

Worksheet #3 - Cylindrical and Spherical Coordinates

I Convert the coordinates of a point from one system to another system among the Cartesian, cylindrical, and spherical coordinate systems.

Cartesian	Cylindrical	Spherical
(2, 6, -3)	_____	_____
_____	(8, $\pi/6$, 1)	_____
_____	_____	(12, $\pi/6$, $2\pi/3$)

II Sketch the graphs of the equations

(A) $z = 3$

(B) $r = 7$

(C) $\rho = 7$

(D) $r^2 = z$

$$(E) \theta = \pi/6$$

$$(F) \phi = \pi/3$$

$$(G) \rho = 5 \sec(\phi)$$

$$(H) r = \sin(\theta)$$

- III** Convert the equations from Cartesian coordinates to (a) Cylindrical coordinates
(b) Spherical coordinates
(A) $x^2 + y^2 + z^2 = 25$

(B) $x^2 + y^2 = 25$

(C) $x^2 + y^2 + z^2 - 2z = 0$

IV Find inequalities that describe the solid and state the coordinate system used. Try to choose the coordinate systems so that the equations are as simple as possible.

(A) A cube with edges 7 meters long.

(B) A cylindrical shell 8 feet long with an inside diameter of 1.23 feet and an outside diameter of 3.14 feet.

(C) A spherical shell with inside radius of 2 meters and outside radius of 2.5 meters.

(D) The solid that remains after a hole 1 foot in diameter is drilled through the center of a sphere 8 feet in diameter.

Extra Credit The doughnut with outer radius 3 inches and inner radius 1.2 inches.