

## MA/CSSE 474 Homework #3 (33 points total) Updated for Spring, 2018

Submit to drop box on Moodle.

2.1 means Exercise 1 from Chapter 2.

You do not have to turn in the problems that are not highlighted in yellow, but you should still think about them.

Please reread the instructions that precede the problem list in the HW1 assignment sheet. They apply here also.

1. (t-6) 5.2(j) *aa and bb as substrings* [If you need simpler practice (and you probably do!), do some other parts of 5.2 first]. For this and other similar problems, you do not need to give the entire formal definition of your FSM.  
A transition diagram or transition table is sufficient.
2. (t-6) 5.2(l) *no more than one pair of consecutive 0's and 1's* (that's part *el*, the letter that comes between *k* and *m* in the English alphabet)
3. 5.3 *Rock, Paper, Scissors*
4. (t-3) 5.4 *L(M) contains  $\varepsilon$*  The answer is simple and straightforward, so don't look for anything complicated or tricky.
5. (t-6) *divisible by 3* Let  $L$  be  $\{w \in \{0, 1\}^* : \exists n, k \in \mathbb{N} (w = \langle n \rangle \wedge n = 3k)\}$ . I.e. the set of binary representations of natural numbers that are divisible by 3. Leading zeroes are allowed. Recall that  $0 \in \mathbb{N}$ .  
Draw the transition diagram or a transition table for a DFSA that accepts  $L$ . [Hint: think about remainders *mod* 3. Another hint: There are not many states].
6. 5.5 *determine membership in L(M)*
7. 5.6(a) *FSM to accept a simple language*
8. (t-6) 5.6(c) *decimal encoding of integer with a substring divisible by 3* Note that this one is decimal, while problem 5 is binary. Also notice the "contains a substring" part.
9. (t-6) 5.7 *three identical symbols in a row*

Some past questions and answers from Piazza:

### Minimize FSM?

Q: Should we try to minimize our FSM on the homework or does it matter?

A: Trying to write your DFSA's with as few states as you can is a good idea, but it is not required for this assignment. Later this week we will look at an algorithm for doing that.

## Pair of consecutive 1s/0s Problem 2

Q: For Problem #2 in HW 3 (2.1), does 111 constitute as 1 or 2 pairs of consecutive 1s? You could count the 2nd 1 as the 2nd 1 in the 1st pair or the 1st 1 in the 2nd pair.

A: There are indeed two pairs in the three 1's.

## HW3 Problem 5: Are the binary strings fed with the most significant bit first?

Q: Does it not matter?

A: Unless a specific problem specifies otherwise, assume that binary strings are written with the most significant bit/digit first.

## Empty string in HW 3 problem 5

Q: For problem 5 (binary representations of integers divisible by 3), can we consider the empty string a representation of 0, or should we avoid this?

A: The machine should not accept the empty string.