Sketch of impact

Definitions

**Central Impact**: Both mass centers are located on the line of impact (always true for particles).

**Eccentric Impact**: Both mass centers are not located on the line of impact.

**Direct Impact**: Both velocities, $v_A$ and $v_B$, lie along the line of impact.

**Oblique Impact**: Both velocities, $v_A$ and $v_B$, do not lie along the impact.
Procedure:
1. Draw the impact (impulse-momentum diagrams are especially helpful for rigid body impact).
2. Look at each object by itself, that is, define your system to be each object individually first.
   - Is there any direction with no impulsive forces acting? If so, apply LM in that direction. Note: A direction that frequently does not have any impulses acting is along the plane of contact (tangential direction).
   - Is there any point that you could take angular momentum about that has no impulsive moments? If so, apply AM about that point.
3. Look at both objects together, that is, define your system to be both objects.
   - Is there any new direction with no impulsive forces acting? If so, apply LM in that direction.
   - Is there any point that you could take angular momentum about that has no impulsive moments? If so, apply AM about that point.
4. **Coefficient of restitution** (experimentally determined constitutive model for a given combination of materials, assumed to be constant)

\[ e = \left( \frac{v'_{PB_n} - v'_{PA_n}}{v_{PB_n} - v_{PA_n}} \right) \quad \text{or} \quad v'_{PB_n} - v'_{PA_n} = -e(v_{PB_n} - v_{PA_n}) = e(v_{PA_n} - v_{PB_n}) \]

where

- \( e \) = the coefficient of restitution \((0 \leq e \leq 1)\)
- \( v'_{PA_n} \) = the velocity of the point of contact on object A in the normal direction after the impact
- \( v'_{PB_n} \) = the velocity of the point of contact on object B in the normal direction after the impact
- \( v_{PA_n} \) = the velocity of the point of contact on object A in the normal direction before the impact
- \( v_{PB_n} \) = the velocity of the point of contact on object B in the normal direction before the impact

Special Case: Oblique Central Impact

A in t-direction: \( v'_{A_t} = v_{A_t} \)
B in t-direction: \( v'_{B_t} = v_{B_t} \)

A and B together in n-direction: \( m_A v'_{A_n} + m_B v'_{B_n} = m_A v_{A_n} + m_B v_{B_n} \)

Coefficient of Restitution: \( v'_{B_n} - v'_{A_n} = e(v_{A_n} - v_{B_n}) \)