

Name \_\_\_\_\_ Section \_\_\_\_\_

**EM406**  
Examination I  
September 23, 2005

Problem	Score
1	/10
2	/40
3	/35
4	/15
Total	/100

Show all work for credit  
AND  
Turn in your signed help sheet

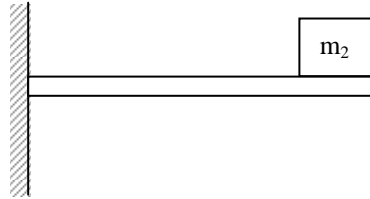
Name \_\_\_\_\_  
EM406 Examination I

**Problem 1**

10 pts  
September 23, 2005

**Problem 1**

Assuming the mass of the beam is 0.6 kg and it has a natural frequency of 100 rad/s. What lumped mass,  $m_2$ , needs to be attached to the end to reduce the natural frequency to 80 rad/s?



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**Problem 2**

40 pts  
September 21, 2004

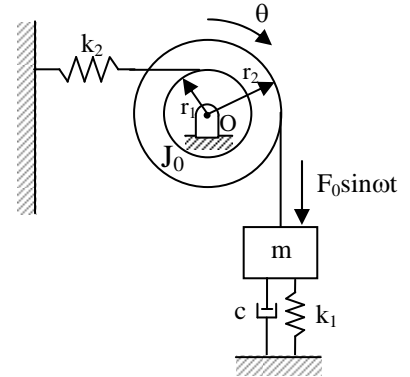
Find

- the equation of motion for the system shown in terms of  $\theta$ .
- the natural frequency and damping ratio in terms of the labeled system parameters

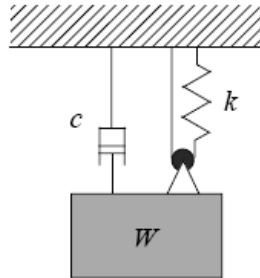
Assume the equation of motion with numbers is:

$$2\ddot{\theta} + 10\dot{\theta} + 200\theta = 5\sin\omega t .$$

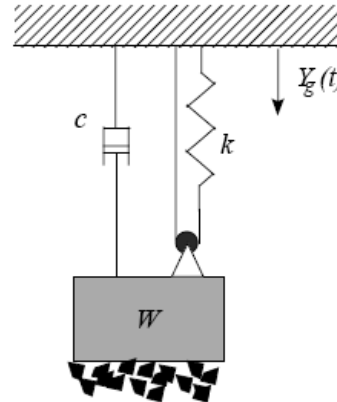
- Determine the steady state response for  $\omega = 12$  rad/s.
- Using your answer from part c) determine the maximum pretension required in the rope so that it does not go slack.  
Assume  $J_0 = 1$  kg-m<sup>2</sup>,  $k_2 = 5000$  N/m,  $r_1 = 0.1$  m. (5 pts)



An electromagnet weighing  $W = 400$  lbs is holding up  $W_2 = 200$  lbs of scrap iron. At time  $t = 0$ , the magnet is turned off and the scrap iron is dropped. Simultaneously, the support for the system starts moving according to  $Y_g(t) = 2 \sin \omega t$  inches, where positive is indicated in the figure below.



(a) Electromagnet in static equilibrium under own weight



(b) Electromagnet in static equilibrium under combined self-weight and scrap iron

- Determine the equation of motion for the system after the magnet is turned off. Be sure to clearly label your variables and directions of positive motion, as well as your reference point from which you are measuring. Leave in symbolic form.
- Determine the initial conditions for the dynamic motion after the iron is dropped if  $k = 100$  lb/in. (5 pts)
- What is the magnitude steady state response given  $\zeta = 0.05$ ,  $k = 100$  lb/in and the forcing frequency is three times the natural frequency of the system.
- Discuss how you would determine the total response of the system, but do not actually do any calculations or algebra. (5 pts)

A laboratory notebook for a secret project was burned in a fire by terrorists. The only two scraps of paper remaining are shown below and you know that they refer to the same vibrating system. Determine the natural frequency and damping ratio for the system. To save time, set up the equations but do not solve.

