## ECE-320, Quiz #9

1) Consider the following state variable model

$$\dot{q}(t) = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} q(t) + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u(t)$$
$$y(t) = \begin{bmatrix} 3 & 0 \end{bmatrix} q(t)$$

Assume state variable feedback of the form  $u(t) = G_{vf}r(t) - Kq(t)$  The closed loop transfer function for this system is which of the following?

a) 
$$G(s) = \frac{-6G_{pf}}{s(s-1+2k_2)-2k_1+1}$$
 b)  $G(s) = \frac{6G_{pf}}{s(s-1+2k_2)-2k_1+1}$ 

c) 
$$G(s) = \frac{6G_{pf}}{s(s-1+2k_2)+2k_1-1}$$
 d)  $G(s) = \frac{-6G_{pf}}{s(s-1+2k_2)+2k_1-1}$ 

2) Consider the following state variable model

$$\dot{q}(t) = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} q(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u(t)$$
$$y(t) = \begin{bmatrix} 1 & 0 \end{bmatrix} q(t)$$

Assume state variable feedback of the form  $u(t) = G_{pf}r(t) - Kq(t)$  Is the closed loop transfer function for this system equal to

$$G(s) = \frac{G_{pf}}{s+1+k_1}$$

a) yes b) no

3) Is the following system *controllable*?

$$G(s) = \frac{8G_{pf}}{s^2 + 12s + (k_1 + k_2 + 20)}$$

- a) Yes b) No c) impossible to determine
- 4) Is the following system controllable?

$$G(s) = \frac{G_{pf}}{s^2 + (k_2 + k_1 - 1)s + (k_2 + 2)}$$

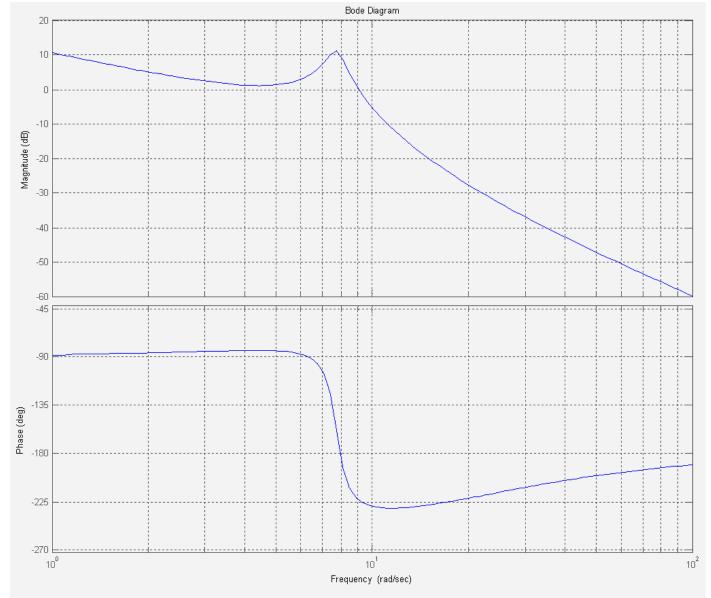
- a) Yes b) No c) impossible to determine
- 5) A system with state variable feedback has the following transfer function

$$G(s) = \frac{G_{pf}}{(s - k_1 k_2)^2}$$

Is the system controllable?

- a) Yes b) No c) impossible to determine
- 6) Consider a plant that is unstable but is a controllable system. Is it possible to use state variable feedback to make this system stable?
- a) Yes b) No
- 7) Is it possible for a system with state variable feedback to change the zeros of the plant (other than by pole-zero cancellation)?
- a) Yes b) No
- 8) Is it possible for a system with state variable feedback to introduce zeros into the closed loop system?
- a) Yes b) No
- 9) If a plant has n poles, then a system with state variable feedback with no pole-zero cancellations will have
- a) more than n poles b) less than n poles c) n poles d) it is not possible to tell

Problems 10-13 refer to the following open loop Bode plot of G(s)H(s). The frequency range is from 1 to 100 radians/sec.



10) The gain crossover frequency used to determine the phase margin for this system is best estimated as

- a) 9 rad/sec

- b) 8 rad/sec c) 7.5 rad/sec d) 1 rad/sec e) 10 rad/sec

11) The *phase crossover frequency* for this system is best estimated as

- a) 9 rad/sec b) 8 rad/sec c) 7.5 rad/sec d) 1 rad/sec
- e) 10 rad/sec

12) The phase margin for this system is best estimated as

- a)  $+45^{\circ}$  b)  $-45^{\circ}$  c)  $+135^{\circ}$  d)  $-135^{\circ}$

13) The gain margin for this system is best estimated as

a) +10 dB b) -10 dB b)  $\infty \text{ dB}$  c) 7 dB