## Quiz #8

Problems 1 and 2 refer to a system with poles at -2+j. -2-j. -4, -1+2j, -1-2j, and -20

- 1) The best estimate of the <u>settling time</u> for this system is
- a) 4 seconds b) 2 seconds c) 1 second d) 0.2 seconds
- 2) The **dominant pole(s)** of this system are
- a) -2+j and -2-j b) -1+2j and -1-2j c) -4 d) -20

3) How many terms will there be in the partial fraction expansion of  $H(s) = \frac{(s+1)^2}{s^2(s+2)^2}$ ? a) 2 b) 3 c) 4 d) 6

4) How many terms will there be in the partial fraction expansion of  $H(s) = \frac{s}{(s^2 + 1)(s + 2)}$ ? a) 0 b) 1 c) 2 d) 3

**5**) An impulse response h(t) is composed of the terms  $1, e^{-t}, te^{-t}$ 

A possible corresponding transfer function (for some constant value A) is

a) 
$$H(s) = \frac{A}{s(s+1)}$$
  
b)  $H(s) = \frac{A}{s^2(s+1)}$   
c)  $H(s) = \frac{As}{(s+1)}$   
d)  $H(s) = \frac{A}{s(s+1)^2}$ 

Problems 6 and 7 refer to the following transfer function

$$H(s) = \frac{2s+1}{(s+2)^2+1}$$

**6)** For this transfer function, the corresponding impulse response h(t) is composed of which terms?

a) 
$$e^{-t} \cos(2t), e^{-t} \sin(2t)$$
  
b)  $e^{-2t} \cos(t), e^{-2t} \sin(t)$   
c)  $e^{-t} \cos(4t), e^{-t} \sin(4t)$   
d)  $e^{-4t} \cos(t), e^{-4t} \sin(t)$ 

7) The **poles** of the transfer function are

a) 2 ± j	b) -2± j
c) -1 ± 2j	d) -1 ± 4j

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Problems 8 and 9 refer to the impulse responses of six different systems given below:

$$h_{1}(t) = [t + e^{-t}]u(t)$$

$$h_{2}(t) = e^{-2t}u(t)$$

$$h_{3}(t) = [2 + \sin(t)]u(t)$$

$$h_{4}(t) = [1 - t^{3}e^{-0.1t}]u(t)$$

$$h_{5}(t) = [1 + t + e^{-t}]u(t)$$

$$h_{6}(t) = [te^{-t}\cos(5t) + e^{-2t}\sin(3t)]u(t)$$

8) The number of stable systems is
a) 0 b) 1 c) 2 d) 3
9) The number of unstable systems is
a) 0 b) 1 c) 2 d) 3

10) Which of the following transfer functions represents a stable system?

$$\begin{aligned} G_a(s) &= \frac{s-1}{s+1} & G_b(s) = \frac{1}{s(s+1)} & G_c(s) = \frac{s}{s^2 - 1} \\ G_d(s) &= \frac{s+1}{(s+1+j)(s+1-j)} & G_e(s) = \frac{(s-1-j)(s-1+j)}{s} & G_f(s) = \frac{(s-1-j)(s-1+j)}{(s+1-j)(s+1+j)} \end{aligned}$$

a) all but  $G_c$  b) only  $G_a$ ,  $G_b$ , and  $G_d$  c) only  $G_a$ ,  $G_d$ , and  $G_f$ d) only  $G_d$  and  $G_f$  e) only  $G_a$  and  $G_d$ 

**11**) For the transfer function

$$H(s) = \frac{1}{s^2(s+2)}$$

the corresponding impulse response h(t) is composed of which terms?

a)  $t^2 e^{-2t}$  b) t and  $t e^{-2t}$  c)  $1, t, t e^{-2t}$ d)  $t^2, e^{-2t}$  e) none of these

**12)** The Laplace transform of x(t) = u(t) - u(t-2) is a)  $X(s) = 1 - e^{-2s}$  b)  $X(s) = 1 - e^{+2s}$  c)  $X(s) = \frac{1}{s} - \frac{e^{-2s}}{s}$  d) none of these

**13**) The Laplace transform of 
$$x(t) = te^{-3t}u(t)$$
 is  
a)  $X(s) = \frac{1}{s+3} \frac{1}{s+3}$  b)  $X(s) = \frac{1}{s+3}$  c)  $X(s) = \frac{1}{(s+3)^2}$  d)  $X(s) = \frac{2}{(s+3)^2}$ 

14) The Laplace transform of 
$$x(t) = (t-2)u(t-2)$$
 is  
a)  $X(s) = \frac{1}{s-2}$  b)  $X(s) = \frac{e^{-2s}}{s^2}$  c)  $X(s) = \frac{e^{-2s}}{s-2}$  d) none of these

## For the following three problems, the following relationship may be useful

$$T_p = \frac{\pi}{\omega_d}, T_s = \frac{4}{\sigma}, \theta = \cos^{-1}(\zeta)$$

**15)** The (dark) shaded area in the s-plane figure below shows the possible pole location for an ideal second order system that meets which of the following constraints?

a) 
$$T_s \le 1$$
 b)  $T_s \ge 1$  c)  $T_s \ge 4$  d)  $T_s \le 4$  e) none of these



**16)** Assuming we are allowed to place our poles only in the (dark) shaded areas, which of the following two shaded regions will in general result in a **smaller settling time** for our system?

a) the region in the top figure b) the region in the bottom figure



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**17)** Assuming we are allowed to place our poles only in the (dark) shaded areas, which of the following two shaded regions will in general result in a **smaller time to peak** for our system?



a) the region in the top figure b) the region in the bottom figure

**18)** One of the shaded regions below shows the possible pole locations for a percent overshoot less than 10%, and the other shows the possible pole locations for a percent overshoot less than 20%. Which of the two graphs shows the possible pole locations for a percent overshoot less than 20%?



