION RELATION:  $25 \times 3$  POSSIBILITIES
    - DOORS RELATION:  $25 \times 2$  POSSIBILITIES

**MORE THAN 5.6 BILLION  
INSTANCES CHECKED!**

**PROGRAM TESTING CAN BE USED  
TO SHOW THE PRESENCE OF BUGS,  
BUT NEVER TO SHOW THEIR ABSENCE.**

**DIJKSTRA**

**IT CAN'T USUALLY SHOW  
THEIR PRESENCE EITHER.**

**– JACKSON**

# **THE SMALL SCOPE HYPOTHESIS**

**MOST BUGS HAVE SMALL  
COUNTEREXAMPLES**

# P1 QUESTIONS