

MA 439 - Math of Image Processing  
Worksheet #3  
Professor Broughton

Name: \_\_\_\_\_

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Do not hand in

1. Write out  $F_4$  the  $4 \times 4$  Fourier transform matrix.
2. Let  $X$  be the signal  $X = [0, 1, 2, 1]$  compute  $\hat{X}$ .
3. Plot  $X$  and its periodic extension to the sample point 1. What properties does  $X$  have. What properties does  $\hat{X}$  have.

4. Repeat 2 and 3 for  $X = [0, -2, 0, 2]$ .

5. Compute  $F_4^* F_4$  and use this information to determine  $F_4^{-1}$ .

6. What matrix formula should one use to compute  $X$  from  $\hat{X}$ . Carry out the computation for the  $X$  given in 2.

For the remaining questions let  $X$  be the signal obtained by sampling  $f(t) = 2 + 0.5 \cos(10\pi t) - .075 \sin(24\pi t)$  at the points  $n/N$  for  $n = 0, \dots, N - 1$ .

7. Let  $N = 128$ . Write out  $X$  as a sum of  $E_k$  's where  $0 \leq k \leq N - 1$ .

$$X =$$

8. let  $X$  and  $N$  be as in 7. Compute all the nonzero  $\widehat{X}(k)$  for  $0 \leq k \leq N - 1$ . Use the dot product relations.

9. Now let  $N = 16$ , and let  $X$  be as previously defined. Write out  $X$  as a sum of  $E_k$  's where  $-\frac{N}{2} < k \leq \frac{N}{2}$ .

$$X =$$

10. Let  $X$  and  $N$  be as in 9. Compute all the nonzero  $\widehat{X}(k)$  for  $-\frac{N}{2} < k \leq \frac{N}{2}$ . Use the dot product relations.