



LECTURE 3 - 1

Feedback (Closed-loop) Control



Quote of the Week

“A common mistake people make when trying to design something completely foolproof is to underestimate the ingenuity of complete fools.”



ANNOUNCEMENTS

- Lab 3 - Wall Following (PD Control) is due on **Thursday, 3/25/10**
- The lab memo and code is due on Angel by midnight on **Thursday, 3/25/10**
- Quiz 5 on Feedback Control on **Tuesday, 3/23/10**



OBJECTIVES

Upon completion of this lecture the student should be able to:

- Define closed-loop and open-loop control
- Describe the different types of feedback control
- Compare and contrast the system responses based upon the types of control
- Use feedback control to create basic behaviors for a mobile robot



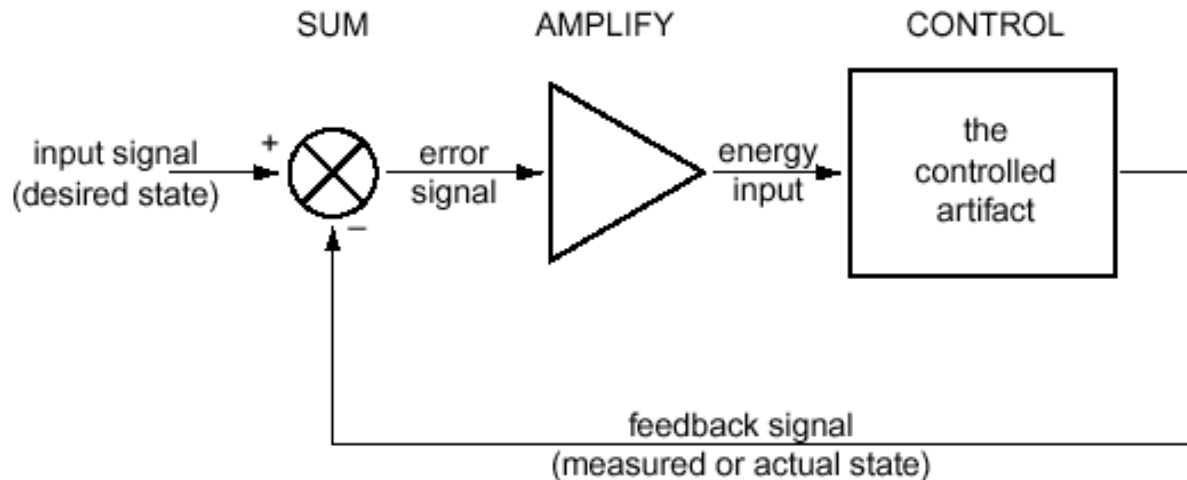
FEEDBACK CONTROL

- **Feedback Control** is a means of getting a robot to achieve and maintain a desired state.
- The desired state (goal state) is the **set point** and it is achieved by continuously comparing its current state with its desired state.
- The difference between current and desired state is the **error**
- The goal of any control system is to minimize the error



FEEDBACK CONTROL

Feedback (closed loop) control is when a system achieves and maintains a *desired state* by continuously comparing its current and desired states, then adjusting the current state to minimize the difference





ERROR AND OVERSHOOT

- *Error* is the difference in the current state and desired state of the system
 - The controller has to minimize the error at all times
- *Zero/non-zero error:*
 - Tells whether there is an error or not
 - The least information we could have
- *Direction of error:*
 - Which way to go to minimize the error
- *Magnitude of error:*
 - The distance to the goal state
- *Overshoot*
 - Is when the robot goes beyond its set point (position) or changes direction before stabilizing on it
- Control is much easier if we know both magnitude and direction



GAINS AND OSCILLATIONS

- Incorrect controller gains will cause the system to undershoot or overshoot the desired state and cause **oscillations**
- Gain values determine if the system will:
 - keep oscillating
 - increase in oscillations
 - stabilize
- **Damping** is the process of systematically decreasing oscillations
- A system is **properly damped** if it does not oscillate out of control or has no oscillations at all
- The robot **oscillates** around the set point. In general, the behavior of a feedback system oscillates around the desired set point



WALL FOLLOWING

- Use feedback to design a wall following robot
- Infrared and/or sonar will provide distance to the wall (analog)
- The *set point* will be distance to the wall
- The *error* will be the difference between the set point and current distance to wall
- Control algorithm:
 - If distance-to-wall is correct, then keep moving
 - else if distance-to-wall is too large, then turn toward the wall
 - else if distance-to-wall is too small, then turn away from the wall
- With this algorithm, the robot will keep moving and wiggling back and forth as it moves. The amount of wiggling is determined by how often the error is computed and how much correction (turn) is made each time.



HOW TO DECREASE OSCILLATIONS?

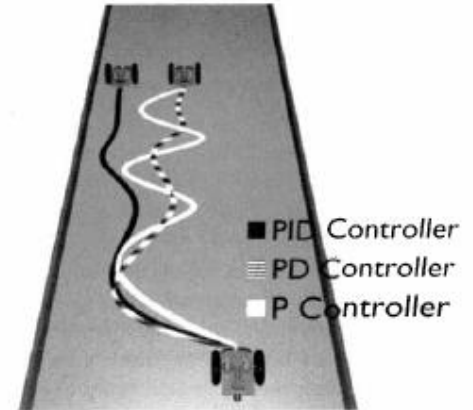
- Compute the error often so the robot *turns more* often
- Adjust the turn angle so that the robot turns by *smaller angles*
- Use a *range of distances* to define the robot's goal
- Determining these values depends on specific robot parameters
 - Robot's speed of movement
 - Range of the sensors
 - Sampling rate of the sensor



TYPES OF FEEDBACK CONTROL

There are 3 types of
basic feedback controllers

- P: proportional control
- PD: proportional derivative control
- PID: proportional integral derivative control





PROPORTIONAL (P) CONTROL

- The response of the system is proportional to the amount of the error
- The output of the controller is proportional to the input (speed or velocity error):

$$\text{output} = K_p * \text{error input}$$

- K_p is a proportionality constant (gain)
- The controller generates a stronger response the farther away the system is from the goal state
- The robot will turn sharply toward the wall if it is really far from it
- The robot will turn gently toward the wall if it is slightly away from it
- As the proportional gain becomes larger it will introduce **overshoot** and **oscillations**

PROPORTIONAL CONTROL: WALL FOLLOWING

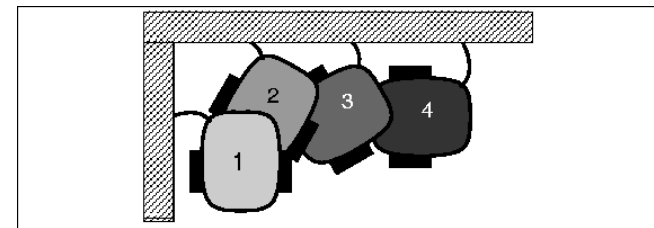
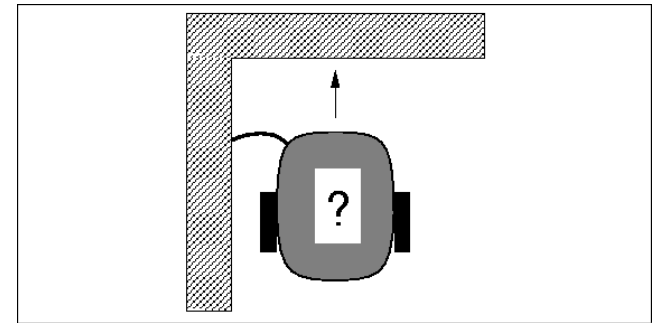


- The distance to wall parameter would be used to determine the angle and distance and/or speed that the robot moves
- The larger the error, the larger the movement
- The smaller the error, the smaller the movement
- The parameters that determine the magnitude of the system's response are called *gains*
- Determining the right gain requires *trial and error*, testing and calibrating the system
- If the system is well understood, the gains can be computed mathematically



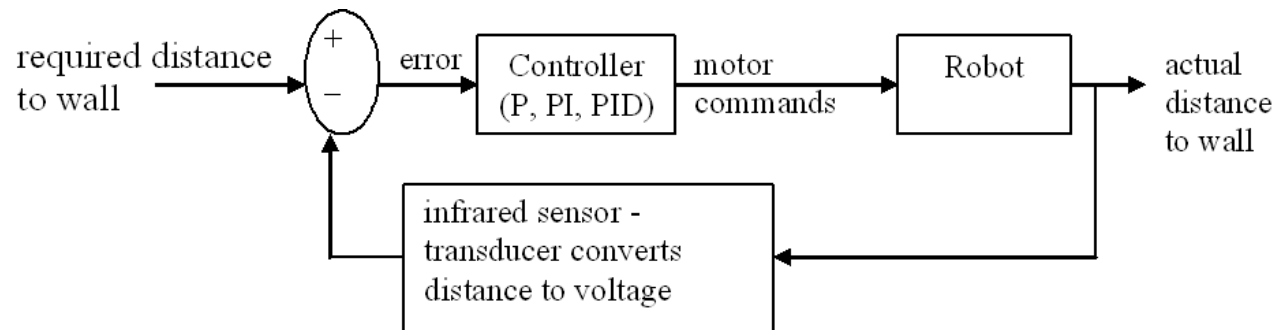
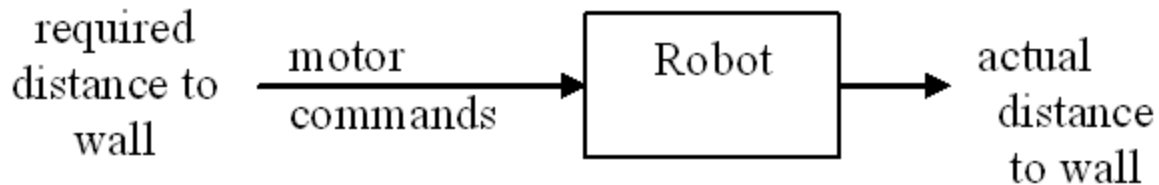
WALL FOLLOWING: CORNERS

- Negotiating a corner
 - Make little turns, drive straight ahead, detect the wall, back up, repeat
 - The disadvantage is that this method is time consuming and produces jerky movements
- Alternative (proportional control):
 - Execute a turn command that was timed to accomplish a ninety degree rotation based upon distance to the wall
 - Works reliably only when the robot is very predictable (battery strength, traction on the surface, and friction)





OPEN LOOP VERSUS CLOSED LOOP CONTROL





PROPORTIONAL CONTROL: ROBOT POSITION

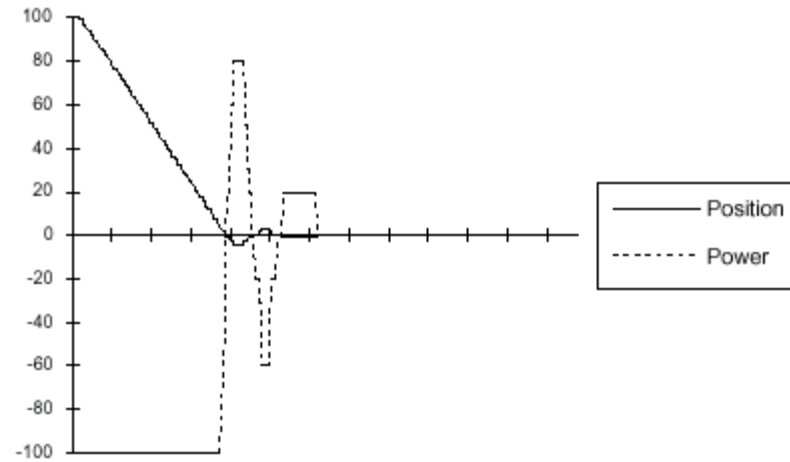
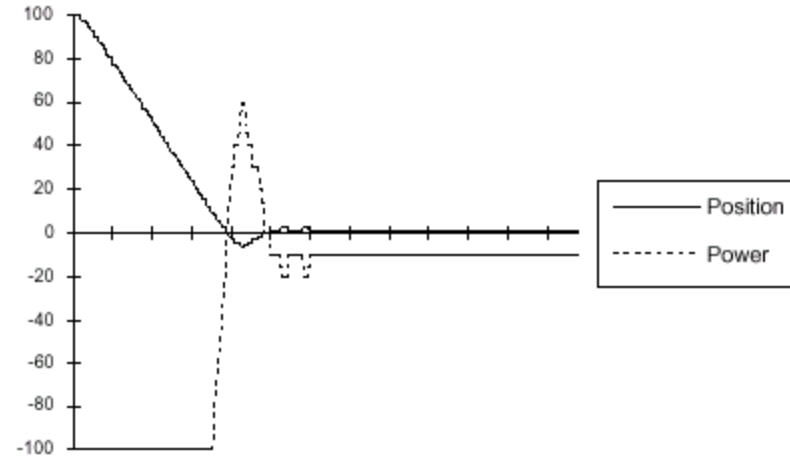
- What if the robot is 100 cm from home and your goal is to move the robot forward to the home position.
- The **set point** is position = 0 cm (home)
- The **error** is (set point – position = 0 - position)
- A simple Proportional controller has:
 - Motor Power Command = set point – position = 0 - position
- Initially, the error is -100
 - The motor turns on full speed
 - As it starts going, the error becomes progressively smaller
- Halfway, at position = 50 cm, the error is -50
 - at that point the motor goes at 50% of full power
- When it arrives at the intended position of 100, the error is zero
 - the motor is off

POSITION CONTROL



- $K_p=10$:
 - System overshoots the zero point, and had to turn around
 - *Offset Error*: System did not stabilize at the goal
 - Power command too small to activate the motor
 - The response is *critically damped*
- $K_p=20$:
 - Offset error is solved
 - Oscillation: the system overshoots the goal
 - The response is *slightly underdamped*

$$power = K_p * (0 - position)$$

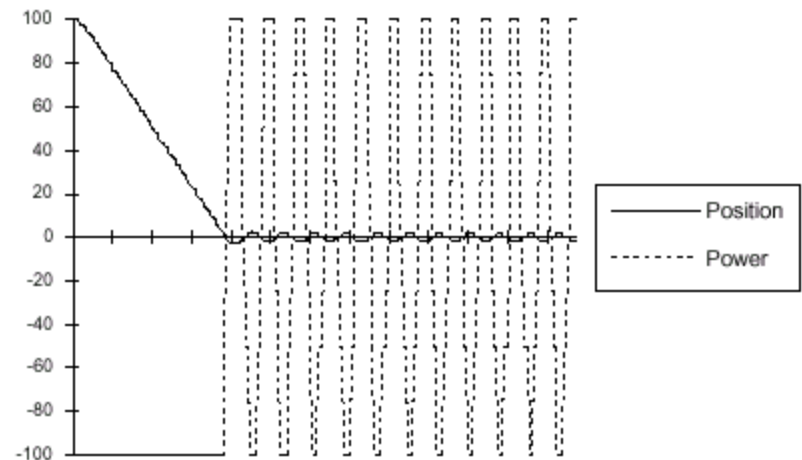
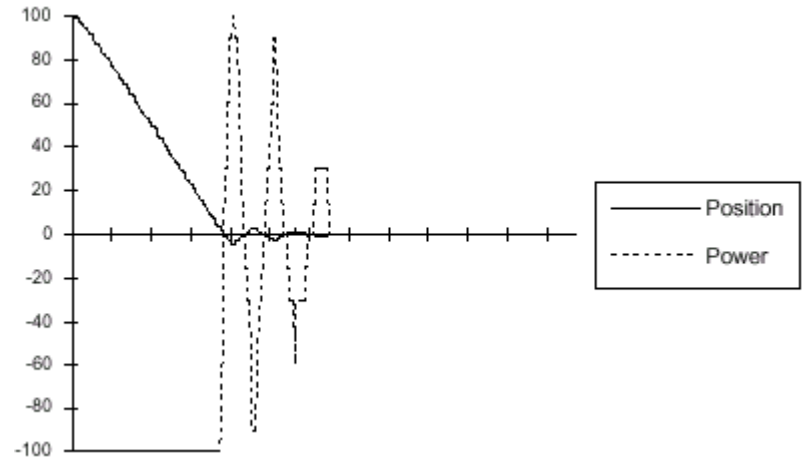




POSITION CONTROL

- $K_p=30$:
 - Oscillation problem is more pronounced;
 - The response is *underdamped*
- $K_p=50$:
 - Oscillation behavior has taken over
 - System cannot stabilize at the set point
 - A small error generates a power command that moves the system across the set point
 - The system is *undamped*

$$power = K_p * (0 - position)$$





VELOCITY CONTROL

- Setting gains is difficult, and simply increasing the *proportional gain* does not remove oscillations
- The system needs to be controlled differently when it is close to the desired state than when it is far from it
- In proportional control, the *momentum* of the correction carries the system beyond the desired state, and causes oscillations

$$\textit{Momentum} = \textit{mass} * \textit{velocity}$$



DERIVATIVE (D) CONTROL

- Solution: correct the momentum as the system approaches the desired state
 - Subtract an amount proportional to the velocity
- As the system nears the desired state, we subtract an amount proportional to the velocity:

$$- (\textit{gain} * \textit{velocity})$$

Derivative term (velocity is the derivative of position)

- A controller that has a derivative term is called a *derivative (D) controller*



DERIVATIVE CONTROL

- A derivative controller has an output proportional to the derivative of its error input:

$$output = K_d * d (error input)/dt$$

- K_d is a proportionality constant
- The intuition behind derivative control:
 - Controller corrects for the momentum as it approaches the desired state
- *Wall Following*: Slow down the robot and decrease the turning angle while getting closer to the desired state
- *Position Control*: Decrease the motor power while getting closer to the desired state



PROPORTIONAL-DERIVATIVE (PD) CONTROL

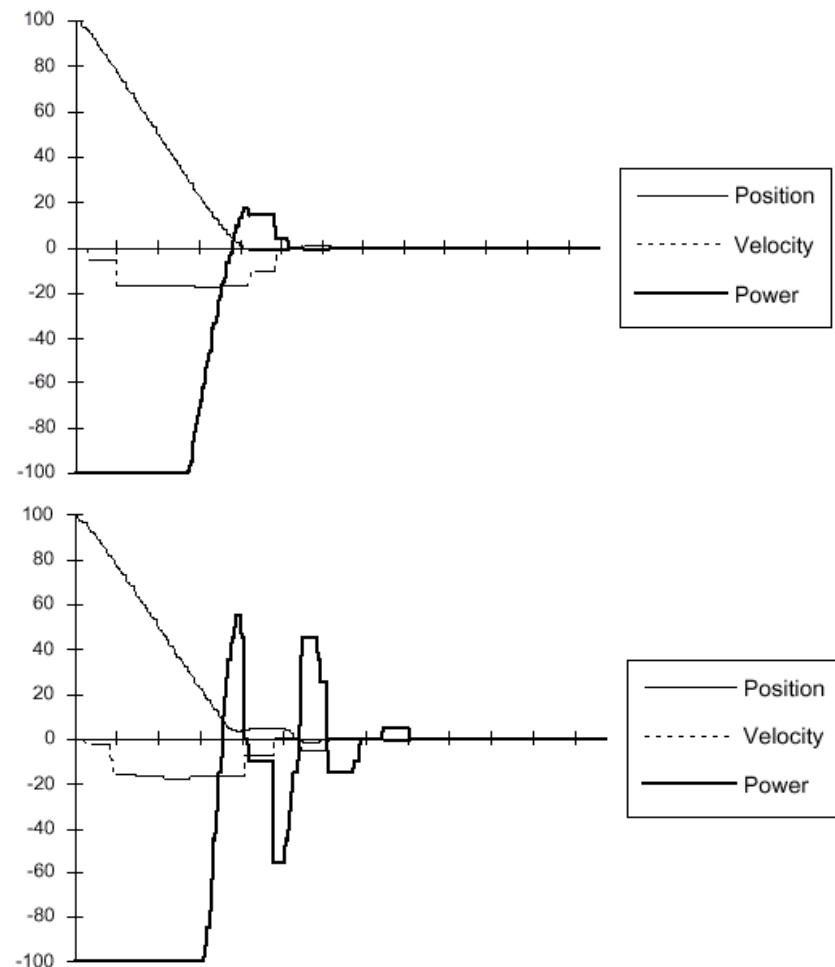
- Proportional-derivative control is a
 - Combination (sum) of proportional and derivative terms
$$\text{output} = K_p * (\text{error input}) + K_d * d(\text{error input})/dt$$
- **PD Control** is used extensively in industrial process control
 - Combination of varying the power input when the system is far away from the set point, and correcting for the momentum of the system as it approaches the set point is quite effective
- **PD Control** improves the transient response of the robot to slow the controller momentum, typically with negative feedback
- **PD Control** is sometimes referred to as **rate control** because it is based upon the rate of change of the error
- In a wall following algorithm this would reduce the sharpness of the turn when the rate of change reaches some threshold



PROPORTIONAL-DERIVATIVE CONTROL

- $K_p = 4, K_d = 1$:
 - Overshoot is minimized, no oscillatory behavior at all
- $K_p = 10, K_d = 5$:
 - Unstable; K_d is too large
 - Position graph: controller “puts on the brakes” too hard and the system stops moving before the destination set point
 - When the velocity hits zero, the proportional gain kicks in again and the system corrects

$$power = K_p * (0 - position) + K_d * velocity$$





INTEGRAL (I) CONTROL

- Errors accumulate as the robot is running for a long time
- The system keeps track of its own repeatable, fixed errors called *steady state errors*
- How can we solve the problem?
 - Sum up the errors and compensate for them when they become significantly large
- The control system can be improved by introducing an *integral term*
$$output = K_i * \int (error\ input) dt$$
- K_i = proportionality constant
- Intuition:
 - System keeps track of its repeatable, steady state errors
 - These errors are integrated (summed up) over time
 - When they reach a threshold, the system compensates for them



PROPORTIONAL-INTEGRAL (PI) CONTROL

- Proportional-integral control is a
 - Combination (sum) of proportional and derivative terms

$$\text{output} = K_p * (\text{error input}) + K_i * \int (\text{error input}) dt$$

- **PI Control** improves the steady state response and would correct for steady state or offset error
- **PI Control** is sometimes also referred to as **reset control** because it resets the steady state error to 0
- In a wall following algorithm, after the sum of the distance error reaches some threshold then adjust the turn angle



PROPORTIONAL INTEGRAL DERIVATIVE (PID) CONTROL

- PID control is a sum of all three of the basic controls

$$\text{output} = K_p * (\text{error input}) + K_i * \int (\text{error input})dt + K_d * d(\text{error input})/dt$$

- This controller improves both the steady-state and transient response of the robot's wall following algorithm



DETERMINING CONTROLLER GAINS

- How do we determine the controller gain?
- Empirically (trial and error):
 - requires that the system be tested extensively
- Analytically (mathematics):
 - require that the system be well understood and characterized mathematically (a model)
- Automatically
 - by trying different values at run-time

FEEDBACK CONTROL AND CONTROL THEORY



- *Feedback control* is the lower level of control theory for controlling wheels or continuously moving actuators
- However, for achieving higher level goals
 - navigation
 - coordination
 - interaction
 - collaboration
 - human-robot interaction
- It is necessary to use techniques from the field of *artificial intelligence (control architectures)*