

# CSSE 220 Day 13

Multithreading  
Recursion

Checkout *Multithreading* and  
*Recursion* project from SVN

# Questions

# The World is Concurrent

»» Joe Armstrong,  
*Programming in Erlang*

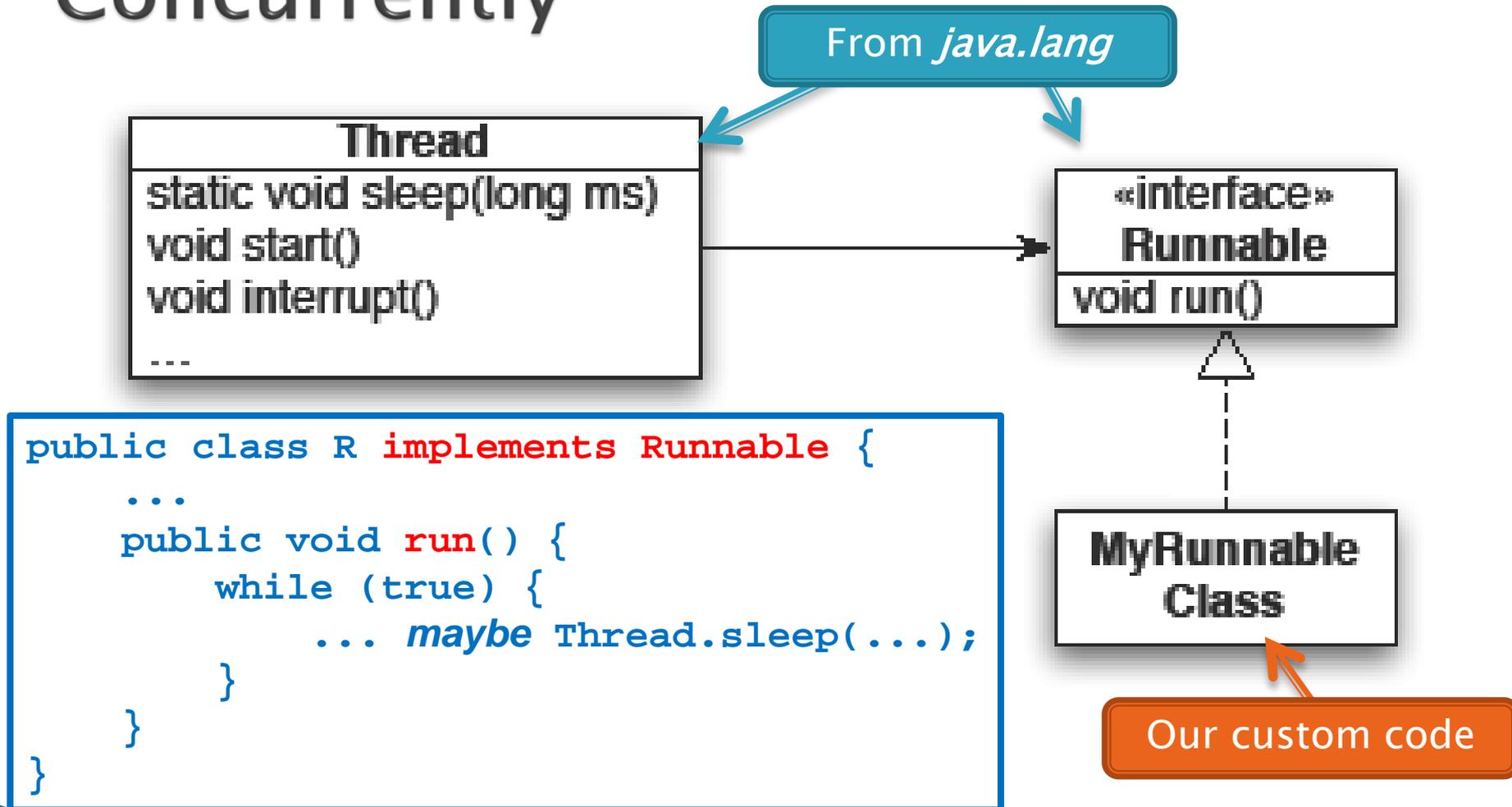
# Multithreading

- ▶ A technique to:
  - Run multiple pieces of code “simultaneously” on a single machine

Time → Slices	1	2	3	4	5	6	7	8	9	10	11	12	13	14
running thread 1	█	█	□	█	□	□	□	█	□	█	□	□	█	█
running thread 2	□	□	█	□	█	█	█	□	█	□	█	█	□	□

- Run different parts of a program on different processor cores

# Running Our Own Code Concurrently



Wherever you want to start the Thread:

```
new Thread(object of type R).start();
```

Q3

# Animation with Threads

- ▶ Example 1: A single object
  - “Animate” it with button clicks
  - Animate it with a Timer

```
Timer timer = new Timer(50, animatorButton);  
timer.start();
```

- Animate it by using a thread

```
public class R implements Runnable {  
    ...  
    public void run() {  
        while (true) {  
            ... maybe Thread.sleep(...);  
        }  
    }  
}
```

Wherever you want to start the Thread:

```
new Thread(object of type R).start();
```

# Animation with Threads

- ▶ Example 2: Multiple objects
  - Use separate thread for each object's "brain"
  - Another thread asks Java to update the GUI



# Other Uses for Threads

- ▶ Web servers: many users connecting
  - ▶ Desktop applications:
    - layout, spellchecking, auto-save, ...
  - ▶ Scientific computing
  - ▶ Weather forecasting
  - ▶ ...
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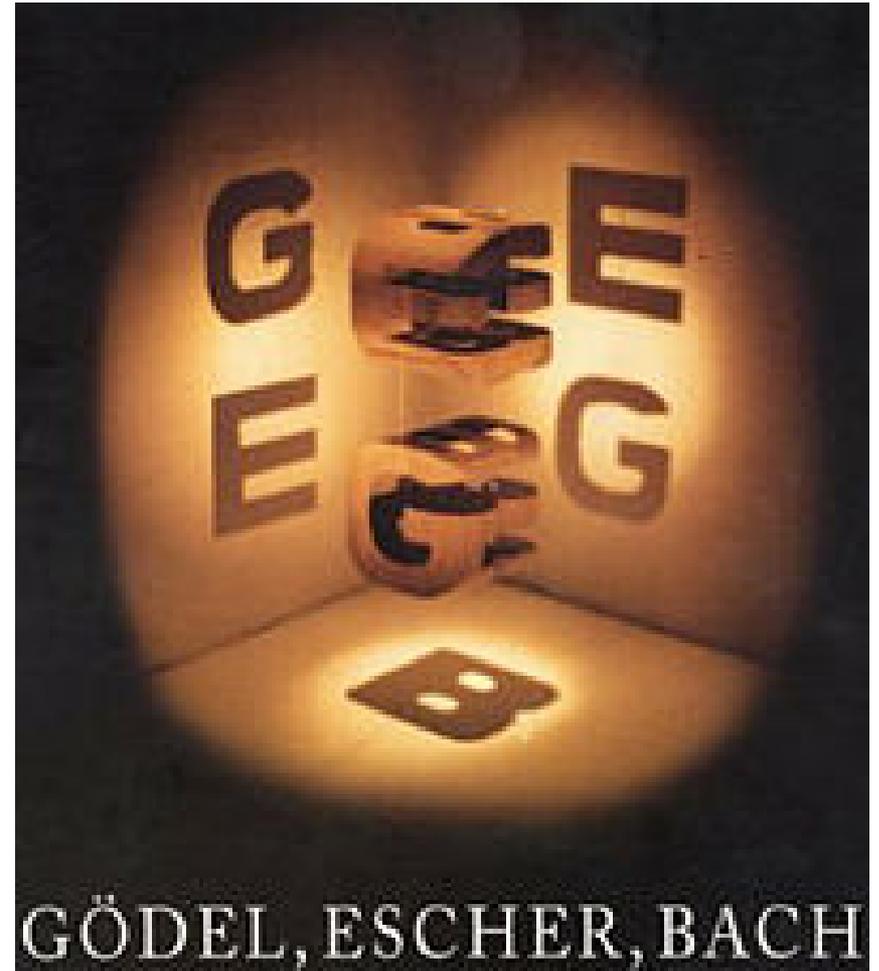
# Caution!

- ▶ What if one thread is in the middle of performing an action when its time slice ends?
- ▶ What if a second thread's action interferes with the first's action?
- ▶ See bank example in today's project

**Optional:** For a way to fix this, see Big Java Section 20.4

# Gödel, Escher, Bach

- ▶ By Douglas Hofstadter
- ▶ Argues that a major component of intelligence is **our ability to think about thinking**



# Recursion

- ▶ A solution technique where the same computation **occurs repeatedly** as the problem is solved



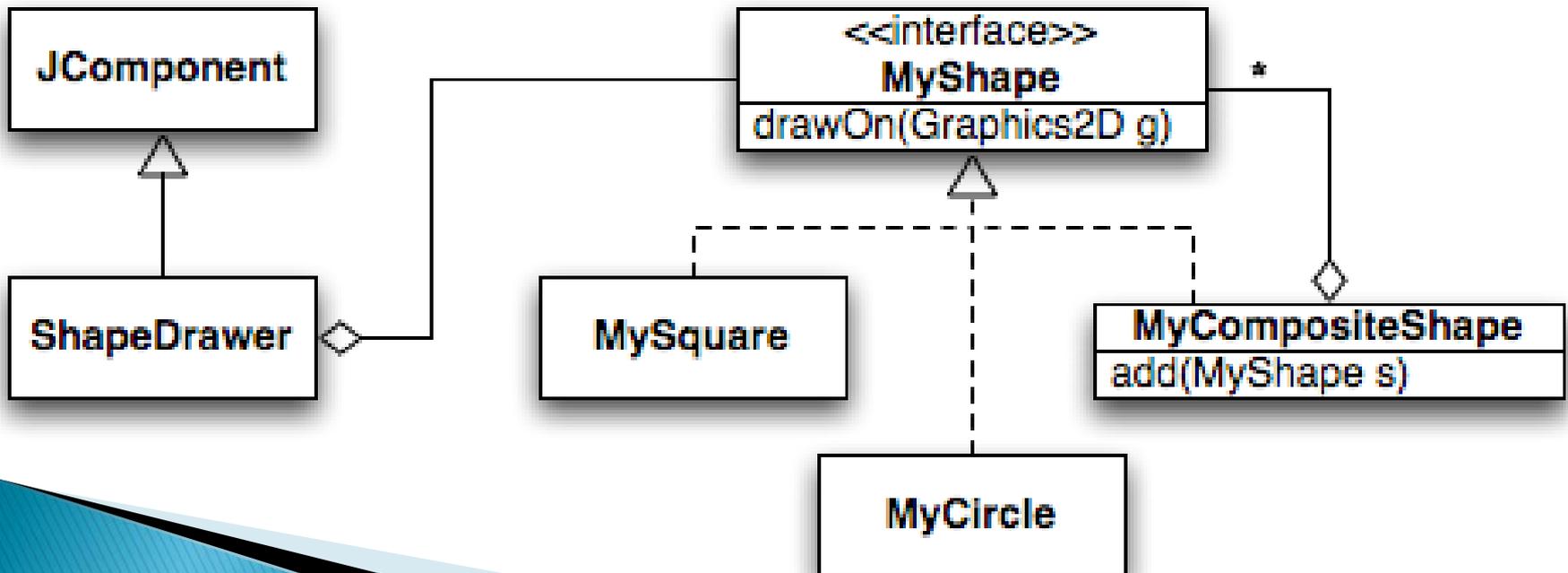
recurs

- ▶ Examples:
  - Sierpinski Triangle: tonight's HW
  - Towers of Hanoi:  
<http://www.mathsisfun.com/games/towerofhanoi.html>  
or search for Towers of Hanoi

# Recursion

- ▶ A solution technique where the same computation **occurs repeatedly** as the problem is solved

recurs



# An example – Triangle Numbers

- ▶ If each red block has area 1, what is the *area*  $A(n)$  of the Triangle whose *width* is  $n$ ?

- Answer:

$$A(n) = n + A(n-1)$$

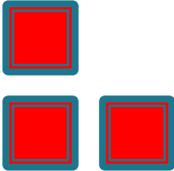
- ▶ The above holds for which  $n$ ? What is the answer for other  $n$ ?

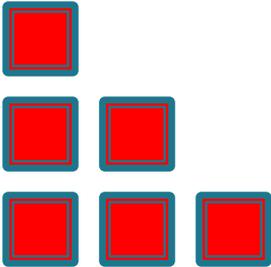
- Answer: The recursive equation holds for

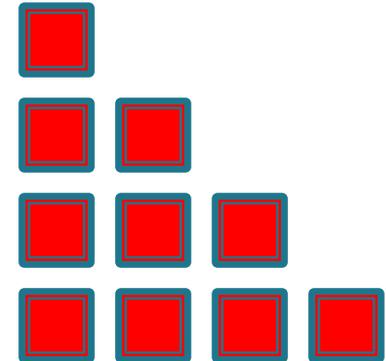
$$n \geq 1.$$

For  $n = 0$ , the area is 0.

Triangle with width 1 {  }

Triangle with width 2 {  }

Triangle with width 3 {  }

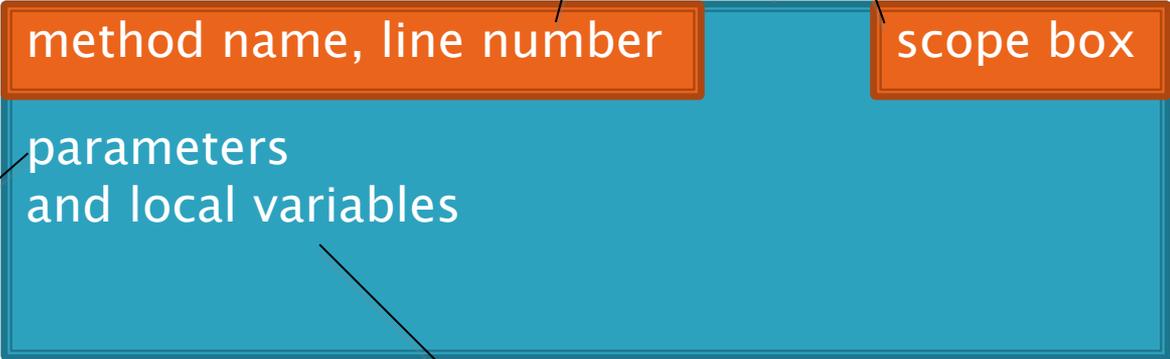
Triangle with width 4 {  }

# Frames for Tracing Recursive Code

1. Draw box when method starts

2. Fill in name and first line no.

3. Write class name (for static method) or draw reference to object (for non-static method)



4. List every parameter and its argument value.

5. List every local variable declared in the method, **but no values yet**

6. Step through the method, update the line number and variable values, draw new frame for new calls

Thanks to David Gries for this technique

7. "Erase" the frame when the method is done.

Q5-Q6

# Optional Practice

- ▶ Trace the **buildShape(MAX\_DEPTH)** method call in **shapes.Main's** main method

# Key Rules to Using Recursion

- ▶ Always have a **base case** that **doesn't recurse**
- ▶ Make sure recursive case always **makes progress**, by **solving a smaller problem**
- ▶ **You gotta believe**
  - Trust in the recursive solution
  - Just consider one step at a time

# Programming Problem

- ▶ Add a recursive method to Sentence for computing whether Sentence is a palindrome

Sentence
String text
String toString() boolean isPalindrome

# Recursive Helpers

- ▶ Our `isPalindrome()` makes lots of new Sentence objects
- ▶ We can make it better with a “recursive helper method”
  - ▶ Many recursive problems require a helper method

```
public boolean isPalindrome() {  
    return isPalindrome(0, this.text.length() - 1);  
}
```



Position of first letter of the remaining String to check



Position of last letter of the remaining String to check

# Homework part 1

- ▶ Reverse a string...recursively!
  - ▶ A recursive helper can make this really short!
- 

# Another Definition of Recursion

- ▶ “If you already know what recursion is, just remember the answer. Otherwise, find someone who is standing closer to Douglas Hofstadter than you are; then ask him or her what recursion is.”

—Andrew Plotkin

# Recursive Functions

- ▶ Factorial:

$$n! = \begin{cases} 1 & \text{if } n \leq 1 \\ n * (n - 1)! & \text{otherwise} \end{cases}$$

Base Case

Recursive step

- ▶ Ackermann function:

$$A(m, n) = \begin{cases} n + 1 & \text{if } m = 0 \\ A(m - 1, 1) & \text{if } m > 0 \text{ and } n = 0 \\ A(m - 1, A(m, n - 1)) & \text{otherwise} \end{cases}$$

# Team Project

## »» Work time

*Be sure everyone is getting a chance to drive.*