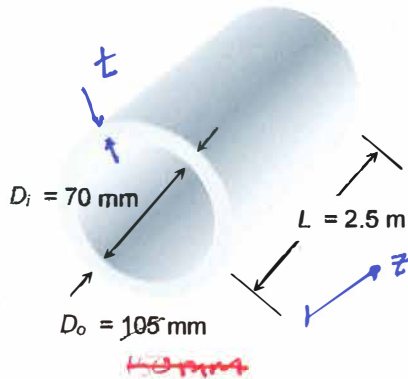


Example

A cast iron pipe has inside and outside diameters of 70 mm and ~~150~~¹⁰⁵ mm, respectively. The length of the pipe is 2.5 m and the coefficient of thermal expansion is $\alpha = 12.1 \times 10^{-6}/^{\circ}\text{C}$. For a 70°C increase in temperature, find the new pipe dimensions.



$$\epsilon_{T,z} = \alpha \Delta T = \frac{\delta_L}{L}$$

$$= 12.1 \times 10^{-6} \cdot (70^{\circ}\text{C}) = 0.000847$$

$$\Rightarrow \delta_L = \epsilon_{T,z} \cdot L = (0.000847) (2.5 \text{ m}) = 0.00212 \text{ m}$$

$$L_2 = L + \delta_L = \boxed{2.002 \text{ m}}$$

$$\epsilon_{T,D_o} = \alpha \Delta T = \dots = 0.00847$$

$$= \frac{\delta_{D_o}}{D_o}$$

$$\delta_{D_o} = \epsilon_{T,D_o} D_o = 0.00847 (105 \text{ mm}) = 0.889 \text{ mm}$$

$$D_{o,2} = D_o + \delta_{D_o} = 105 + 0.889 = \boxed{105.89 \text{ mm}}$$

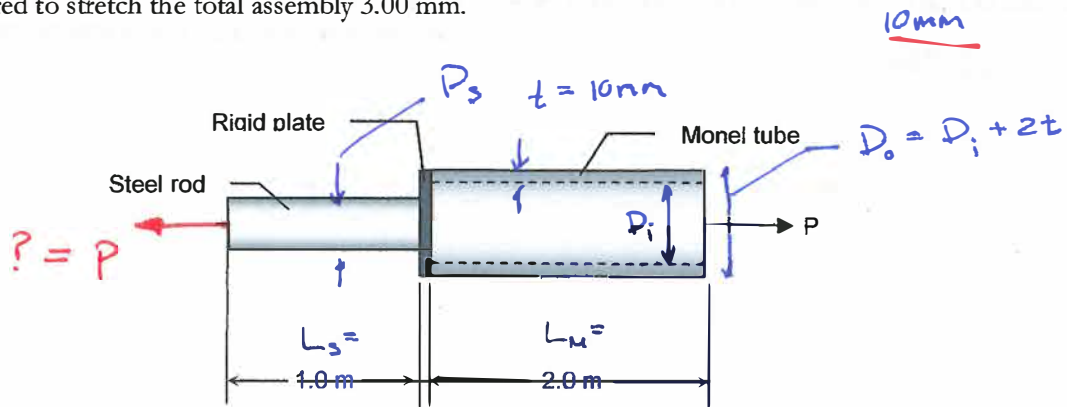
$$\dots \delta_{D_i} = \epsilon_T D_i = 0.00847 (70 \text{ mm}) = 0.593 \text{ mm}$$

$$D_{i,2} = D_i + \delta_{D_i} = \boxed{70.59 \text{ mm}}$$

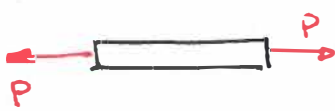
WOULD $\epsilon_{T,t} = \frac{\delta_t}{t} = \alpha \Delta T$ WORK? YES!!

Example

A steel ($E = 200 \text{ GPa}$) rod with diameter 30 mm and length 1.0 m is attached to a 2.0-m long Monel ($E = 180 \text{ GPa}$) tube via a rigid plate. The Monel tube has internal diameter of 40 mm and a wall thickness of 10 mm. Determine the total axial load required to stretch the total assembly 3.00 mm.



F.B.D. STEEL



$$\sigma_s = \frac{P}{A_s}$$

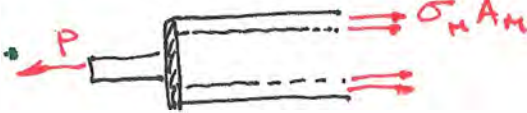
HOOKES' LAW

$$\sigma_s = E_s \epsilon_s$$

$$\frac{P}{A_s} = E_s \frac{\delta_s}{L_s}$$

$$\delta_s = \frac{P L_s}{A_s E_s} \quad \left(= \frac{P}{K} \right)$$

F.B.D. MONEL



$$\sigma_M = E_M \epsilon_M$$

$$\frac{P}{A_M} = E_M \frac{\delta_M}{L_M}$$

$$\delta_M = \frac{P L_M}{A_M E_M}$$

↑↑ FORMULA SHOWS UP A LOT.
↓↓

$$\delta = \delta_s + \delta_M = 0.003 \text{ m} = \frac{P L_s}{A_s E_s} + \frac{P L_M}{A_M E_M}$$

$$P = \frac{\delta}{\frac{L_s}{A_s E_s} + \frac{L_M}{A_M E_M}} = \frac{\delta}{\frac{L_s}{\frac{\pi D_s^2}{4} E_s} + \frac{L_M}{\frac{\pi (D_o^2 - D_i^2)}{4} E_M}}$$

$$= \frac{\delta}{\frac{L_s}{\frac{\pi D_s^2}{4} E_s} + \frac{L_M}{\frac{\pi (D_i + 2t)^2 - D_i^2}{4} E_M}} = \frac{0.003 \text{ m}}{\frac{1.0 \text{ m}}{\frac{\pi (0.030)^2 \text{ m}^2 \cdot 200 \times 10^9 \frac{\text{N}}{\text{m}^2}}{4}} + \dots}$$

...

$$= 2.12 \times 10^5 \text{ N}$$