

PHYSICS III
Dr. Joenathan – Winter 2000

HOMEWORK VI

Chapter 24; 5, 17, 26, 36, 39

24-5.

(a)

$$\begin{aligned}U_{123} &= \frac{1}{4\pi\epsilon_0} \left(\frac{q_1 q_2}{r_{12}} + \frac{q_1 q_3}{r_{13}} + \frac{q_2 q_3}{r_{23}} \right) \\&= \frac{1}{4\pi\epsilon_0} \left[\frac{(6.00 \times 10^{-6} \text{ C})(4.00 \times 10^{-6} \text{ C})}{1.50 \text{ m}} + \frac{(6.00 \times 10^{-6} \text{ C})(-3.00 \times 10^{-6} \text{ C})}{5.00 \text{ m}} + \frac{(4.00 \times 10^{-6} \text{ C})(-3.00 \times 10^{-6} \text{ C})}{3.50 \text{ m}} \right] \\&= 8.06 \times 10^{-2} \text{ J}\end{aligned}$$

(b)

$$\begin{aligned}U_{23} &= \frac{1}{4\pi\epsilon_0} \frac{q_2 q_3}{r_{23}} = \left(8.99 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} \right) \frac{(4.00 \times 10^{-6} \text{ C})(-3.00 \times 10^{-6} \text{ C})}{3.50 \text{ m}} \\&= -3.08 \times 10^{-2} \text{ J}\end{aligned}$$

$$\Delta U = U_{23} - U_{123} = -3.08 \times 10^{-2} \text{ J} - 8.06 \times 10^{-2} \text{ J} = -0.111 \text{ J}$$

$$\Delta K + \Delta U = 0$$

$$\Delta K = K_1 = -\Delta U = +0.111 \text{ J}$$

(c)

$$\begin{aligned}U_{13} &= \frac{1}{4\pi\epsilon_0} \frac{q_1 q_3}{r_{13}} = \left(8.99 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} \right) \frac{(6.00 \times 10^{-6} \text{ C})(-3.00 \times 10^{-6} \text{ C})}{5.00 \text{ m}} \\&= -3.24 \times 10^{-2} \text{ J}\end{aligned}$$

$$\Delta U = U_{13} - U_{123} = -3.24 \times 10^{-2} \text{ J} - 8.06 \times 10^{-2} \text{ J} = -0.113 \text{ J}$$

$$\Delta K = K_2 = -\Delta U = +0.113 \text{ J}$$

24-17.

(a)

$$\begin{aligned}\Delta V &= -\int_0^f \mathbf{E} \cdot d\mathbf{s} = -\mathbf{E} \cdot \Delta\mathbf{s}_{AB} - \mathbf{E} \cdot \Delta\mathbf{s}_{BC} \\ &= -(600. \text{ V/m } \hat{i} + 800. \text{ V/m } \hat{j}) \cdot (3.00\text{ m}) \hat{i} - (600. \text{ V/m } \hat{i} + 800. \text{ V/m } \hat{j}) \cdot (4.00\text{ m}) \hat{j} \\ &= -5.00 \times 10^3 \text{ V}\end{aligned}$$

(b)

$$\begin{aligned}\Delta V &= -\mathbf{E} \cdot \Delta\mathbf{s}_{AD} - \mathbf{E} \cdot \Delta\mathbf{s}_{DC} \\ &= -(600. \text{ V/m } \hat{i} + 800. \text{ V/m } \hat{j}) \cdot (4.00\text{ m}) \hat{j} - (600. \text{ V/m } \hat{i} + 800. \text{ V/m } \hat{j}) \cdot (3.00\text{ m}) \hat{i} \\ &= -5.00 \times 10^3 \text{ V}\end{aligned}$$

(c)

$$\begin{aligned}\Delta V &= -\mathbf{E} \cdot \Delta\mathbf{s}_{AC} = -\left(600. \frac{\text{ V}}{\text{ m}} \hat{i} + 800. \frac{\text{ V}}{\text{ m}} \hat{j}\right) \cdot (3.00\text{ m } \hat{i} + 4.00\text{ m } \hat{j}) \\ &= -5.00 \times 10^3 \text{ V}\end{aligned}$$

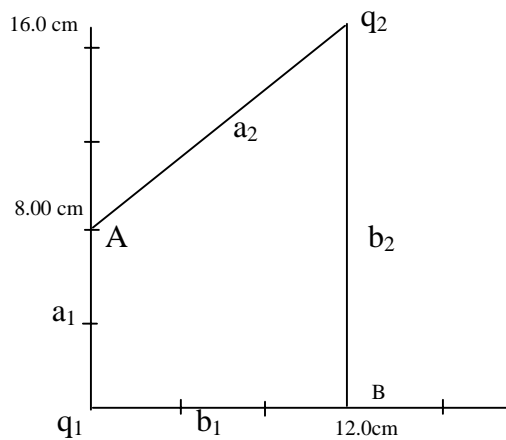
24-26.

(a)

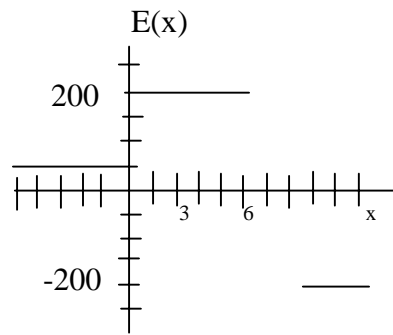
$$\Delta V_{AB} = V_B - V_A$$

$$\begin{aligned} V_A &= \frac{1}{4\pi\epsilon_0} \left(\frac{q_1}{a_1} + \frac{q_2}{a_2} \right) \\ &= \frac{1}{4\pi\epsilon_0} \left(\frac{24.0 \times 10^{-6} \text{ C}}{0.080 \text{ m}} + \frac{-36.0 \times 10^{-6} \text{ C}}{\sqrt{(0.120 \text{ m})^2 + (0.080 \text{ m})^2}} \right) \\ &= +4.53 \times 10^5 \text{ V} \end{aligned}$$

$$\begin{aligned} V_B &= \frac{1}{4\pi\epsilon_0} \left(\frac{q_1}{b_1} + \frac{q_2}{b_2} \right) \\ &= \frac{1}{4\pi\epsilon_0} \left(\frac{24.0 \times 10^{-6} \text{ C}}{0.120 \text{ m}} + \frac{-36.0 \times 10^{-6} \text{ C}}{0.160 \text{ m}} \right) \\ &= -2.25 \times 10^5 \text{ V} \\ \Delta V_{AB} &= -2.25 \times 10^5 \text{ V} - 4.53 \times 10^5 \text{ V} = -6.78 \times 10^5 \text{ V} \end{aligned}$$



24-36. (b) Between $x = 3$ and $x = 6$ m



24-39.

(a)

$$V_B = \frac{1}{4\pi\epsilon_0} \left[\frac{2Q}{y} - \frac{2Q}{\sqrt{a^2 + y^2}} \right]$$

$$= \frac{Q}{2\pi\epsilon_0} \left[\frac{1}{y} - \frac{1}{\sqrt{a^2 + y^2}} \right]$$

(b)

$$E_B = -\frac{\partial V_B}{\partial y} = \frac{Q}{2\pi\epsilon_0} \left[\frac{1}{y^2} - \frac{y}{(a^2 + y^2)^{3/2}} \right]$$