

# **ECE-420**

## **Exam 1**

### **Fall 2013**

**Calculators can only be used for simple calculations. Solving integrals, differential equations, systems of equations, etc. does not count as a simple calculation.**

**You must show your work to receive credit.**

**Problem 1**      \_\_\_\_\_/25

**Problem 2**      \_\_\_\_\_/25

**Problem 3**      \_\_\_\_\_/10

**Problem 4**      \_\_\_\_\_/20

**Problem 5**      \_\_\_\_\_/20

**Total**      \_\_\_\_\_

1) For impulse response  $h(n) = \left(\frac{1}{2}\right)^{n-1} u(n-3)$  and input  $x(n) = \left(\frac{1}{6}\right)^{n-3} u(n-1)$

a) Determine  $H(z)$

b) Determine  $X(z)$

c) Assume  $Y(z) = z^{-3}G(z)$ , determine  $g(n)$  and then  $y(n)$

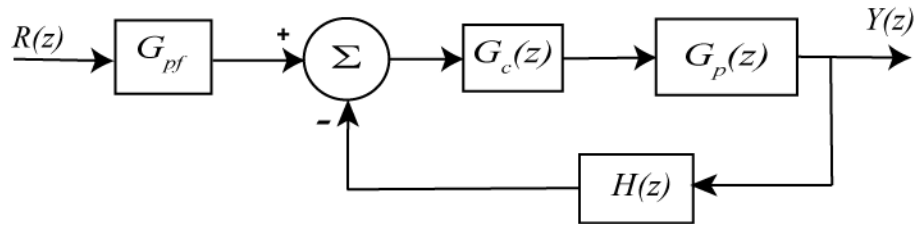
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- 2) Consider the difference equation  $y(n+1) + 2y(n) = x(n)$  with the initial condition  $y(0) = 1$
- Assuming the input is a unit step function, determine the zero input response (ZIR) and the zero state response (ZSR)
  - Determine an expression for the system output
  - Use the difference equation to compute  $y(0)$ ,  $y(1)$ ,  $y(2)$  and  $y(3)$
  - Compare the values from part **c** with the values you compute from your answer to part **b**

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- 3) Use long division to determine the first three nonzero terms in the impulse response for the following transfer function  $H(z) = \frac{z}{z^2 + 3z - 1}$

4) Assume the following feedback configuration



If  $H(z) = z^{-1}$ ,  $G_c(z) = \frac{c(z+a)}{z+b}$ ,  $G_p(z) = \frac{2}{z+1}$  determine the parameters  $a$ ,  $b$ , and  $c$  so all of the closed loop poles are at 0.5.

Hint:  $(z - 0.5)^3 = z^3 - 1.5z^2 + 0.75z - 0.125$

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- 5) For impulse response  $h(n) = 2^n u(2 - n)$  and input  $x(n) = \left(\frac{1}{3}\right)^{n-1} u(n-2)$ , the system output can be written as  $A(n)u(n-4) + B(n)u(3-n)$ . Determine an expression for  $A(n)$  **or**  $B(n)$ . You do not need to simplify your expression but you must evaluate all sums.

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