

# ECE-205 : Dynamical Systems

## Homework #3

Due : **Tuesday** December 14 at the beginning of class

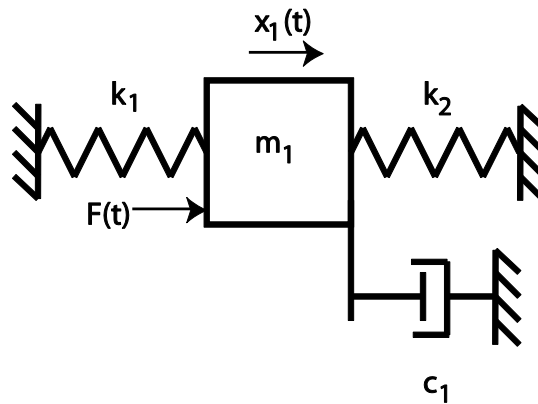
**Exam 1, Thursday December 16**

1) Problem 3.3 (From the Notes)

2) Problem 3.5 (From the Notes)

3) Problem 3.6 (From the Notes)

4) (Pre-Lab, this is part of the homework) Consider the following one degree of freedom system we will be utilizing this term:



a) Draw a free body diagram of the forces on the mass.

b) Show that the equations of motion can be written:

$$m_1 \ddot{x}_1(t) + c_1 \dot{x}_1(t) + (k_1 + k_2)x_1(t) = F(t)$$

or

$$\frac{1}{\omega_n^2} \ddot{x}_1(t) + \frac{2\zeta}{\omega_n} \dot{x}_1(t) + x_1(t) = K F(t)$$

c) What are the damping ratio  $\zeta$ , the natural frequency  $\omega_n$ , and the static gain  $K$  in terms of  $m_1$ ,  $k_1$ ,  $k_2$ , and  $c_1$ ?