

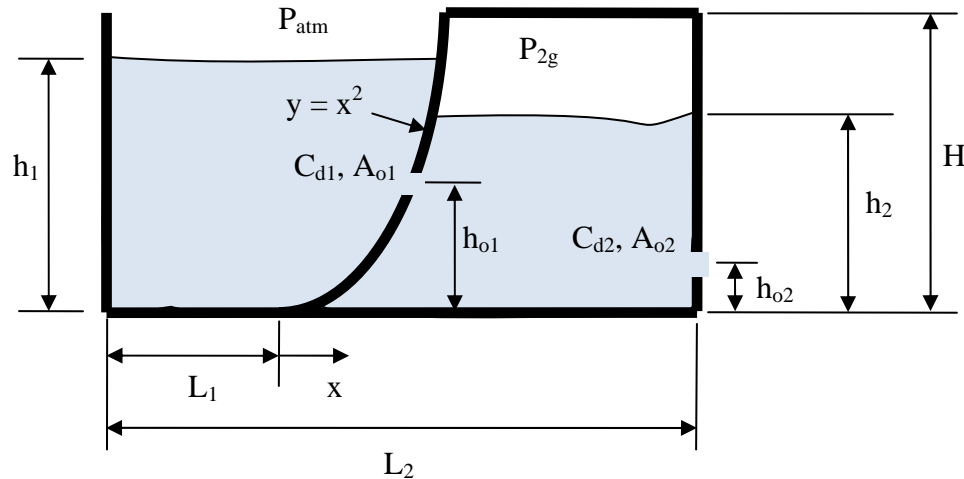
Name: \_\_\_\_\_ Section: \_\_\_\_\_

**ES 205**  
Examination II  
May 5, 2009

<b>Problem</b>	<b>Score</b>
1	/40
2	/40
3	/20
<b>Total</b>	/100

Show all work for credit  
AND  
Turn in your signed help sheet

Consider the two-chambered tank below. Both tanks have rectangular cross sections with width,  $w$ , out of the page. There are two orifices, one between the tanks along the parabolic divider. The other orifice is out of the straight side of the right-hand chamber. Set up the differential equations for the heights of fluid in the two tanks. **DO NOT ATTEMPT TO SOLVE THESE EQUATIONS** but clearly number you equations and list your unknowns. Assume all the tank dimensions, orifice parameters, and fluid properties are known. Note that  $P_{2g}$  is a constant and known gage pressure.



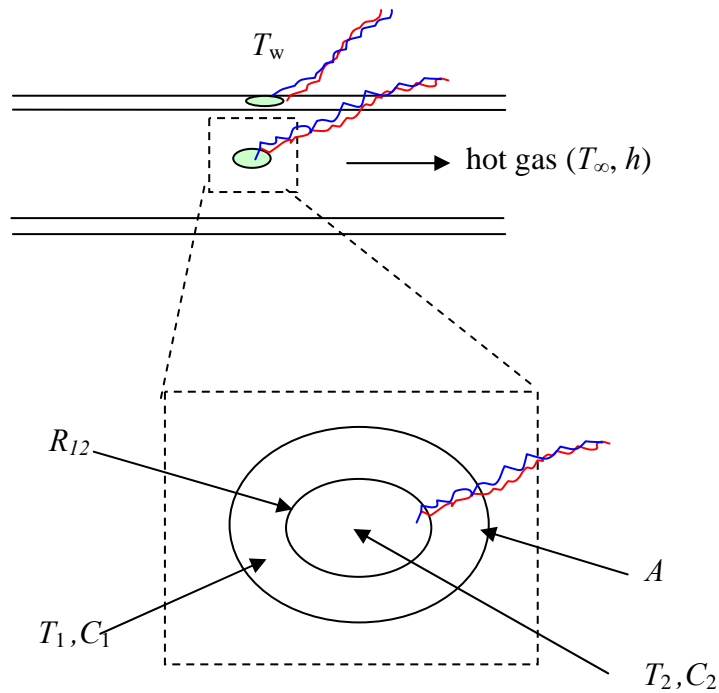
Unknowns: \_\_\_\_\_

Name: \_\_\_\_\_

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Hot gas flows in a duct instrumented with two thermocouples. A shielded thermocouple is placed in the gas stream and consists of two volumes having different thermal capacitances  $C_1$  and  $C_2$ . Heat is transferred between the two volumes at a rate given by  $\dot{Q} = \Delta T/R_{12}$ , where  $R_{12}$  represents the thermal resistance of the interface between the two layers and  $\Delta T$  is the temperature difference between the two volumes. An expanded view of this thermocouple is shown in the dotted lines. The thermocouple mounted in the wall is not sheathed.

- (a) Determine the governing differential equations for the temperature  $T_1$  and  $T_2$ . Assume  $T_w$ ,  $\varepsilon$ ,  $\sigma$ ,  $T_\infty$ ,  $h$ ,  $A$ , and  $R_{12}$  are known.
- (b) Assume that at steady state the following is known: The thermocouple embedded in the duct wall indicates a temperature  $T_w = 700^\circ\text{F}$ . The thermocouple immersed in the center of the hot gas stream has emissivity  $\varepsilon = 0.6$ , a convection coefficient of  $30 \text{ btu}/(\text{hr}\cdot\text{ft}^2\cdot\text{F})$ , and indicates a temperature  $T_2 = 900^\circ\text{F}$ . The Stefan-Boltzman constant in USCS units is  $\sigma = 0.1714 \times 10^{-8} \text{ btu}/(\text{hr}\cdot\text{ft}^2\cdot\text{R}^4)$ . Determine the actual temperature of the gas.



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ES 205 Examination II

**Problem 3**

20 pts.

**Problem 3.1** (3 pts.)

A second order system has a damping ratio of 0.1, a natural frequency of 4 rad/s and is forced with  $f(t) = 8 \sin 8t$ . Determine the phase difference, in radians, between the input and the steady-state output.

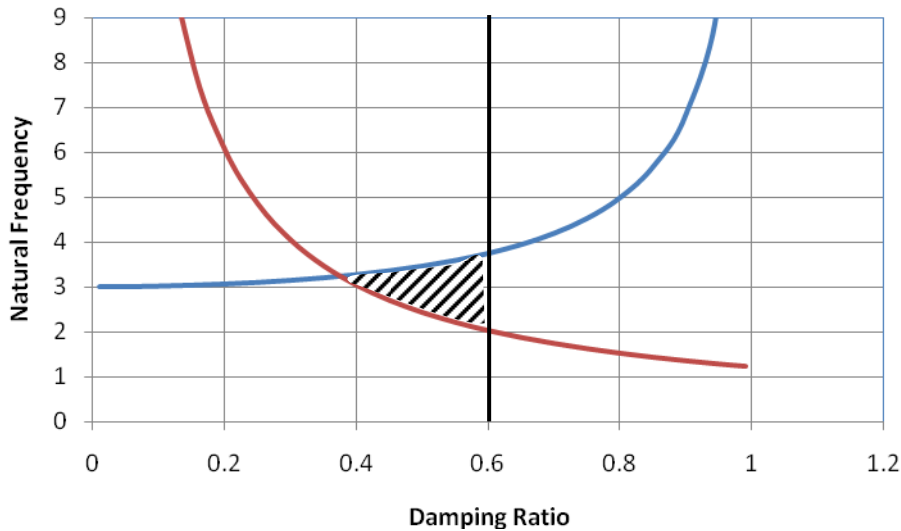
**Problem 3.2** (2 pts.)

When calculating the log-incomplete response why do you exclude data past 4 time constants?

**Problem 3.3** (6 pts.)

A design space for a second order system subject to a step input is shown below. Cross hatching shows the acceptable region. Label the curve for

- Percent overshoot
- Settling time
- Peak time

**Problem 3.4** (9 pts.)

Determine the performance specifications for Problem 3.3 for percent overshoot, settling time and peak time.