

ECE-320 Linear Control Systems

Winter 2013, Exam 2

You may only use your computer on the sisotool problem.

You may only use Matlab on this problem.

Problem 1 _____/25

Problem 2 _____/25

Problem 3-9 _____/21

Problem 10 _____/29

Total _____/100

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1) (25 points) For impulse response $h(n) = \left(\frac{1}{2}\right)^{n-1} u(n+1)$ and input $x(n) = \left(\frac{1}{4}\right)^{n+1} u(n-1)$, determine

the system output by evaluating the convolution sum $y(n) = \sum_{k=-\infty}^{\infty} h(n-k)x(k)$

Note: you do not have to simplify your answer, but you must remove all sums and include a unit step function of some sort.

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2) (25 points) For impulse response $h(n) = \left(\frac{1}{2}\right)^{n-1} u(n)$ and input $x(n) = \left(\frac{1}{3}\right)^{n+1} u(n-1)$,

a) determine the z-transform of $h(n)$, $H(z)$

b) determine the z-transform of $x(n)$, $X(z)$

c) determine $y(n)$

Hint: Assume $Y(z) = z^{-2}G(z)$, determine $g(n)$ and then $y(n)$

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Problem 3-9, 3 points each

3) Is the following system *controllable*? $G(s) = \frac{G_{pf}}{(s - k_1 k_2)^2}$

a) Yes b) No c) impossible to determine

4) Is the following system *controllable*? $G(s) = \frac{8G_{pf}}{s^2 + 12s + (k_1 + k_2 + 20)}$

a) Yes b) No c) impossible to determine

5) Is the following system *controllable*? $G(s) = \frac{G_{pf}}{s^2 + (k_2 + k_1 - 1)s + (k_2 + 2)}$

a) Yes b) No c) impossible to determine

6) Consider a plant that is unstable but is a controllable system. Is it possible to use state variable feedback to make this system stable?

a) Yes b) No

7) Is it possible for a system with state variable feedback to change the zeros of the plant (other than by pole-zero cancellation) ?

a) Yes b) No

8) Is it possible for a system with state variable feedback to introduce zeros into the closed loop system?

a) Yes b) No

9) If a plant has n poles, then a system with state variable feedback with no pole-zero cancellations will have

a) more than n poles b) less than n poles c) n poles d) it is not possible to tell

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10) (29 points) (*sisotool* problem)

Consider the plant

$$G_p(s) = \frac{50}{s^2 + 10s + 100}$$

Design a PID controller using *sisotool* with **complex conjugate zeros** so that

$$T_s \leq 2.0 \text{sec}$$

$$P.O. \leq 10\%$$

In addition, your controller must be designed so that

$$k_p \leq 1.0$$

$$k_i \leq 5$$

$$k_d \leq 0.05$$

Write your final values for k_p , k_i , k_d , and the transfer function of the controller in the space below.

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