

NAME \_\_\_\_\_ BOX NUMBER \_\_\_\_\_

Problem 1 ( 30 ) \_\_\_\_\_

Problem 2 ( 40 ) \_\_\_\_\_

Problem 3 ( 30 ) \_\_\_\_\_

\_\_\_\_\_

Total (100) \_\_\_\_\_

**INSTRUCTIONS**

- **Closed book/notes exam. (Unit conversion page provided)**
- **Help sheet allowed. (8-1/2 x 11" sheet of paper, one side)**
- **Laptops may be used; however, no pre-prepared worksheets or files may be used.**

1) Show all work for complete credit.

- Start all problems at the ANALYSIS stage, but clearly label any information you use for your solution.

• **Problems involving conservation principles MUST clearly identify the system and show a clear, logical progression from the basic principle.**

- Don't expect us to read your mind as to how or why you did something in the solution. Clearly indicate how you arrived at your answer.
- **Always crunch numbers last on an exam.** The final numerical answer is worth the least amount of points. (Especially if all I would have to do is plug in the numbers into a well-documented solution.)

2) Useful Rule of Thumb (Heuristic): (100 point exam)/(50 min) = 2 points/minute. That means a 10 point problem is not worth more than 5 minutes of your time (at least the first time around).

3) Please remain seated until the end of class or everyone finishes. (Raise your hand and I'll pick up your exam if you have other work you need or want to do.)

<u>USEFUL INFORMATION</u>	SI	USCS	Molar Mass	
Ideal Gas Constant: $R_u = 8.314 \text{ kJ}/(\text{kmol}\cdot\text{K})$		$= 1545 \text{ (ft}\cdot\text{lbf)}/(\text{lbmol}\cdot^\circ\text{R})$	Air	28.97
		$= 1.986 \text{ Btu}/(\text{lbmol}\cdot^\circ\text{R})$	O <sub>2</sub>	32.00
Standard Acceleration of Gravity: $g = 9.810 \text{ m/s}^2$		$= 32.174 \text{ ft/s}^2$	N <sub>2</sub>	28.01
Density of liquid water $= 1000 \text{ kg/m}^3$		$= 62.4 \text{ lbm/ft}^3$	H <sub>2</sub>	2.016
		$= 1.94 \text{ slug/ft}^3$	CO <sub>2</sub>	44.01

## Length

$$1 \text{ ft} = 12 \text{ in} = 0.3048 \text{ m} = 1/3 \text{ yd}$$

$$1 \text{ m} = 100 \text{ cm} = 1000 \text{ mm} = 39.37 \text{ in} = 3.2808 \text{ ft}$$

$$1 \text{ mile} = 5280 \text{ ft} = 1609.3 \text{ m}$$

## Mass

$$1 \text{ kg} = 1000 \text{ g} = 2.2046 \text{ lbm}$$

$$1 \text{ lbm} = 16 \text{ oz} = 0.45359 \text{ kg}$$

$$1 \text{ slug} = 32.174 \text{ lbm}$$

## Temperature Values

$$(T/K) = (T/^{\circ}\text{R}) / 1.8$$

$$(T/K) = (T/^{\circ}\text{C}) + 273.15$$

$$(T/^{\circ}\text{C}) = [(T/^{\circ}\text{F}) - 32] / 1.8$$

$$(T/^{\circ}\text{R}) = 1.8(T/K)$$

$$(T/^{\circ}\text{R}) = (T/^{\circ}\text{F}) + 459.67$$

$$(T/^{\circ}\text{F}) = 1.8(T/^{\circ}\text{C}) + 32$$

## Temperature Differences

$$(\Delta T/^{\circ}\text{R}) = 1.8(\Delta T / K)$$

$$(\Delta T/^{\circ}\text{R}) = (\Delta T/^{\circ}\text{F})$$

$$(\Delta T / K) = (\Delta T/^{\circ}\text{C})$$

## Volume

$$1 \text{ m}^3 = 1000 \text{ L} = 10^6 \text{ cm}^3 = 10^6 \text{ mL} = 35.315 \text{ ft}^3 = 264.17 \text{ gal}$$

$$1 \text{ ft}^3 = 1728 \text{ in}^3 = 7.4805 \text{ gal} = 0.028317 \text{ m}^3$$

$$1 \text{ gal} = 0.13368 \text{ ft}^3 = 0.0037854 \text{ m}^3$$

## Volumetric Flow Rate

$$1 \text{ m}^3/\text{s} = 35.315 \text{ ft}^3/\text{s} = 264.17 \text{ gal/s}$$

$$1 \text{ ft}^3/\text{s} = 1.6990 \text{ m}^3/\text{min} = 7.4805 \text{ gal/s} = 448.83 \text{ gal/min}$$

## Force

$$1 \text{ N} = 1 \text{ kg}\cdot\text{m}/\text{s}^2 = 0.22481 \text{ lbf}$$

$$1 \text{ lbf} = 1 \text{ slug}\cdot\text{ft}/\text{s}^2 = 32.174 \text{ lbm}\cdot\text{ft}/\text{s}^2 = 4.4482 \text{ N}$$

## Pressure

$$1 \text{ atm} = 101.325 \text{ kPa} = 1.01325 \text{ bar} = 14.696 \text{ lbf}/\text{in}^2$$

$$1 \text{ bar} = 100 \text{ kPa} = 10^5 \text{ Pa}$$

$$1 \text{ Pa} = 1 \text{ N}/\text{m}^2 = 10^{-3} \text{ kPa}$$

$$1 \text{ lbf}/\text{in}^2 = 6.8947 \text{ kPa} = 6894.7 \text{ N}/\text{m}^2$$

[lbf/in<sup>2</sup> often abbreviated as “psi” ]

## Energy

$$1 \text{ J} = 1 \text{ N}\cdot\text{m}$$

$$1 \text{ kJ} = 1000 \text{ J} = 737.56 \text{ ft}\cdot\text{lbf} = 0.94782 \text{ Btu}$$

$$1 \text{ Btu} = 1.0551 \text{ kJ} = 778.17 \text{ ft}\cdot\text{lbf}$$

$$1 \text{ ft}\cdot\text{lbf} = 1.3558 \text{ J}$$

## Energy Transfer Rate

$$1 \text{ kW} = 1 \text{ kJ}/\text{s} = 737.56 \text{ ft}\cdot\text{lbf}/\text{s} = 1.3410 \text{ hp} = 0.94782 \text{ Btu}/\text{s}$$

$$1 \text{ Btu}/\text{s} = 1.0551 \text{ kW} = 1.4149 \text{ hp} = 778.17 \text{ ft}\cdot\text{lbf}/\text{s}$$

$$1 \text{ hp} = 550 \text{ ft}\cdot\text{lbf}/\text{s} = 0.74571 \text{ kW} = 0.70679 \text{ Btu}/\text{s}$$

## Specific Energy

$$1 \text{ kJ}/\text{kg} = 1000 \text{ m}^2/\text{s}^2$$

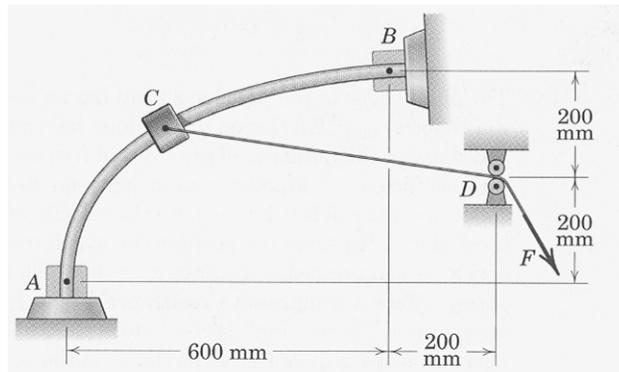
$$1 \text{ Btu}/\text{lbm} = 25037 \text{ ft}^2/\text{s}^2$$

$$1 \text{ ft}\cdot\text{lbf} / \text{lbm} = 32.174 \text{ ft}^2/\text{s}^2$$

**Problem 1** (30 points)

The collar  $C$  slides on the curved rod in the vertical plane under the action of a constant force  $F$  in the cord guided by the small pulleys at  $D$ . The collar has a mass of  $0.70$  kg and slides without friction.

If the collar is released from rest at  $A$ , determine the value of the constant force  $F$  that will result in the collar striking the stop at  $B$  with a velocity of  $4$  m/s.



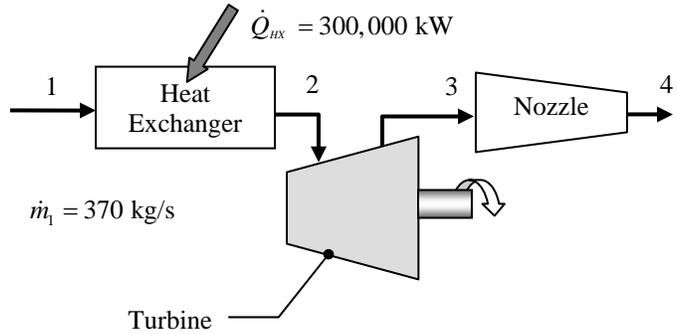
**Problem 2** (40 points)

The system shown at right is the back end of a jet aircraft engine. Operating information about the system is shown in the table and figure. Air flows steadily through the system. Assume changes in gravitational potential energy are negligible and air can be modeled as an ideal gas with room temperature specific heats.

- (a) Determine the velocity of the air leaving the nozzle, in m/s.
- (b) Determine the cross-sectional area  $A_c$  at the nozzle outlet, in  $m^2$
- (c) Determine the shaft power out of the turbine, in kW.

State	$T$ ( $^{\circ}C$ )	$P$ (kPa)	$V$ (m/s)	$A_c$ ( $m^2$ )
1	600	800	$V_1 \approx V_2$	----
2	???	800	$V_2 \approx V_3$	----
3	1300	600	$V_3 \ll V_4$	----
4	950	100	???	???

Turbine: steady-state and adiabatic  
 Nozzle: steady-state and adiabatic  
 Heat exchanger: steady-state



**Problem 3** (30 points)

A well-insulated copper tank of mass 13 kg contains 4 kg of liquid water. Initially, the temperature of the copper is  $27^{\circ}\text{C}$  and the temperature of the water is  $50^{\circ}\text{C}$ . As the tank and its contents come to equilibrium, an electrical resistor of negligible mass transfers 100 kJ of energy to the contents of the tank. Assume copper and liquid water can be modeled as incompressible substances.

- (a) Determine the final temperature of the tank and water.
- (b) If current through the resistor is 0.5 amps and the applied voltage is 110 volts, determine (i) the electrical power supplied to the resistor and (ii) how long the resistor was “on” to deliver 100 kJ of electrical energy.

