

NAME _____ BOX NUMBER _____

Problem 1 (30) _____

Problem 2 (35) _____

Problem 3 (35) _____

Total (100) _____

INSTRUCTIONS

- **Closed book/notes exam. (Unit conversion page provided)**
- **Help sheet allowed. (8-1/2 x 11" sheet of paper, one side)**
- **Laptops may be used; however, no pre-prepared worksheets or files may be used.**

1) Show all work for complete credit.

- **Start all problems at the ANALYSIS stage**, but clearly label any information you use for your solution.

• **Problems involving conservation or accounting principles MUST clearly identify the system and show a clear, logical progression from the basic principle(s) to the problem-specific solution.**

- **Don't expect us to read your mind** as to how or why you did something in the solution. Clearly indicate how you arrived at your answer and how you used the given information in the process.
- **Always crunch numbers last on an exam.** The final numerical answer is worth the least amount of points. (Especially if all we would have to do is plug in the numbers into a well-documented solution.)

2) Useful Rule of Thumb (Heuristic): (100 point exam)/(50 min) ≈ 2 point/minute. That means a 10 point problem is not worth more than 5 minutes of your time (at least the first time around).

3) Please remain seated until the end of class or everyone finishes. (Raise your hand and I'll pick up your exam if you have other work you need or want to do.)

USEFUL INFORMATION	SI	USCS	Molar Mass [kg/kmol; lbm/lbmol]	
Ideal Gas Constant: R_u	= 8.314 kJ/(kmol-K)	= 1545 (ft-lbf)/(lbmol-°R)	Air	28.97
		= 1.986 Btu/(lbmol-°R)	O ₂	32.00
Standard Acceleration of Gravity: g	= 9.810 m/s ²	= 32.174 ft/s ²	N ₂	28.01
Density of liquid water	= 1000 kg/m ³	= 62.4 lbm/ft ³	H ₂	2.016
		= 1.94 slug/ft ³	CO ₂	44.01

Length

$$1 \text{ ft} = 12 \text{ in} = 0.3048 \text{ m} = 1/3 \text{ yd}$$
$$1 \text{ m} = 100 \text{ cm} = 1000 \text{ mm} = 39.37 \text{ in} = 3.2808 \text{ ft}$$
$$1 \text{ mile} = 5280 \text{ ft} = 1609.3 \text{ m}$$

Mass

$$1 \text{ kg} = 1000 \text{ g} = 2.2046 \text{ lbm}$$
$$1 \text{ lbm} = 16 \text{ oz} = 0.45359 \text{ kg}$$
$$1 \text{ slug} = 32.174 \text{ lbm}$$

Temperature Values

$$(T/K) = (T/^{\circ}\text{R}) / 1.8$$
$$(T/K) = (T/^{\circ}\text{C}) + 273.15$$
$$(T/^{\circ}\text{C}) = [(T/^{\circ}\text{F}) - 32] / 1.8$$
$$(T/^{\circ}\text{R}) = 1.8(T/K)$$
$$(T/^{\circ}\text{R}) = (T/^{\circ}\text{F}) + 459.67$$
$$(T/^{\circ}\text{F}) = 1.8(T/^{\circ}\text{C}) + 32$$

Temperature Differences

$$(\Delta T/^{\circ}\text{R}) = 1.8(\Delta T / K)$$
$$(\Delta T/^{\circ}\text{R}) = (\Delta T/^{\circ}\text{F})$$
$$(\Delta T / K) = (\Delta T/^{\circ}\text{C})$$

Volume

$$1 \text{ m}^3 = 1000 \text{ L} = 10^6 \text{ cm}^3 = 10^6 \text{ mL}$$
$$= 35.315 \text{ ft}^3 = 264.17 \text{ gal}$$
$$1 \text{ ft}^3 = 1728 \text{ in}^3 = 7.4805 \text{ gal} = 0.028317 \text{ m}^3$$
$$1 \text{ gal} = 0.13368 \text{ ft}^3 = 0.0037854 \text{ m}^3$$

Volumetric Flow Rate

$$1 \text{ m}^3/\text{s} = 35.315 \text{ ft}^3/\text{s} = 264.17 \text{ gal/s}$$
$$1 \text{ ft}^3/\text{s} = 1.6990 \text{ m}^3/\text{min} = 7.4805 \text{ gal/s}$$
$$= 448.83 \text{ gal/min}$$

Force

$$1 \text{ N} = 1 \text{ kg}\cdot\text{m}/\text{s}^2 = 0.22481 \text{ lbf}$$
$$1 \text{ lbf} = 1 \text{ slug}\cdot\text{ft}/\text{s}^2 = 32.174 \text{ lbm}\cdot\text{ft}/\text{s}^2 = 4.4482 \text{ N}$$

Pressure

$$1 \text{ atm} = 101.325 \text{ kPa} = 1.01325 \text{ bar}$$
$$= 14.696 \text{ lbf}/\text{in}^2$$
$$1 \text{ bar} = 100 \text{ kPa} = 10^5 \text{ Pa}$$
$$1 \text{ Pa} = 1 \text{ N}/\text{m}^2 = 10^{-3} \text{ kPa}$$
$$1 \text{ lbf}/\text{in}^2 = 6.8947 \text{ kPa} = 6894.7 \text{ N}/\text{m}^2$$

[lbf/in² often abbreviated as “psi”]

Energy

$$1 \text{ J} = 1 \text{ N}\cdot\text{m}$$
$$1 \text{ kJ} = 1000 \text{ J} = 737.56 \text{ ft}\cdot\text{lbf} = 0.94782 \text{ Btu}$$
$$1 \text{ Btu} = 1.0551 \text{ kJ} = 778.17 \text{ ft}\cdot\text{lbf}$$
$$1 \text{ ft}\cdot\text{lbf} = 1.3558 \text{ J}$$

Energy Transfer Rate

$$1 \text{ kW} = 1 \text{ kJ}/\text{s} = 737.56 \text{ ft}\cdot\text{lbf}/\text{s}$$
$$= 1.3410 \text{ hp} = 0.94782 \text{ Btu}/\text{s}$$
$$1 \text{ Btu}/\text{s} = 1.0551 \text{ kW}$$
$$= 1.4149 \text{ hp} = 778.17 \text{ ft}\cdot\text{lbf}/\text{s}$$
$$1 \text{ hp} = 550 \text{ ft}\cdot\text{lbf}/\text{s} = 0.74571 \text{ kW} = 0.70679 \text{ Btu}/\text{s}$$

Specific Energy

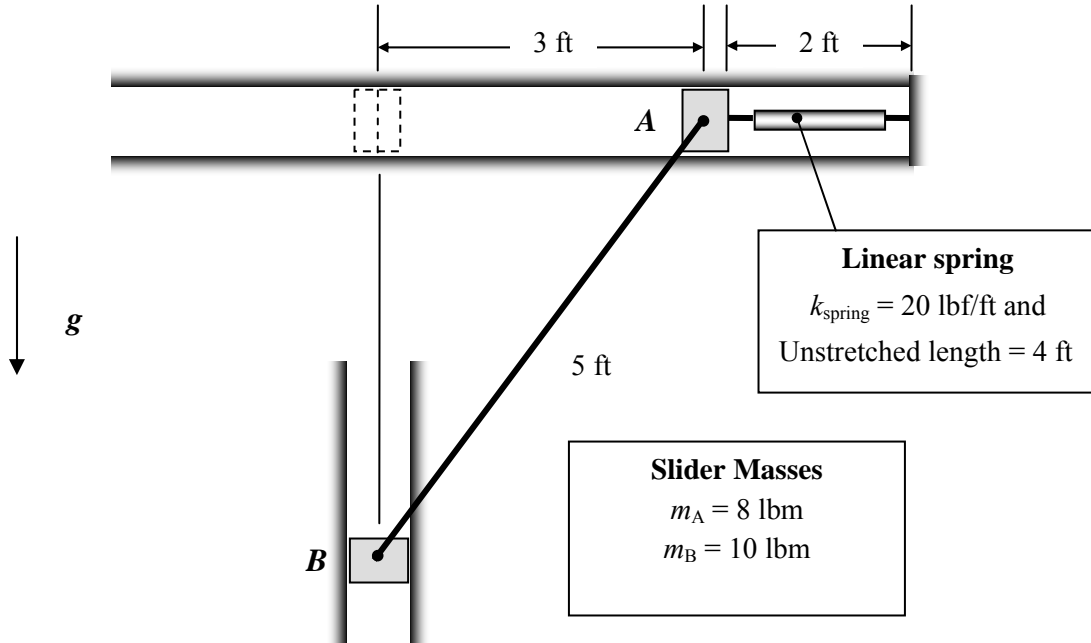
$$1 \text{ kJ}/\text{kg} = 1000 \text{ m}^2/\text{s}^2$$
$$1 \text{ Btu}/\text{lbm} = 25037 \text{ ft}^2/\text{s}^2$$
$$1 \text{ ft}\cdot\text{lbf}/\text{lbm} = 32.174 \text{ ft}^2/\text{s}^2$$

Problem 1 (30 points)

Two slider masses, A and B , are connected by a massless, rigid link AB , and slider A is attached to a linear spring as shown in the figure. The slider masses move freely in their guides. The rigid link that connects the sliders is attached by frictionless pin joints and rotates freely.

Initially, slider A is held stationary against a spring compressing it 2 ft as shown in the figure. When released, sliders A and B and the rigid link AB are free to move.

Determine the velocity of slider A as it crosses the centerline of the vertical slot, in ft/s (See dashed outline of slider A in figure.)



Problem 2 (35 points)

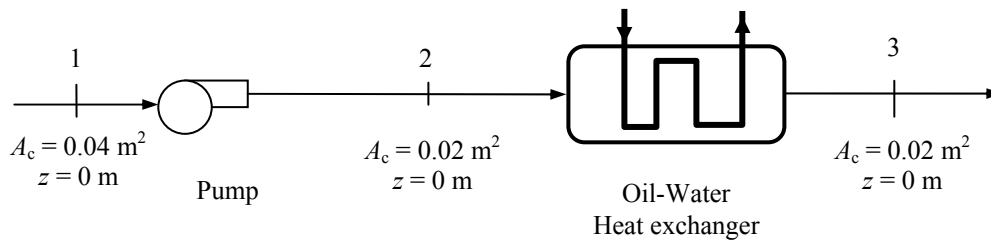
Liquid water enters a steady-state, adiabatic pump at 28°C and 100 kPa with a mass flow rate of 100 kg/s and leaves the pump at 28°C and 2 MPa . The inlet area of the pump is 0.04 m^2 and the outlet area of the pump is 0.02 m^2 . Changes in elevation are negligible.

Leaving the pump, the high-pressure water is heated to 200°C by hot oil in an oil-water heat exchanger. The water stream undergoes a negligible pressure drop as it flows through the heat exchanger and remains a liquid throughout the heating process. Inlet and outlet flow areas appear on the figure and changes in elevation are negligible.

Assume liquid water behaves like an incompressible substance with room-temperature specific heats using the following information: $\rho = 1000\text{ kg/m}^3$; $c = 4.18\text{ kJ/(kg}\cdot\text{K)}$.

Determine:

- (a) the power required to operate the pump, in kW.
- (b) the heat transfer rate of energy into the water in the heat exchanger, in kW.



Problem 3 (35 points)

The piston cylinder device, shown in the figure, models one cylinder of a large stationary power plant. The system contains air.

During an expansion process where pressure and volume are related by the expression $P \cdot V^2 = \text{Constant}$, the gas does 18.0 kN·m of work. Additional state information appears with the figure below:

Assume that air behaves like as an ideal gas with constant, room-temperature specific heats using the following information:

$$R = 0.2870 \text{ kJ}/(\text{kg K}); \quad M_{\text{air}} = 28.97 \text{ kg}/\text{kmol}; \quad c_p = 1.005 \text{ kJ}/(\text{kg K}); \quad c_v = 0.718 \text{ kJ}/(\text{kg K})$$

State 1: $T_1 = 2000 \text{ K}; \quad V_1 = ?? \quad P_1 = ??; \quad m_1 = 0.04181 \text{ kg}$

Process 1–2: Expansion process with $P \cdot V^2 = \text{Constant}$
18.0 kN·m work done by gas

State 2: $T_2 = ??; \quad V_2 = 0.05 \text{ m}^3; \quad P_2 = 120 \text{ kPa}$



Determine:

- (a) the *magnitude* and *direction* of the heat transfer for the process, in kJ.
- (b) the initial volume of the gas, V_1 in m^3 .

