

ECE-205

Exam 2

Fall 2013

Calculators and computers are not allowed. You must show your work to receive credit.

Problem 1 _____/15

Problem 2 _____/17

Problem 3 _____/18

Problem 4 _____/24

Problem 5 _____/26

Total _____

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1) (15 points) Simplify the following as much as possible. Be sure to include any necessary unit step functions

$$y(t) = [t + e^t] \delta(t - 1)$$

$$y(t) = \int_{-\infty}^{t+1} \delta(\lambda + 1) d\lambda$$

$$y(t) = \int_{-t-2}^3 \delta(\lambda - 2) d\lambda$$

$$y(t) = \int_0^t e^{-(t-\lambda)} e^{-2\lambda} d\lambda$$

$$y(t) = \int_0^t e^{-3(t-\lambda)} e^{-3\lambda} d\lambda$$

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2) (17 Points) Determine the *impulse response* for the following systems. Don't forget any necessary unit step functions

a) $y(t) = x(t) + \int_{-\infty}^{t-1} x(\lambda - 2) d\lambda$

b) $y(t) = \int_{-\infty}^t e^{-(t-\lambda)} x(\lambda + 2) d\lambda$

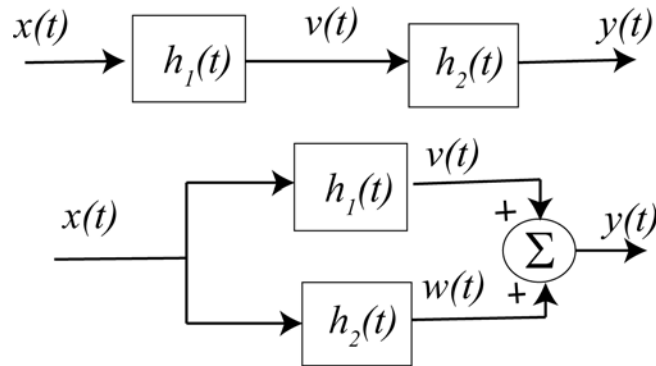
c) $\dot{y}(t) + 2y(t) = 3x(t-1)$

3) (18 points) For the following block diagram

For the following interconnected systems,

i) determine the overall impulse response (the impulse response between input $x(t)$ and output $y(t)$) and

ii) determine if the system is causal.



a) $h_1(t) = \delta(t)$, $h_2(t) = \delta(t+2)$

b) $h_1(t) = e^{-t}u(t)$, $h_2(t) = u(t-2) + \delta(t-2)$

Series Connections:

Parallel Connections:

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4) (24 points) Consider a linear time invariant system with impulse response given by

$$h(t) = e^{-t}[u(t-1) - u(t-3)]$$

The input to the system is given by two rectangular pulses, given by

$$x(t) = [u(t) - u(t-1)] + [u(t-2) - u(t-3)]$$

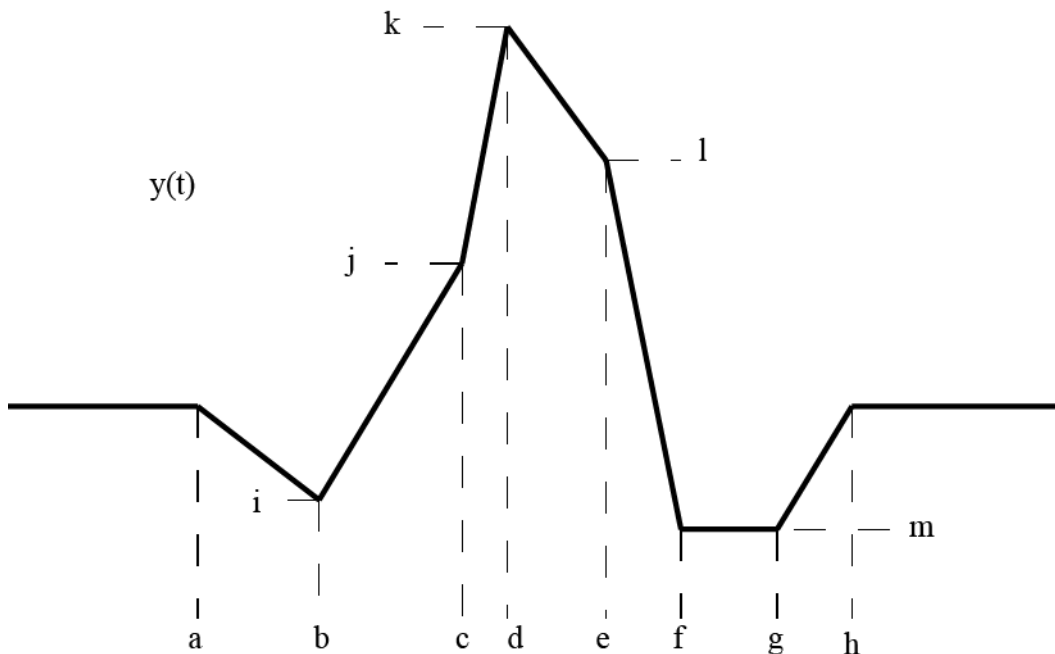
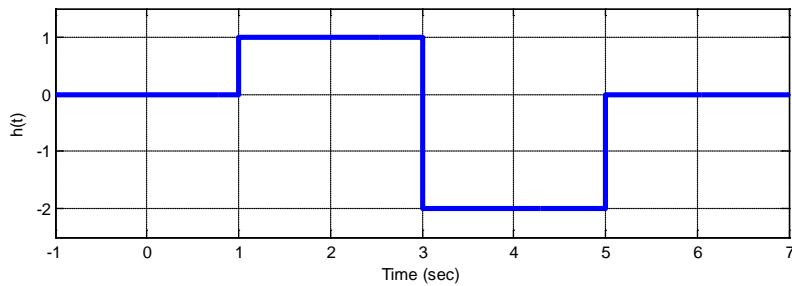
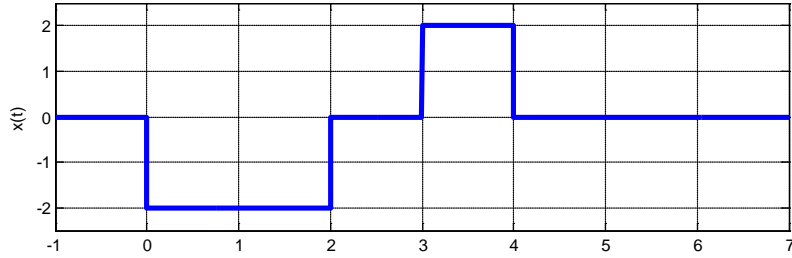
Using **graphical evaluation**, determine the output $y(t)$. Specifically, you must

- Flip and slide $h(t)$, **NOT** $x(t)$
- Show graphs displaying both $h(t - \lambda)$ and $x(\lambda)$ for each region of interest
- Determine the range of t for which each part of your solution is valid
- Set up any necessary integrals to compute $y(t)$. Your integrals must be complete, in that they cannot contain the symbols $x(\lambda)$ or $h(t - \lambda)$ but must contain the actual functions.
- Your integrals **cannot contain any unit step functions**
- **DO NOT EVALUATE THE INTEGRALS!!**

5) (26 Points) An LTI system has input, impulse response, and output as shown below. Determine numerical values for the parameters a - m . Note that parameters a - h correspond to *times*, and i - m correspond to *amplitudes*.

Hints:

- Note that the output is not drawn to scale, it just represents the general shape of the output.
- A good way to check your answer is to flip and slide one of them, then flip and slide the other one.
- It is probably much easier to get the times correct than the amplitudes.



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