

Name _____ CM _____

ECE 300
Signals and Systems

Exam 1
12 January, 2009

This exam is closed-book in nature. Credit will not be given for work not shown.
You may not use calculators!

Problem 1-10 _____ / 20
Problem 11 _____ / 25
Problem 12 _____ / 25
Problem 13 _____ / 30

Exam 1 Total Score: _____ / 100

Multiple Choice Questions (20 points, 2 points each)

1) For the system described by the differential equation $\dot{y}(t) - 2y(t) = x(t+1)$, the impulse response is

- a) $h(t) = e^{-2(t+1)}u(t)$ b) $h(t) = e^{2(t-1)}u(t+1)$ c) $h(t) = e^{-2(t+1)}u(t+1)$ d) $h(t) = e^{2(t+1)}u(t+1)$

2) What is the period of the periodic signal $x(t) = \sin\left(\frac{1}{2}t + \pi\right) + e^{j\frac{t}{3}}$

- a) π b) 2π c) 6π d) 12π e) none of these

3) The signal $x(t) = \cos(t)[u(t) - u(t-10)]$ is

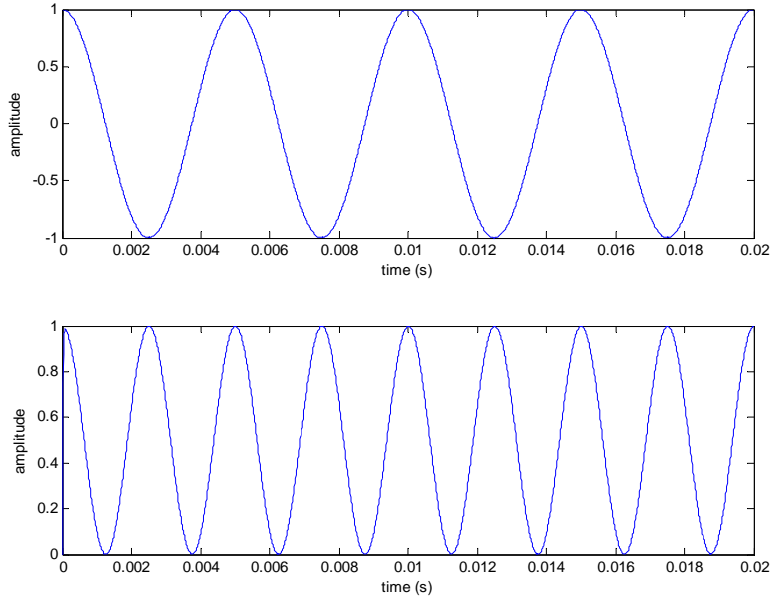
- a) a power signal b) an energy signal c) neither a power nor energy signal

4) The signal $x(t) = 2e^{j3t}$ is

- a) a power signal b) an energy signal c) neither a power nor energy signal

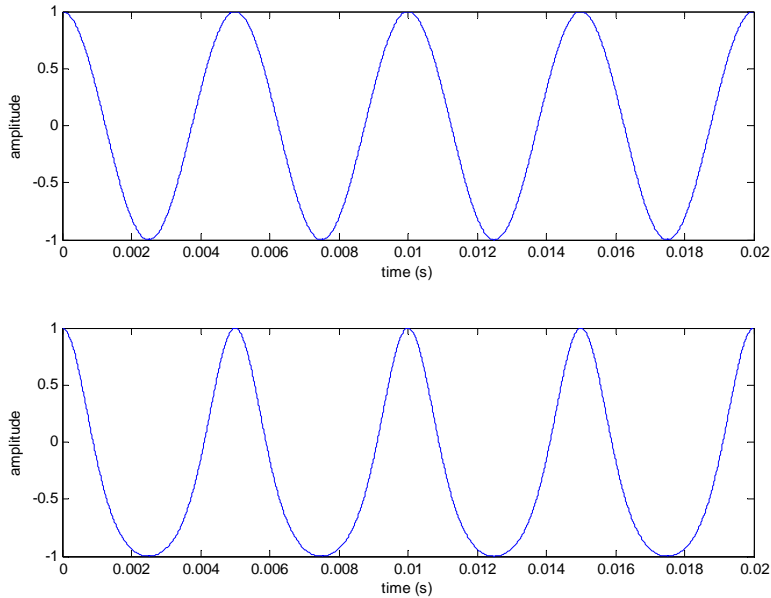
5) Consider a system with the following input (top panel) and output (bottom panel) . Is the system linear?

- a) Yes b) No c) it is not possible to determine

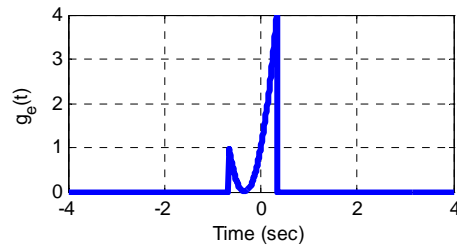
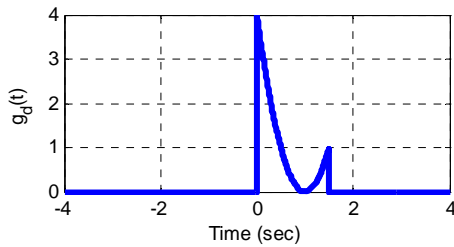
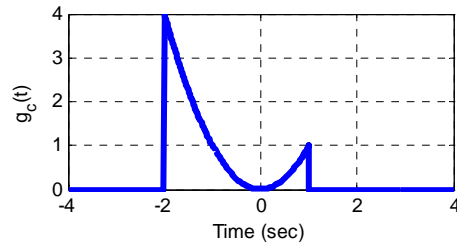
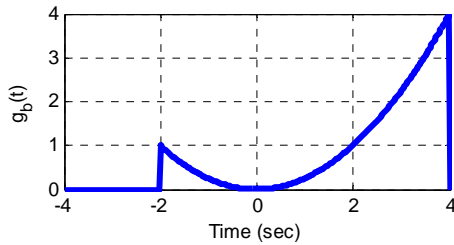
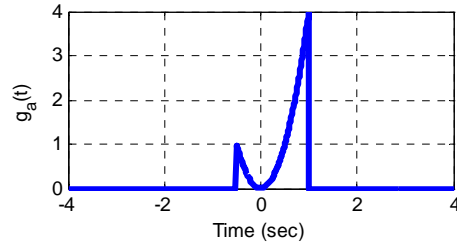
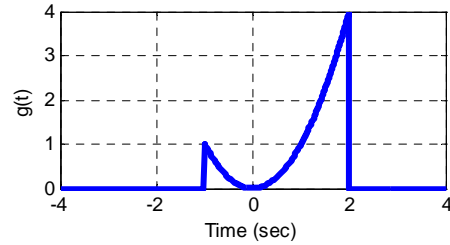


6) Consider a system with the following input (top panel) and output (bottom panel) . Is the system linear?

- a) Yes b) No c) it is not possible to determine



Problems 7-9 refer to the following signals. The original signal, $g(t)$, is in the upper left corner



7) Which signal best represents $g(-t)$?

- a) $g_a(t)$ b) $g_b(t)$ c) $g_c(t)$ d) $g_d(t)$ e) $g_e(t)$

8) Which signal best represents $g(2(1-t))$?

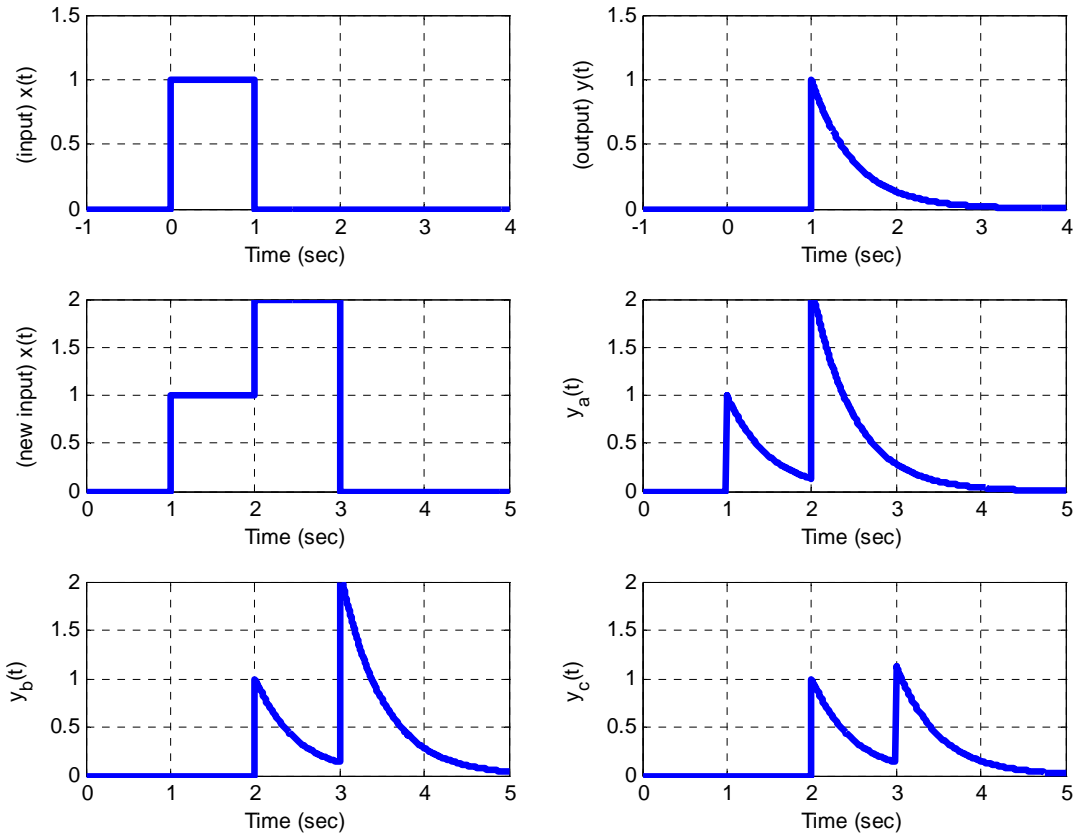
- a) $g_a(t)$ b) $g_b(t)$ c) $g_c(t)$ d) $g_d(t)$ e) $g_e(t)$

9) Which signal best represents $g\left(\frac{t}{2}\right)$?

- a) $g_a(t)$ b) $g_b(t)$ c) $g_c(t)$ d) $g_d(t)$ e) $g_e(t)$

10) Consider an LTI system with known input $x(t)$ and corresponding output $y(t)$ shown in the top row in the figure below. Assume a new input to the system, shown in the left of the middle row. The output of this LTI system will be

- a) $y_a(t)$ b) $y_b(t)$ c) $y_c(t)$ d) none of these



11. System Properties (25 points)

a) Fill in the following table with a Y (Yes) or N (No). Only your responses in the table will be graded, not any work. Assume $x(t)$ is the system input, $y(t)$ is the system output, and $h(t)$ is the impulse response for an LTI system. Also assume we are looking at all times (positive and negative times).

System	Linear ?	Time-Invariant?	Memoryless?	Causal?
$\dot{y}(t) + y(t) = x(t+1) + t$				
$y(t) = x\left(\frac{t-1}{2}\right)$				

b) Determine whether or not the following system is linear and time-invariant. You will be graded on your procedure, not just the final answer. Be sure to show your work.

$$y(t) = \int_{-\infty}^t (x(\lambda) + \lambda) d\lambda$$

12. Impulse Response (25 points)

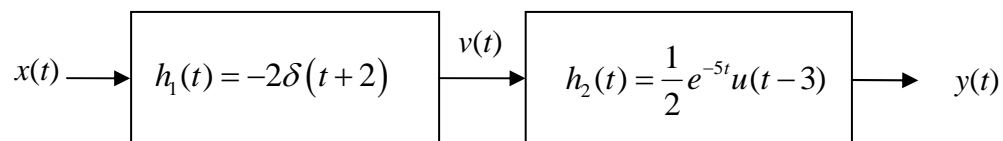
Consider the following system, composed of two subsystems each receiving $x(t)$ as their input. Assume both systems are initially at rest, both systems are causal.

- a) Determine the impulse response for each system given below

$$y(t) = \int_{-\infty}^{t-3} x(\lambda - 1) d\lambda$$

$$y(t) = 4x(t-3)$$

- b) Determine the impulse response between input $x(t)$ and output $y(t)$



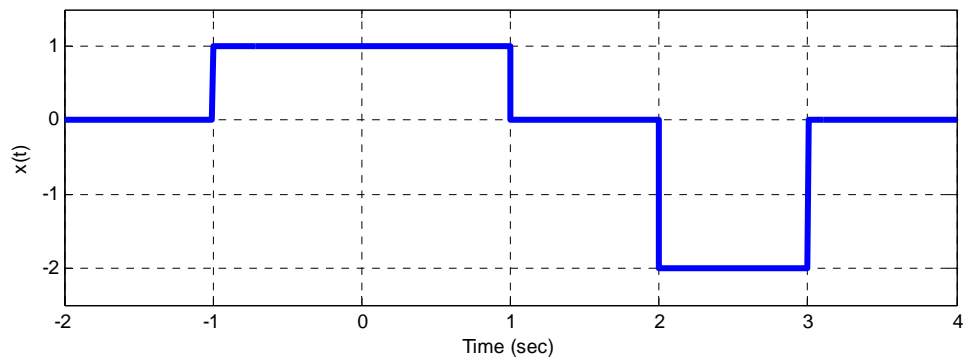
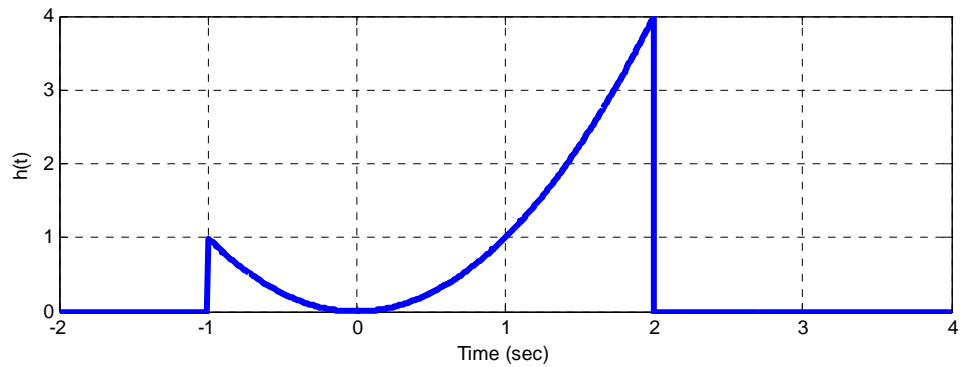
13. (30 points) Consider a causal linear time invariant system with impulse response

$$h(t) = t^2 [u(t+1) - u(t-2)]$$

The input to the system is

$$x(t) = u(t+1) - u(t-1) - 2u(t-2) + 2u(t-3)$$

These two functions are plotted below:



Using **graphical convolution**, set up the integrals to determine the output $y(t)$

Specifically, you must

- Flip and slide $h(t)$
- Show graphs displaying $h(t - \lambda)$ relative to $x(\lambda)$ for each region of interest.
- Determine the ranges of t for which each part of your solution is valid.
- Set up any necessary integrals to compute $y(t)$. Your integrals must be complete and simplified as much as possible (no unit step functions)
- **Do Not Evaluate the Integrals!!**

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Some Potentially Useful Relationships

$$E_{\infty} = \lim_{T \rightarrow \infty} \int_{-T}^T |x(t)|^2 dt = \int_{-\infty}^{\infty} |x(t)|^2 dt$$

$$P_{\infty} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T |x(t)|^2 dt$$

$$e^{jx} = \cos(x) + j \sin(x) \quad j = \sqrt{-1}$$

$$\cos(x) = \frac{1}{2} [e^{jx} + e^{-jx}] \quad \sin(x) = \frac{1}{2j} [e^{jx} - e^{-jx}]$$

$$\cos^2(x) = \frac{1}{2} + \frac{1}{2} \cos(2x) \quad \sin^2(x) = \frac{1}{2} - \frac{1}{2} \cos(2x)$$

$$\text{rect}\left(\frac{t-t_0}{T}\right) = u\left(t-t_0 + \frac{T}{2}\right) - u\left(t-t_0 - \frac{T}{2}\right)$$