ECE-300, Quiz #4

1) Assume we are going to synthesize a periodic signal x(t) using $x(t) = \sum c_k e^{jk\omega_0 t}$ where

$$c_k = \frac{j}{1+k^2}$$
. Will $x(t)$ be a real function?

a) Yes b) No

2) Assume we are going to synthesize a periodic signal x(t) using $x(t) = \sum c_k e^{jk\omega_0 t}$

where
$$c_k = \frac{jk}{1+ik}$$
. Will $x(t)$ be a real function? a) Yes b) No

3) Assume $x(t) = 3\cos(2t-5)$ is the input to a system with transfer function

$$H(\omega) = \begin{cases} 3e^{-j2\omega} & |\omega| < 3\\ 2 & else \end{cases}$$

the output y(t) in steady state will be

a)
$$y(t) = 6\cos(2t - 5)$$

b)
$$y(t) = 9\cos(2t - 5)$$

c)
$$y(t) = 9\cos(2t-5)e^{-j4}$$
 d) $y(t) = 9\cos(2t-9)$

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4) Assume $x(t) = 2\cos(3t)$ is the input to system with transfer function $H(j\omega) = 2e^{-j\omega}$. In steady state the output of the system will be

a)
$$y(t) = 4\cos(3t)e^{-j\omega}$$

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$$y(t) = 4\cos(3t)e^{-j\omega}$$
 b) $y(t) = 4\cos(3t)e^{-j3}$ c) $y(t) = 4\cos(3t-3)$

c)
$$v(t) = 4\cos(3t - 3)$$

d)
$$y(t) = 4\cos(3t+3)$$
 e) none of these

5) Assume x(t) is a periodic function with period T=2 seconds. x(t) is defined over one period as x(t) = t, -1 < t < 1. The average power in x(t) (the power averaged over one period)

a) 0 b)
$$\frac{1}{2}$$
 c) $\frac{1}{3}$ d) $\frac{2}{3}$

c)
$$\frac{1}{3}$$

d)
$$\frac{2}{3}$$

Problems 6 and 7 refer to the following Fourier series representation of a periodic signal

$$x(t) = 2 + \sum_{k=-\infty}^{k=\infty} \frac{2}{2+jk} e^{\frac{jkt}{2}}$$

- 6) The average value of x(t) is
- a) 0
- b) 1 c) 2
- d) 3

7) The fundamental frequency (in Hz) is a) $\frac{1}{2\pi}$ b) 0.5 c) $\frac{1}{4\pi}$ d) 2

a)
$$\frac{1}{2\pi}$$

b) 0.5 c)
$$\frac{1}{4\pi}$$

8) Assume $x(t) = 2\cos(t) + 5\sin(2t) + 6\sin(3t)$ is the input to a system with transfer function $H(j\omega) = 3\Pi\left(\frac{\omega}{5}\right)$. In steady state the output of the system will be

a)
$$y(t) = \left[2\cos(t) + 5\sin(2t) + 6\sin(3t)\right] \left[3\operatorname{rect}\left(\frac{\omega}{5}\right)\right]$$

- b) $y(t) = 6\cos(t) + 15\sin(2t) + 18\sin(3t)$
- c) $y(t) = 6\cos(t) + 15\sin(2t)$
- d) none of these

9) Assume $x(t) = 2\cos(3t) + 4\cos(5t)$ is the input to a system with transfer function given by

$$H(j\omega) = \begin{cases} 2 & 4 < |\omega| < 6 \\ 0 & else \end{cases}$$

The output of the system in steady state will be

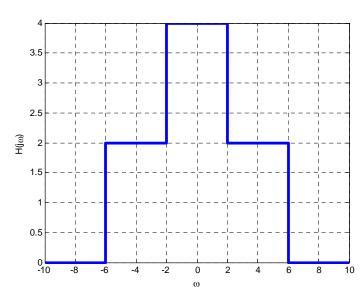
a)
$$y(t) = 4\cos(3t) + 8\cos(5t)$$

b)
$$y(t) = 8\cos(5t)$$

c)
$$y(t) = 4\cos(3t)$$

d) none of these

10) Assume $x(t) = \cos(t) + \cos(5t) + \cos(9t)$ is the input to a system with transfer function



given below:

The output of this system in steady state will be

a)
$$y(t) = 4\cos(t) + 4\cos(5t)$$
 b) $y(t) = 4\cos(t) + 2\cos(5t) + \cos(9t)$

c)
$$y(t) = 4\cos(t) + 2\cos(5t)$$
 d) none of these