Finding Thermodynamic Properties for a Pure, Simple Compressible Substance
— A Simple Algorithm for Liquid-Vapor Systems

Case I: Given $P$ and $T$

(1) Determine the phase of the substance (and hence what set of tables you should consult).

(1a) Go to one of the liquid-vapor Saturation Tables.
(1b) Compare the given $P$ and $T$ against the saturation values reported in the table.

In the Pressure Saturation Table, find the saturation temperature at the given pressure, $T_{\text{sat}(P)}$.
- if $T > T_{\text{sat}(P)}$ then superheated vapor
- if $T < T_{\text{sat}(P)}$ then the compressed (subcooled) liquid

In the Temperature Saturation Table, find the saturation pressure at the given temperature, $P_{\text{sat}(T)}$.
- if $P > P_{\text{sat}(T)}$ then compressed (subcooled) liquid
- if $P < P_{\text{sat}(T)}$ then superheated vapor

(2) Go to the appropriate single-phase table and enter the table using $P$ and $T$. If the values of $P$ and $T$ do not coincide with the given values (as usually happens in real applications) you must linearly interpolate within the table to find the desired values.

**Note: Compressed Liquid Approximation.** If you find the substance is a compressed (subcooled) liquid and you do not have a compressed-liquid table or the pressure is between the saturation value and the lowest value in the compressed-liquid table, you may find it easier (and almost as accurate) to apply the compressed-liquid approximation to estimate the values in the compressed-liquid table using the saturation-table values as follows:

- $u_{(T,P)} \cong u_{f(T)}$ [specific internal energy]
- $v_{(T,P)} \cong v_{f(T)}$ [specific volume]
- $s_{(T,P)} \cong s_{f(T)}$ [specific entropy]
- $h_{(T,P)} = u + P v \cong u_{f(T)} + P v_{f(T)} = h_{f(T)} + \{ P - P_{\text{sat}(T)} \} v_{f(T)}$ [specific enthalpy]

Because $h_{(T,P)} = h_{f(T)}$ is only true if $P = P_{\text{sat}}$ and the error in using this approximation under conditions where $P \neq P_{\text{sat}}$ depends on the specific problem, it is always more accurate to use the full approximation that includes the pressure correction!
**Case II: Given $P$ (or $T$) and $\nu$ (or $u, h, s$ or $x$)**

**1) Determine the phase of the substance** (and hence what set of tables you should consult).

(1a) Go to one of the liquid-vapor Saturation Tables.

(1b) Find the saturated liquid and saturated vapor values for the specific volume: $\nu_f(P)$ and $\nu_g(P)$.

Note: If you are given quality $x$ then you immediately know that it is either a saturated liquid, a saturated liquid-vapor mixture, or a saturated vapor and you can go directly to step (2).

(1c) Compare the given value of $\nu$ against the saturation values to find the phase (and the appropriate table):

- $\nu < \nu_f(P)$; compressed (subcooled) liquid
- $\nu = \nu_f(P)$; saturated liquid
- $\nu_f(P) < \nu < \nu_g(P)$; saturated liquid-vapor mixture
- $\nu = \nu_g(P)$; saturated vapor
- $\nu > \nu_g(P)$; superheated vapor

**2) Go to the appropriate table and enter the table using the values of $P$ and $\nu$.** Linear interpolation may be required if values do not match table entries.

Compressed Liquid: $\nu < \nu_f(P)$ [Quality is undefined.]
- If compressed-liquid approximation is used, let $\nu_f(T) = \nu$ to find temperature. Then use approximation to find other properties. (Since $\nu_f(T)$ is a very weak function of temperature, this approach is very inaccurate. Much more accurate to look for another property like $s$ or $u$ which is a strong function of temperature.)

Saturated Liquid: $\nu = \nu_f(P)$ [Quality: $x = 0$ or $0\%$]
- All properties equal to those for a saturated liquid.

Saturated Liquid-Vapor Mixture: $\nu_f(P) < \nu < \nu_g(P)$ [Quality: $0 < x < 1$ or $0\% < x < 100\%$]
- $T = T_{sat(P)}$, the saturation temperature at pressure $P$
- Calculate quality before finding any other properties: $x = (\nu - \nu_f) / (\nu_g - \nu_f)$
- Then use quality to find other intensive properties, e.g. $u = u_f + x(u_g - u_f)$

Saturated Vapor: $\nu = \nu_g(P)$ [Quality: $x = 1$ or $100\%$]
- All properties equal to those for a saturated vapor.

Superheated Vapor: $\nu > \nu_g(P)$ [Quality is undefined.]
- Enter the superheated vapor table with $P$ and $\nu$. Because $\nu$ often falls between the tabular values, it is often required to linearly interpolate to find the correct temperature which can then be used to find the other values. Sometimes it is necessary to do a double linear interpolation.

**Note:** If you are given temperature instead of pressure use the same process as above starting with temperature saturation table.